



Experimental Techniques

St. Andrews, Scotland
23 Aug - 5 Sept 1998

Introduction

Observables and their Measurement

Experimental Challenge at LHC

Magnets and Muon Detectors

Electromagnetic and Hadronic Calorimetry

Inner Tracking

Signal Processing, Trigger and Data Acquisition

T. S. Virdee
CERN / Imperial College



References

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Lecture Series on LHC pp Detectors

Tracking

Calorimetry

Muon Systems

Electronics

Trigger/DAQ

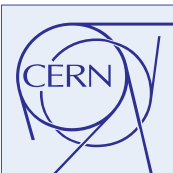
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B. Mansoulie

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G. Hall

P. Sphicas



Particle Physics

Aim to answer the two following questions:

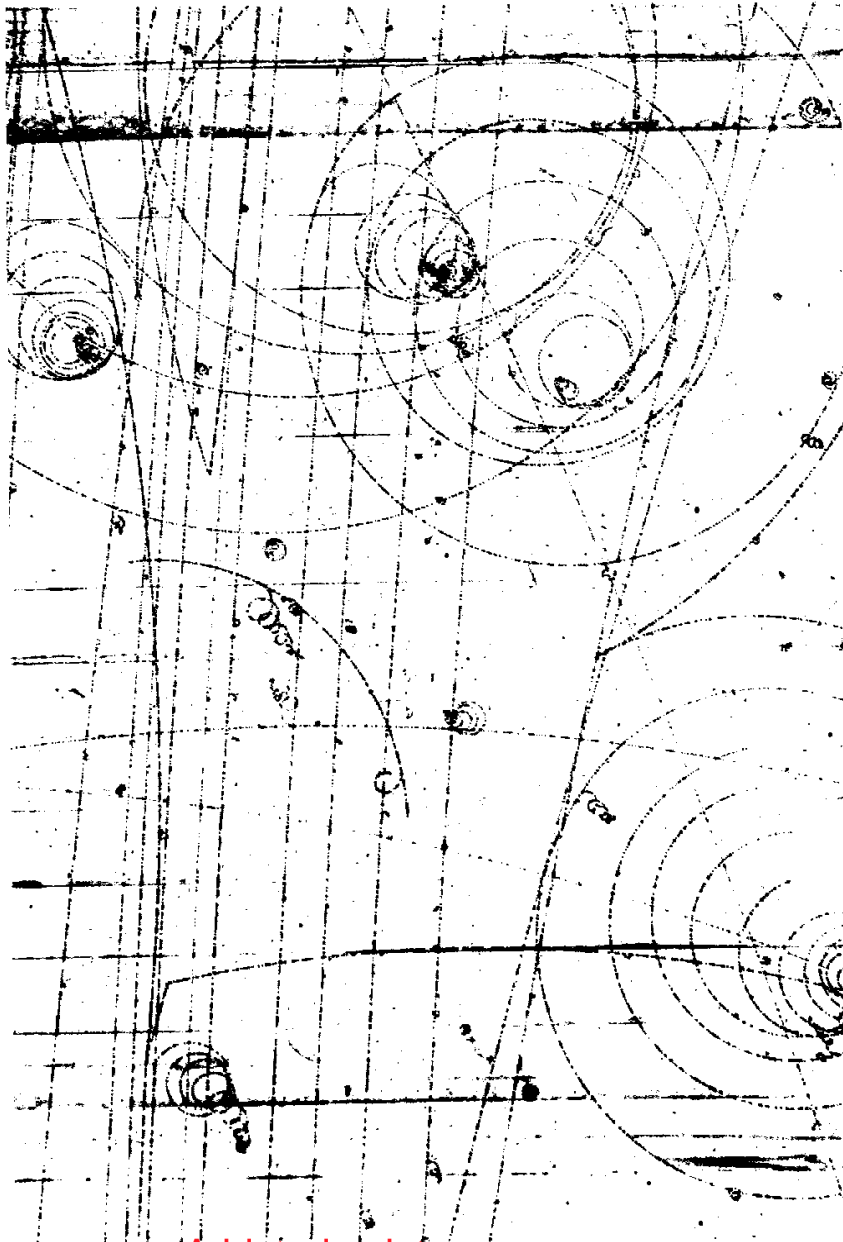
What are the **elementary constituents of matter ?**

What are the **forces that control their behaviour at the most basic level ?**

Experimentally

Aim to measure the energies, directions and identity of the products of hard interactions as precisely as possible

Bubble Chambers



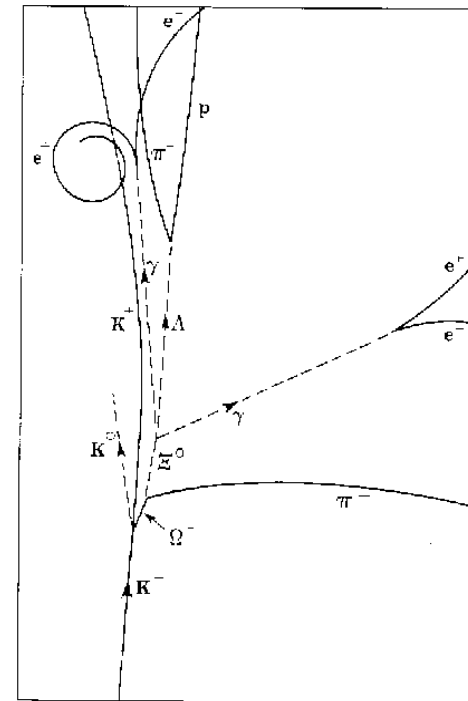
1964 : Production and decay of an Ω meson

$$K^- p \rightarrow K^0 \Omega^- K^+$$

$$\Omega^- \rightarrow \Xi^0 \pi^-$$

$$\Xi^0 \rightarrow \Lambda^0 \pi^0$$

$$\pi^0 \rightarrow \gamma \gamma$$

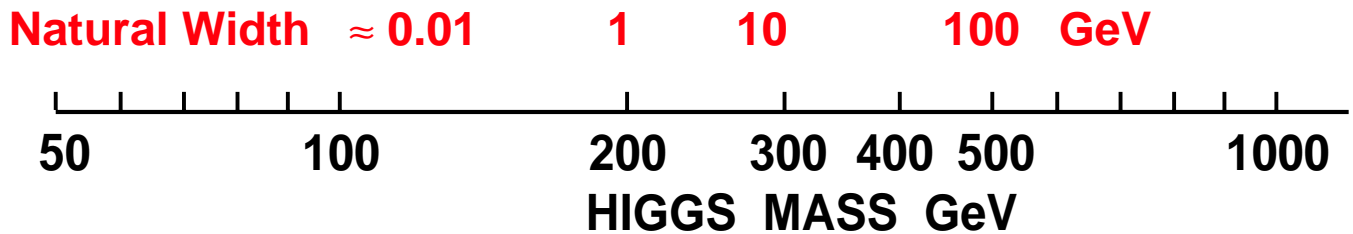




SM Higgs as a Benchmark

At the LHC the SM Higgs provides a good benchmark to test the performance of a detector

SM Higgs production at the LHC



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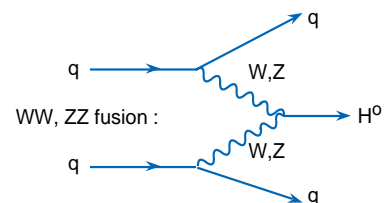
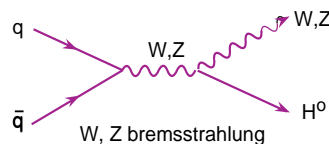
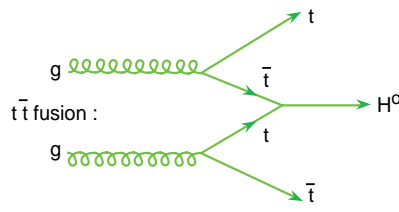
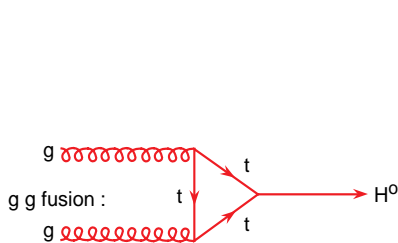
$H \rightarrow \gamma\gamma$ ($WH \rightarrow \gamma\gamma$) ($t\bar{t} H \rightarrow \gamma\gamma$)

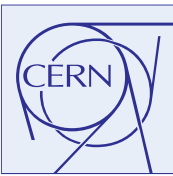
$H \rightarrow ZZ^* \rightarrow 4l$

$H \rightarrow ZZ \rightarrow 4l$

$H \rightarrow ZZ \rightarrow 2\nu + 2\mu$ or $2e$

$H \rightarrow WW$ or $ZZ jj \rightarrow 2ljj$





Reaction Rates

Colliders

Reaction rate, $R = \sigma L$

where σ is the cross-section (in units of cm^2) and L is the 'luminosity' (in units of $\text{cm}^{-2}\text{s}^{-1}$)

For two oppositely moving beams of relativistic particles

$$L = f \cdot n \frac{N_1 N_2}{A}$$

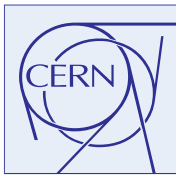
where N_1, N_2 are no, of particles in each bunch,

n is the number of bunches in either beam around the ring,

A is the cross-sectional area of the beams assuming complete overlap, and f is the revolution frequency

e.g. at LHC, $N_1, N_2 \approx 10^{11}$ protons, $n = 2835$, transverse <radius> $\approx 20\mu\text{m}$, $f \approx 10^4$ giving $L \approx 10^{34} \text{ cm}^{-2}\text{s}^{-1}$.

Since $\sigma \approx 100 \text{ mb}$, $R \approx 10^9$ interaction/s



Interaction of Radiation with Matter



Observables

Use the example of SM Higgs production
at the LHC

Muons and electrons

SM, MSSM : $H \rightarrow Z Z^*$ or $ZZ \rightarrow 4l$ or $2e 2\mu$

$Z' \rightarrow 2l$ and F-B asymmetry

Photons

SM, MSSM : $H \rightarrow 2\gamma$

Jets

Jet tagging : high mass Higgs, strong WW scattering

Missing E_t

SM : $H \rightarrow ZZ \rightarrow 2e 2\nu$, MSSM : gluinos, squarks

b-Jets

b-jet tagging: SUSY gluino and squark cascade
decays, $H \rightarrow bb$, CP violation

Taus

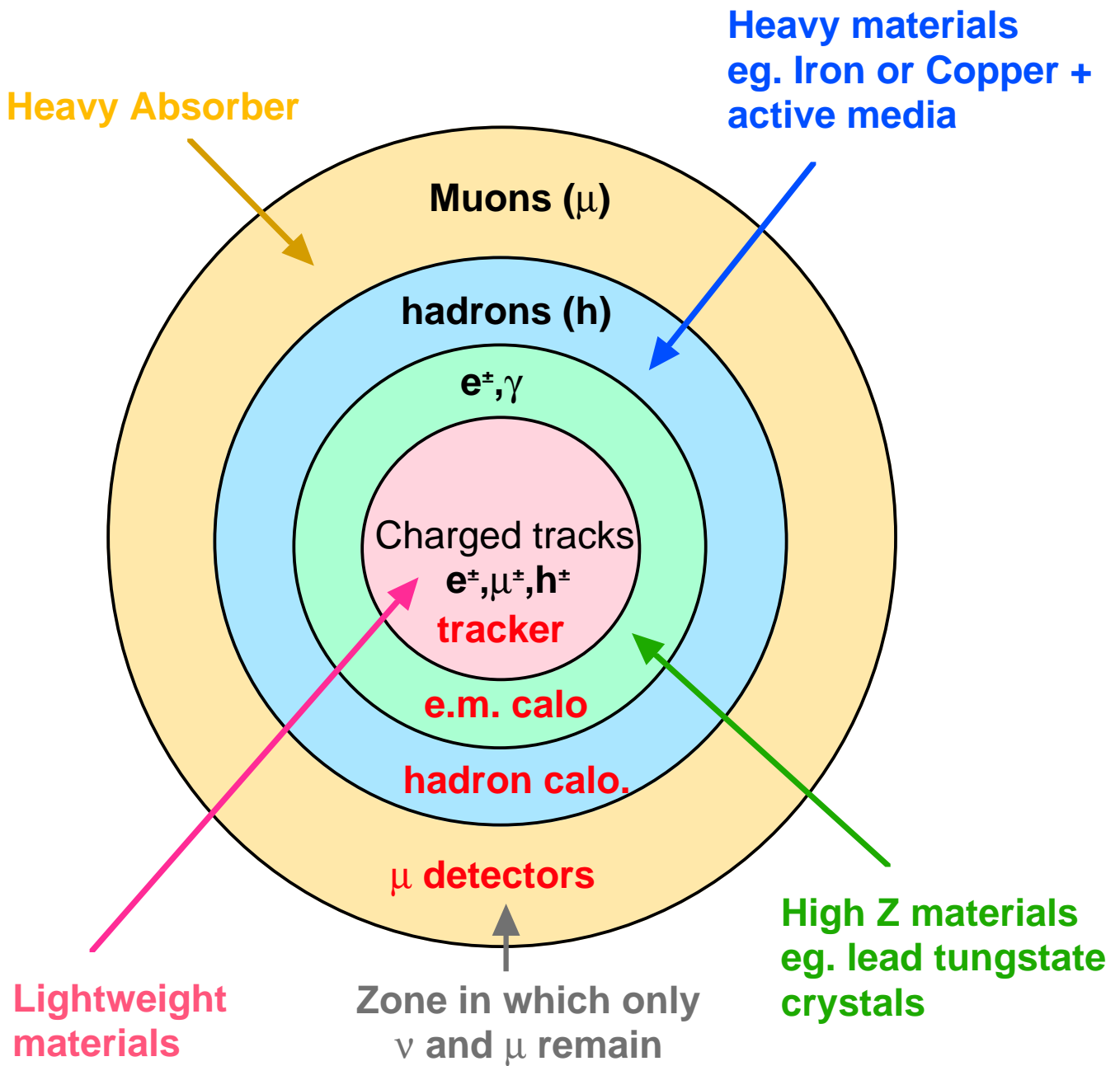
MSSM : $H^+ \rightarrow \tau\nu$, A^0, h^0 and $H^0 \rightarrow \tau\tau$

π^\pm and K^0

CP violation



Onion-like Structure of HEP Experiments



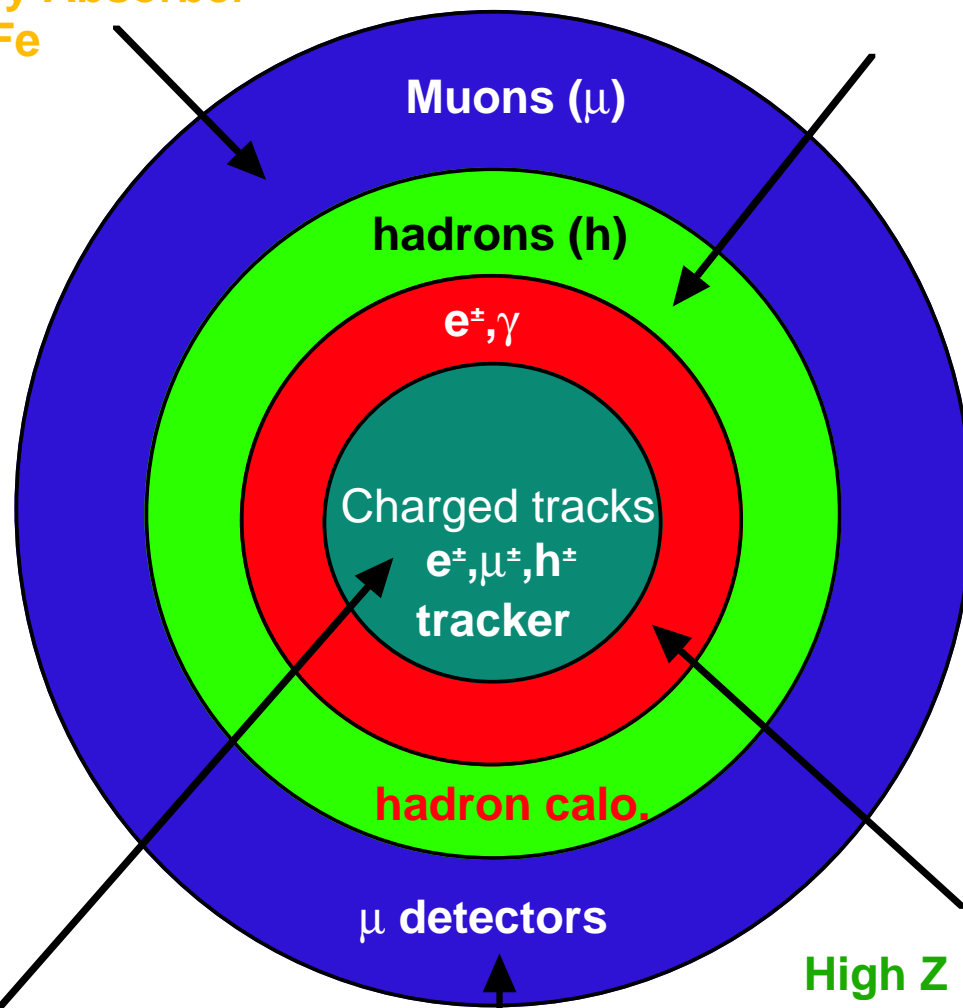
Each layer identifies and measures (or remeasures) the energy of particles unmeasured by the previous layer



Onion-like Structure of HEP Experiments

Heavy Absorber
e.g. Fe

Heavy materials
eg. Iron or Copper +
active media

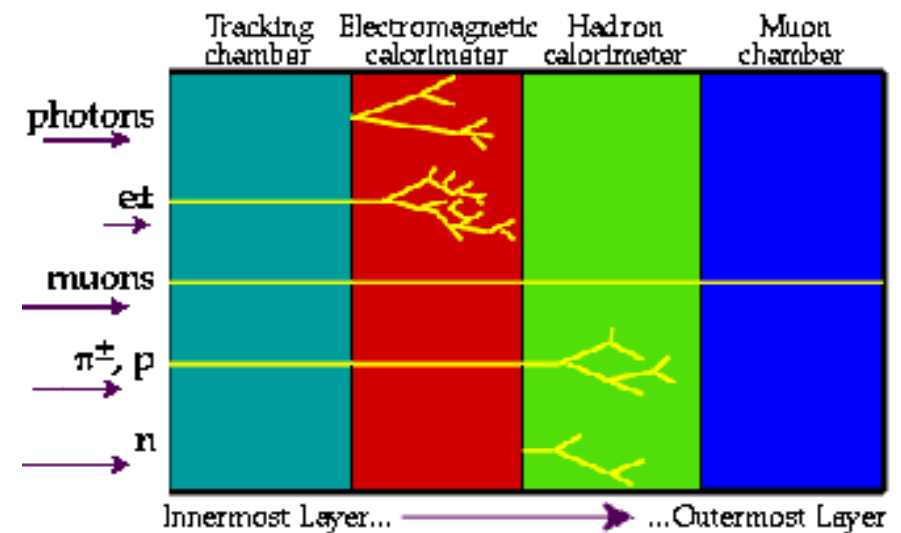


Lightweight
materials

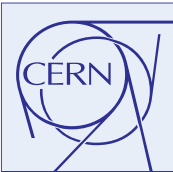
Zone in which only
 ν and μ remain

High Z materials
eg. lead tungstate
crystals

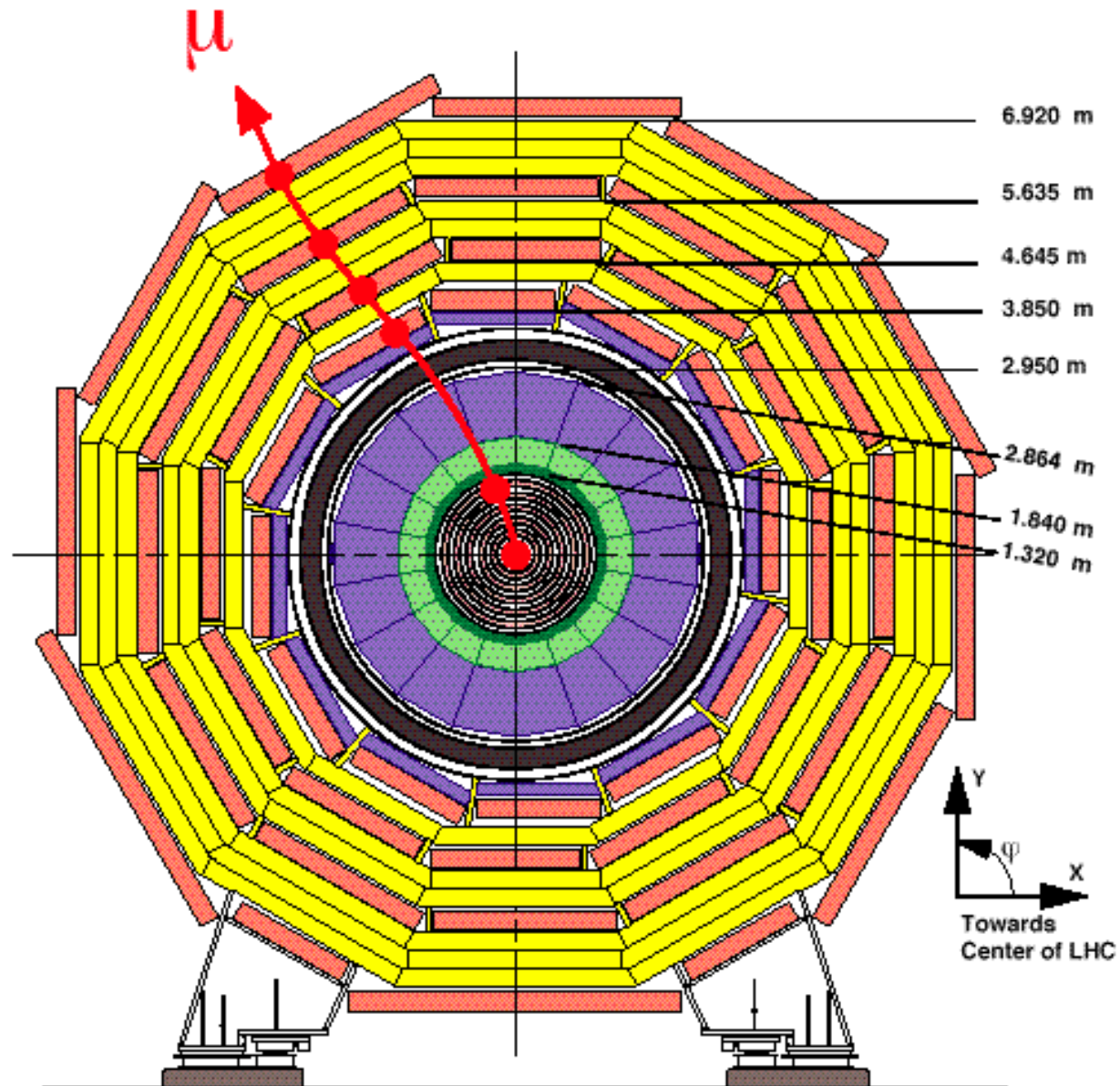
Each layer identifies and measures
(or remeasures) the energy of particles
unmeasured by the previous layer



No single detector can determine
identity and measure
energies/momenta of all particles



Transverse View of CMS



CMS-TS-00079



Experimental Measurements

Measurement of Momentum

Charged particle in a magnetic field

Multiple scattering

Measurement of Energy

characteristics of e.m. cascades

characteristics of hadronic cascades

e.m energy resolution

homogeneous calorimeters

sampling calorimeters

hadronic energy resolution

energy measurement of jets

Identification of Particles

electrons, photons

pions / kaons / protons

muons

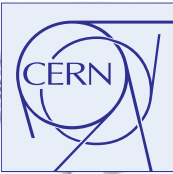
b-jets

neutrinos (and jets)

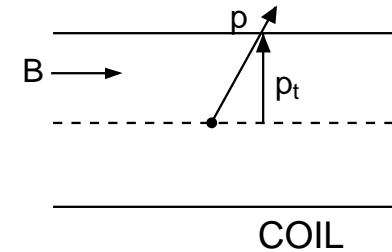
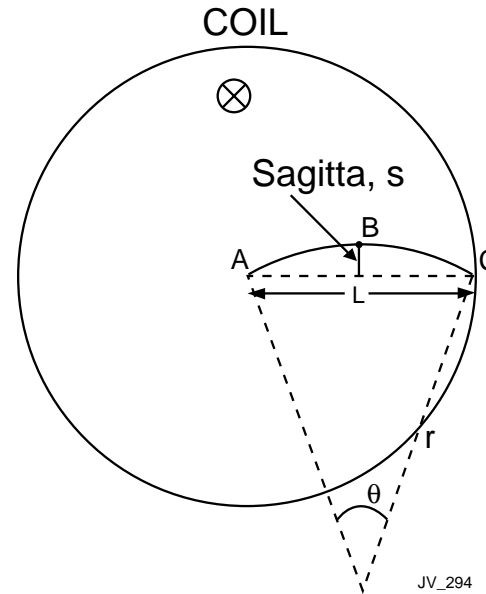


Measurement of Momentum

- Charged Particle in a Magnetic Field
- Relative Momentum Resolution
- Multiple Scattering



Charged Particle in a Magnetic Field



Radius of curvature

$$r = \frac{p_T}{0.3B}$$

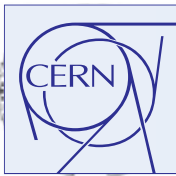
If $r \gg L$ then

$$\sin \frac{\theta}{2} = \frac{L}{2r} \Rightarrow \frac{\theta}{2} \approx \frac{L}{2r} \Rightarrow \theta \approx \frac{0.3BL}{p_T}$$

Sagitta

$$\begin{aligned} s &= r - r \cos(\theta/2) \\ &\approx r \left[1 - \left(1 - \frac{1}{2} \frac{\theta^2}{4} \right) \right] \\ &= \frac{r\theta^2}{8} \approx \frac{0.3BL^2}{8p_T} \end{aligned}$$

e.g. $s \approx 3.75$ cm
for $p_T = 1$ GeV/c, $L = 1$ m and $B = 1$ T



Relative Momentum Resolution

$$\frac{dp_T}{p_T} = \frac{\sigma_s}{s} = \frac{\sqrt{(3/2)} \sigma_x}{s}$$
$$\frac{dp_T}{p_T} = \frac{\sqrt{3}}{2} \sigma_x \frac{8p_T}{0.3BL^2} \quad (2)$$

Momentum resolution degrades linearly with increasing momentum, improves for higher field and the larger radial size of tracking cavity (quadratic in L)

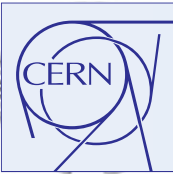
Arrangement of measuring points

Uniform spacing

$$\frac{dp_T}{p_T} = \frac{\sigma_x p_T}{0.3BL^2} \sqrt{\frac{720}{N+4}}$$

e.g. $dp_T/p_T \approx 0.5\%$ for $p_T=1$ GeV/c, $L=1$ m, $B=1$ T, $\sigma_x = 200$ μ m and $N=10$

BUT in a real tracker errors due to multiple scattering has to be included .



Multiple Scattering

- Electric field close to atomic nucleus may give large acceleration to a charged particle.
- For a heavy charged particle ($m \geq m_\mu$) results in a change of direction

Small impact parameter

single large angle scatter can occur (Rutherford Scattering)

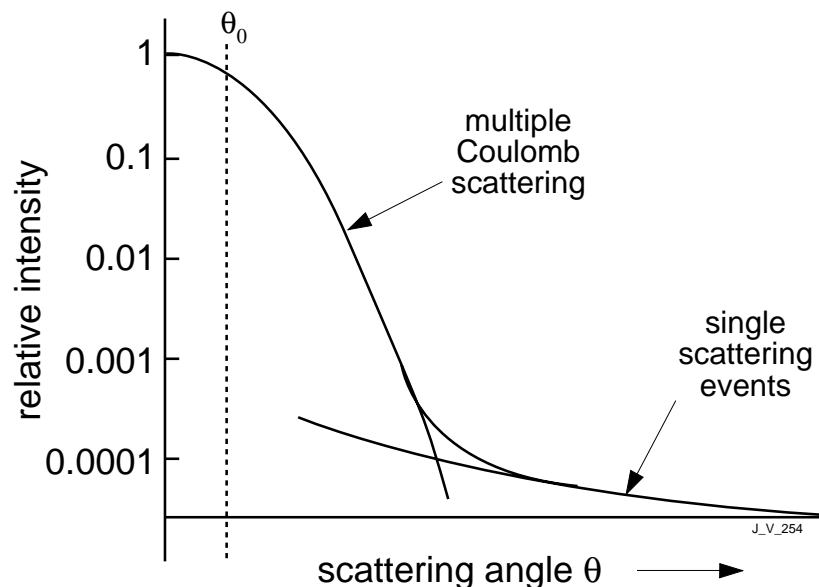
$$\frac{d\sigma}{d\Omega} \propto \frac{1}{\sin^4 \theta / 2}$$

Large impact parameter

- more probable

nuclear charge partly screened by atomic electrons, scattering angle is small

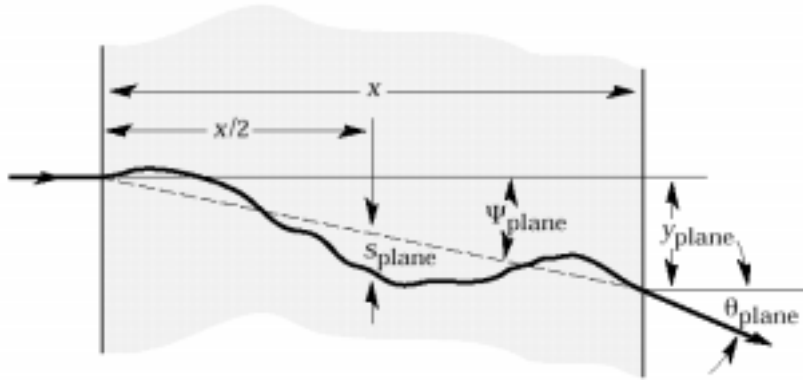
- thick material \rightarrow large no. of random and small deflections - **multiple Coulomb scattering**



rms of scattering angle

$$\theta_0 \approx \frac{13.6 \text{ MeV}}{\beta pc} Z_{inc} \sqrt{\frac{L}{X_0}}$$

Multiple Scattering



s_p - sagitta in plane

Figure 23.5: Quantities used to describe multiple Coulomb scattering. The particle is incident in the plane of the figure.

Apparent sagitta due to multiple scattering $s_p = \frac{L\theta_0}{4\sqrt{3}}$

If extrapolation error from one plane to next is larger than the point resolution then momentum resolution is degraded i.e. if

$$\theta_0 \Delta r > \sigma_x$$

Relative momentum resolution due to multiple scattering is

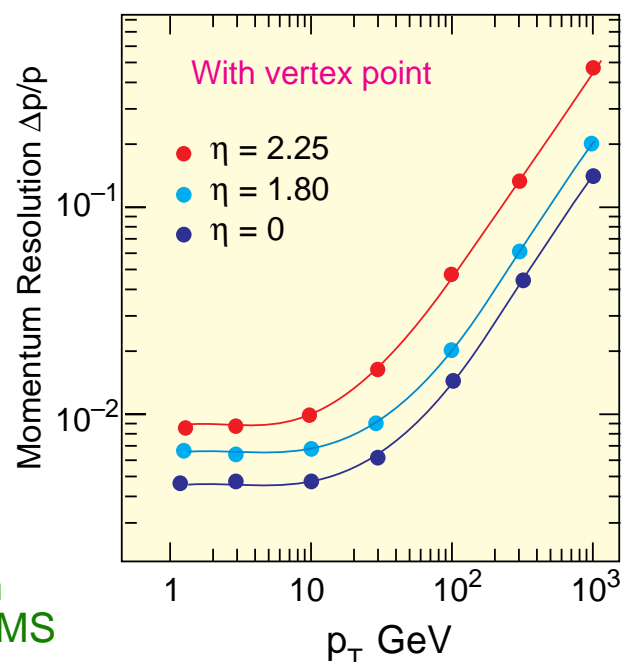
$$\therefore \frac{s_p}{s} = \frac{dp}{p} \Big|_{ms} \approx 0.05 \frac{1}{B\sqrt{LX_0}} \quad \text{since } s = \frac{0.3BL^2}{8p} \quad \begin{array}{l} B \text{ in T,} \\ L \text{ and } X_0 \text{ in m} \end{array}$$

i.e. Resolution is independent of p and $\propto 1/B$

e.g. argon gas, $L = 1 \text{ m}$, $B = 1 \text{ T}$

$$\frac{dp}{p} \Big|_{ms} \approx 0.5\%$$

Estimated Momentum Resolution v/s p_T in CMS





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characteristics of hadronic cascades

e.m energy resolution

homogeneous calorimeters

sampling calorimeters

hadronic energy resolution

energy measurement of jets

Identification of Particles

electrons, photons

pions / kaons / protons

muons

b-jets

neutrinos (and jets)



What is a Calorimeter

Neutral and charged particles incident on a block of material deposit their energy through destruction and creation processes

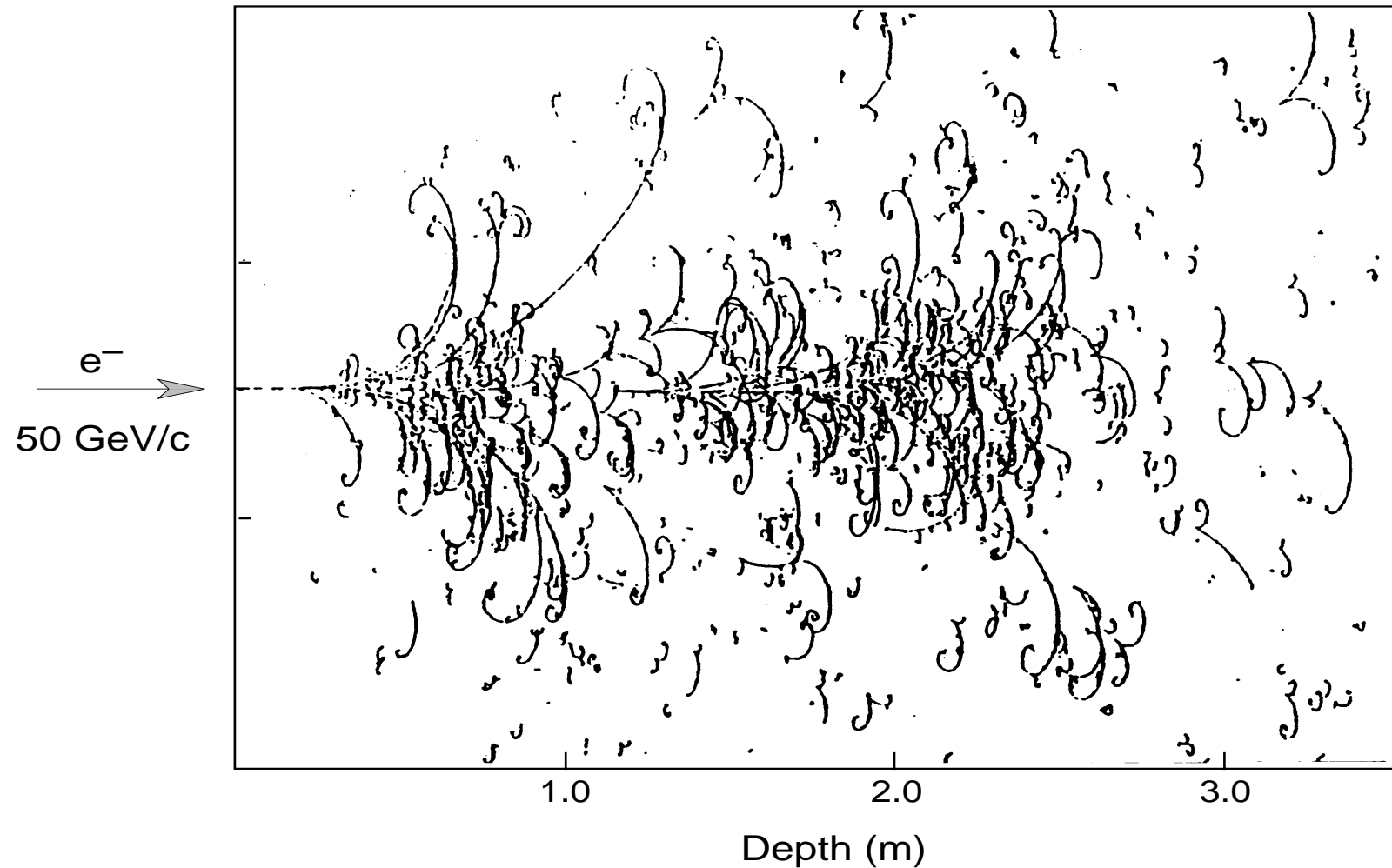
The deposited energy is rendered measurable by ionisation or excitation of the atoms of matter in the active medium.

The active medium can be the block itself (**totally active or homogeneous calorimeter**) or a sandwich of dense absorber and light active planes (**sampling calorimeters**).

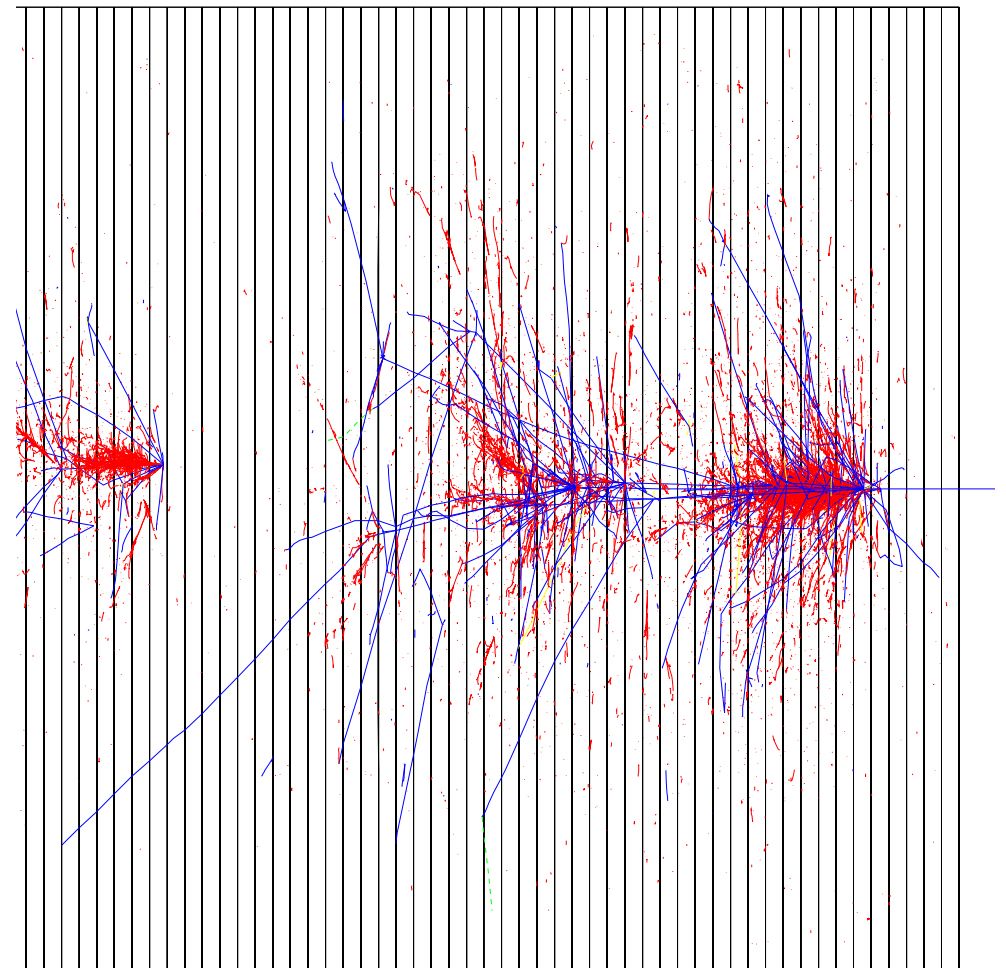
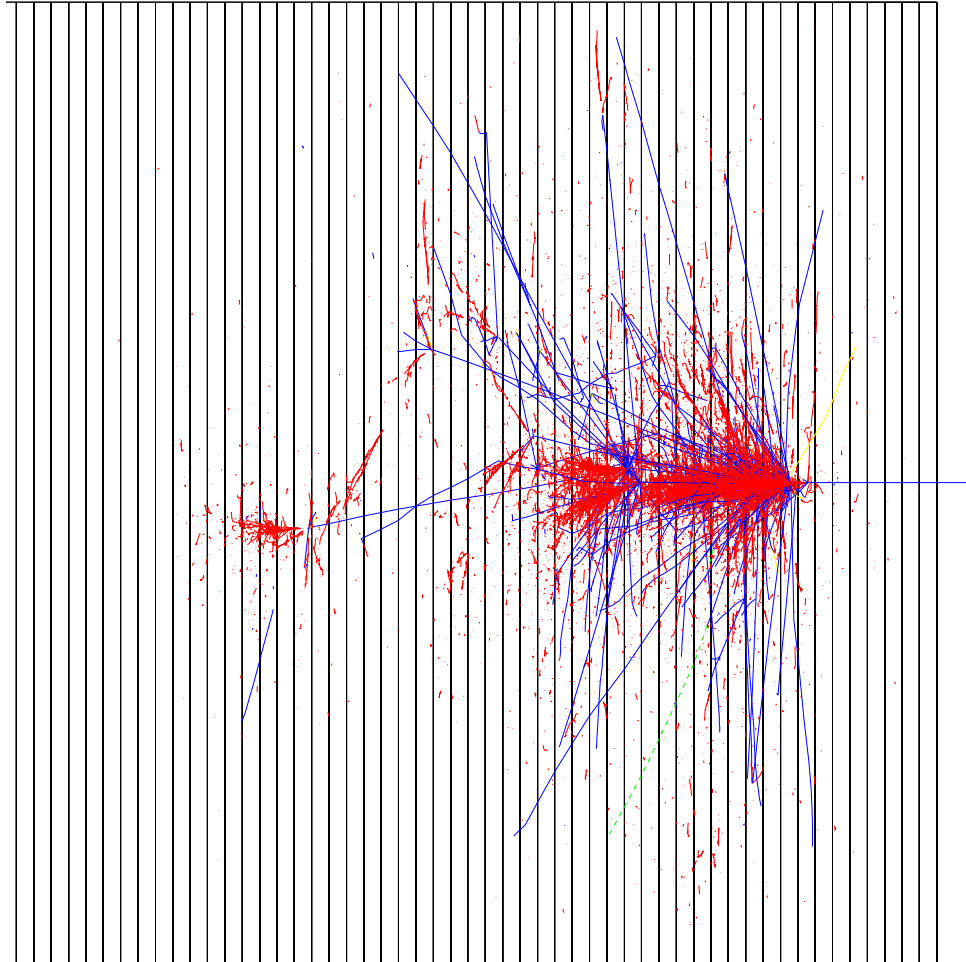
The measurable signal is usually linearly proportional to the incident energy.

An Electron Shower in a Bubble Chamber

Big European Bubble Chamber filled with Ne:H₂ = 70%:30%,
3T Field, L=3.5 m, X₀≈34 cm, 50 GeV incident electron



Hadron Showers in Copper



red - e.m. component
blue - charged hadrons

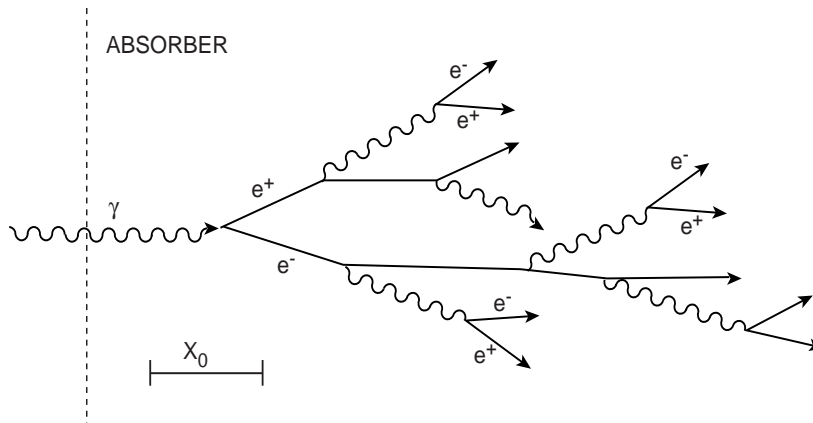


The Electromagnetic Cascade

- em Cascade - Longitudinal Development
- Radiation Length
- Critical Energy and Moliere Radius
- e.m. Cascade - Longitudinal Development
- e.m. Cascade - Longitudinal Development

em Cascade - Longitudinal Development

A high energy e or γ incident on a thick absorber initiates a cascade of e^\pm 's, γ 's via bremsstrahlung and pair production. With increasing depth the number of secondary particles increases while their mean energy decreases.



JV217.c

The multiplication continues until the energies fall below the **critical energy** ϵ . Further dissipation of energy is dominated by ionization or excitation rather than generation of more shower particles.

Consider a simplified model of shower development for e/γ of energy E . It is convenient to describe shower development using scaled variables

$$t = \frac{x}{X_0} \quad \text{and} \quad y = \frac{E}{\epsilon}$$

In one **radiation length**, $1 X_0$, an electron loses about 2/3rd of its energy and a high energy photon has a probability of 7/9 of pair conversion

Naively take X_0 as a generation length.

Assume that after each generation the number of particles increases by a factor of 2.

After t generations, *energy of particles* $e(t) = \frac{E}{2^t}$

number of particles $n(t) = 2^t$



Radiation Length

In dealing with electrons and photons at high energies striking blocks of materials (e.g. calorimeters) it is convenient to measure the depth and radial extent of the resulting cascades in terms of :
Radiation Length (X_0) and Molière Radius (R_M)

Consider the bremsstrahlung process

A free electron cannot radiate a photon. In classical electromagnetism a charged particle emits radiation when it is subjected to acceleration or deceleration. The acceleration/deceleration is greater if the particle is lighter.

$$-\left. \frac{dE}{dx} \right|_{rad} = \left[4n \frac{Z^2 \alpha^3 (\hbar c)^2}{m_e^2 c^4} \ln \frac{183}{Z^{1/3}} \right] E$$

$$-\frac{dE}{dx} \propto E \Rightarrow \frac{dE}{E} = -A dx \Rightarrow E = E_0 e^{-Ax}$$

where A is a constant.

Thus, on average, the distance over which the electron loses all but 1/e of its energy, called the radiation length X_0 ($=1/A$), is

$$X_0 = \left[4n \frac{Z^2 \alpha^3 (\hbar c)^2}{m_e^2 c^4} \ln \frac{183}{Z^{1/3}} \right]^{-1}$$

e.g. for Pb, $Z = 82$, $n = 3.3 \cdot 10^{28} / \text{m}^3$

$X_0 \sim 5.3 \text{ mm}$ which is close to 5.6 mm in PDG

$$\frac{dE}{dx} = -\frac{E}{X_0} \quad \text{and} \quad X_0 \approx \frac{180A}{Z^2} \text{ g.cm}^{-2}$$



Critical Energy and Moliere Radius

Critical Energy, ϵ

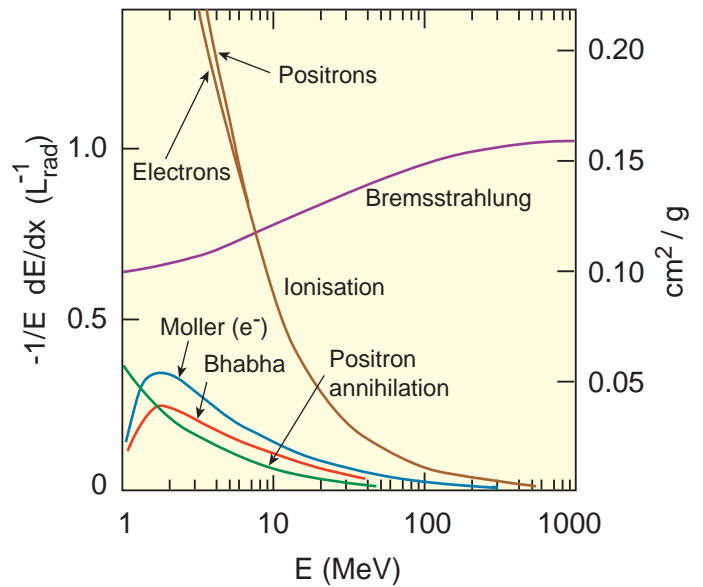
Defined to be the energy at which the energy loss due to ionisation* (at its minimum i.e. $\beta \approx 0.96$) and radiation are equal (over many trials)

$$i.e. \frac{(dE/dx)_{rad}}{(dE/dx)_{ion}} = 1$$

$$\Rightarrow \epsilon = \frac{560}{Z} \quad (E \text{ in MeV})$$

PDG gives $\epsilon = 610/(Z+1.24)$

Fractional Energy Loss by Electrons



Moliere Radius, R_M

This gives the average lateral deflection of critical energy electrons after traversing 1 X_0 and can be parameterised as :

$$R_M = \frac{X_0 E_s}{\epsilon} = \frac{21_{MeV} X_0}{\epsilon} \approx \frac{7A}{Z} \text{ g.cm}^{-2}$$

	Z	ρ g.cm ⁻³	I/Z eV	(1/ ρ) dT/dx MeV/g.cm ⁻²	X_0 cm	ϵ MeV	λ_{int} cm
C	6	2.2	12.3	1.85	~19	103	38.1
Al	13	2.7	12.3	1.63	8.9	47	39.4
Fe	26	7.87	10.7	1.49	1.76	24	16.8
Pb	82	11.35	10.0	1.14	0.56	6.9	15.1
U	92	18.7	9.56	1.10	0.32	6.2	10.5

* $-\frac{dE}{dx}|_{ion} = N_A \frac{Z}{A} \frac{4\pi\alpha^2(\hbar c)^2}{m_e c^2} \frac{Z_i^2}{\beta^2} \left[\ln \frac{2m_e c^2 \gamma^2 \beta^2}{I} - \beta^2 - \frac{\delta}{2} \right]$



e.m. Cascade - Longitudinal Development

At shower max. where $e \sim \epsilon$

$$\text{no. of particles } n(t_{\max}) \approx \frac{E}{\epsilon} = y$$

$$\text{and } t_{\max} \approx \ln \frac{E}{\epsilon} = \ln y$$

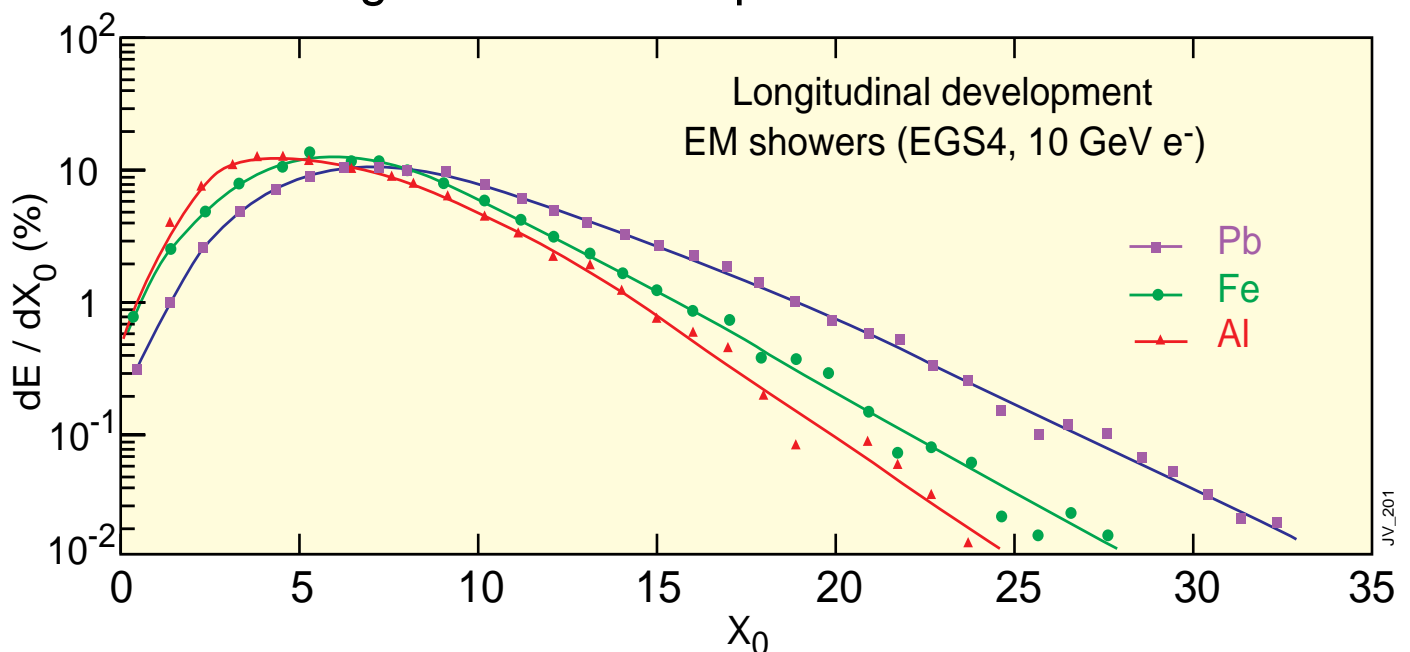
After shower maximum

Critical energy electrons do not travel far ($\sim 1 X_0$) and the remaining energy of the cascade is carried forward by photons giving the typical exponential falloff of energy deposition caused by attenuation of γ 's .

Longitudinal development of 10 GeV showers in Al, Fe and Pb.

It can be noted that the shower max. is deeper for higher Z materials because multiplication continues down to lower energies. The slower decay beyond the max. is due to the lower energies at which electrons can still radiate. Both of the above are due to lower ϵ for higher Z materials.

Longitudinal Development EM Shower



Need a depth of $> 25 X_0$ to contain high energy em showers



e.m. Cascade - Longitudinal Development

Mean longitudinal profile of energy deposition is given by

$$\frac{dE}{dt} = Eb \frac{(bt)^{a-1} e^{-bt}}{\Gamma(a)}$$

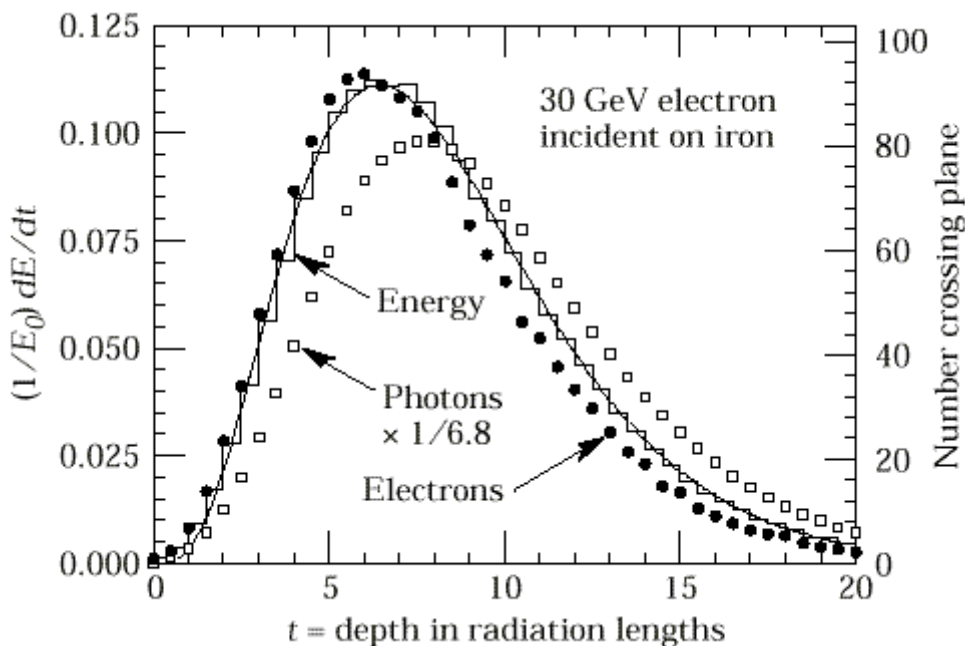
The maximum occurs at $t_{\max} = (a-1) / b$

Fits to t_{\max} give $t_{\max} = \ln y - 0.5$ for e-induced cascades
and $t_{\max} = \ln y + 0.5$ for γ -induced cascades

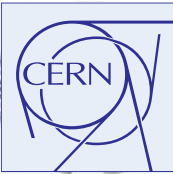
Coefficient a can be found using t_{\max} and assuming $b \sim 0.5$.

The photon showers are longer since the energy deposition only starts after the first pair conversion has taken place. The mean free path length for pair conversion of a high energy photon is

$$X_{\gamma} = \frac{9}{7} X_0 \quad \text{i.e. Prob. of conversion is } e^{-\frac{7}{9} X_0}$$



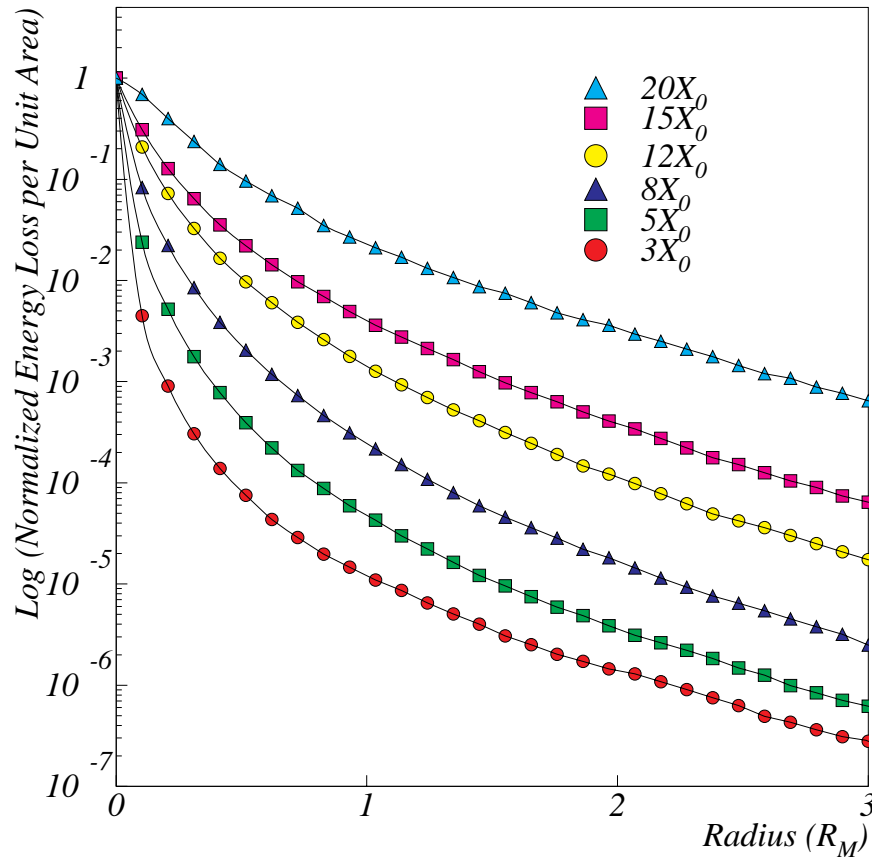
NB. The gamma distribution is flat near the origin while the EGS4 cascade (or a real cascade) increases more rapidly. As a result the above formulas fails badly for about the first two X_0 .



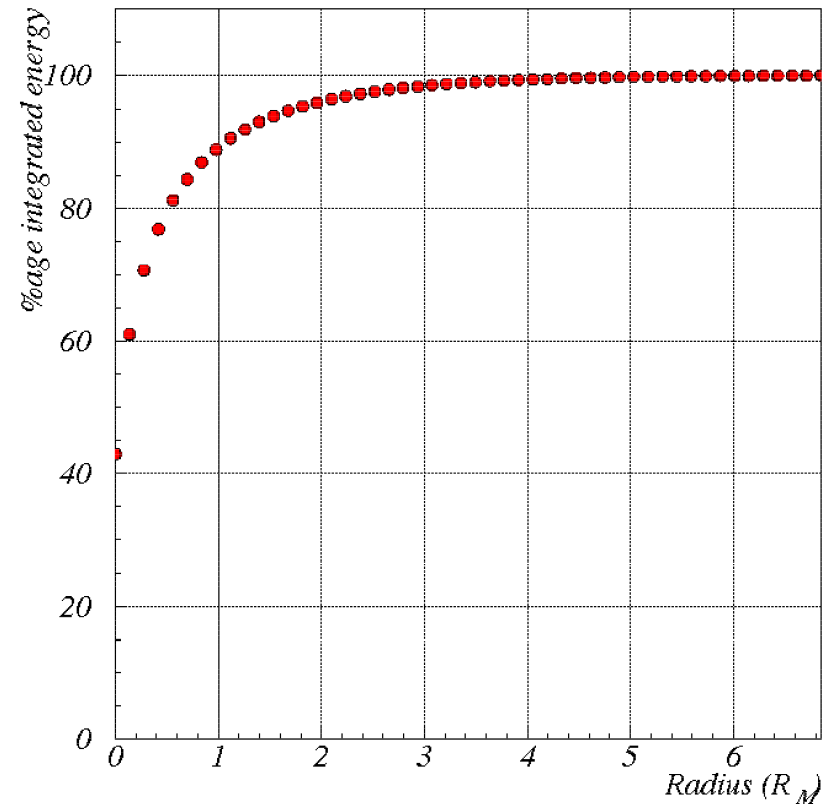
e.m. Cascade - Lateral Development

The lateral spread of an e.m. shower is determined by multiple scattering of e^\pm away from the shower axis and by minimally attenuated photons

50 GeV electrons in $PbWO_4$



50 GeV electrons in $PbWO_4$



An infinite cylinder with a radius of $2R_M$ contains $\approx 95\%$ of the shower energy.

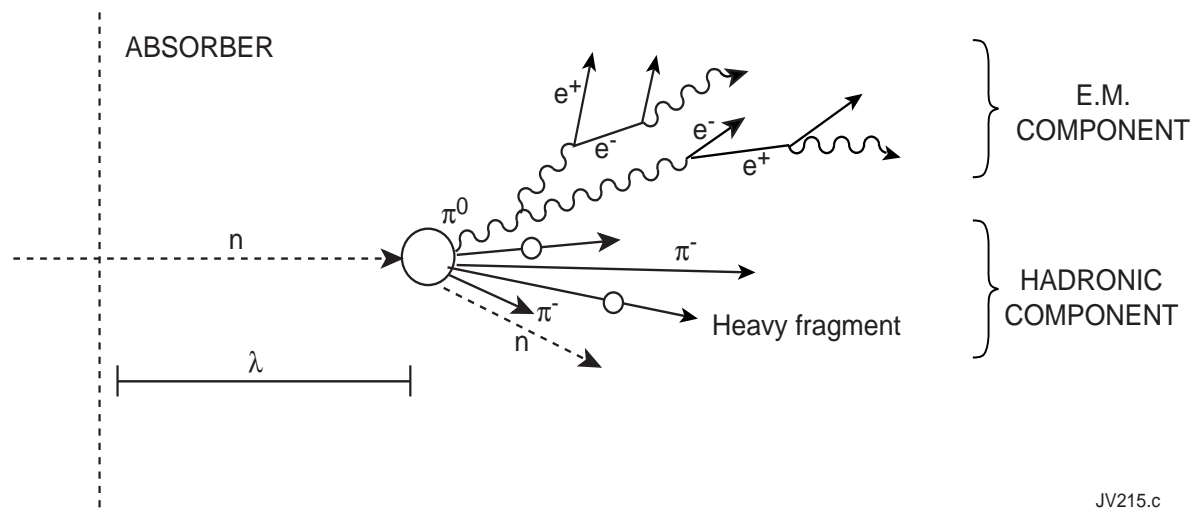


The Hadronic Cascade

- Hadronic Cascade
Longitudinal Development

Hadronic Cascade Longitudinal Development

- A situation analogous to that for em showers exists. The interaction responsible for shower development is the strong one instead of Coulomb.
- A high energy hadron striking an absorber interacts with a nucleus leading to multi-particle production consisting of mesons (e.g. π^\pm , π^0 , K etc.). The hadrons in turn interact with further nuclei leading to a growth in the number of secondary particles.
- Nuclei may breakup leading to spallation neutrons.
- Multiplication continues until the pion production threshold (E_{th}) is reached.



Simple model treats interaction on a black disc of radius R

$$\sigma_{int} = \pi R^2 \propto A^{2/3}$$

In fact $\sigma_{inel} = \sigma_0 A^{0.7}$ where $\sigma_0 = 35 \text{ mb}$

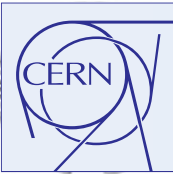
the nuclear interaction length $\lambda_{int} = \frac{A}{N_A \sigma_{int}} \propto A^{1/3}$

Total multiplicity, $n \propto \ln E$

c.m. energy goes into KE of secondaries rather than straight particle production which would imply $n \propto \sqrt{s}$

The secondaries are produced with a limited transverse momentum

$$\langle p_T \rangle \approx 300-400 \text{ MeV}$$



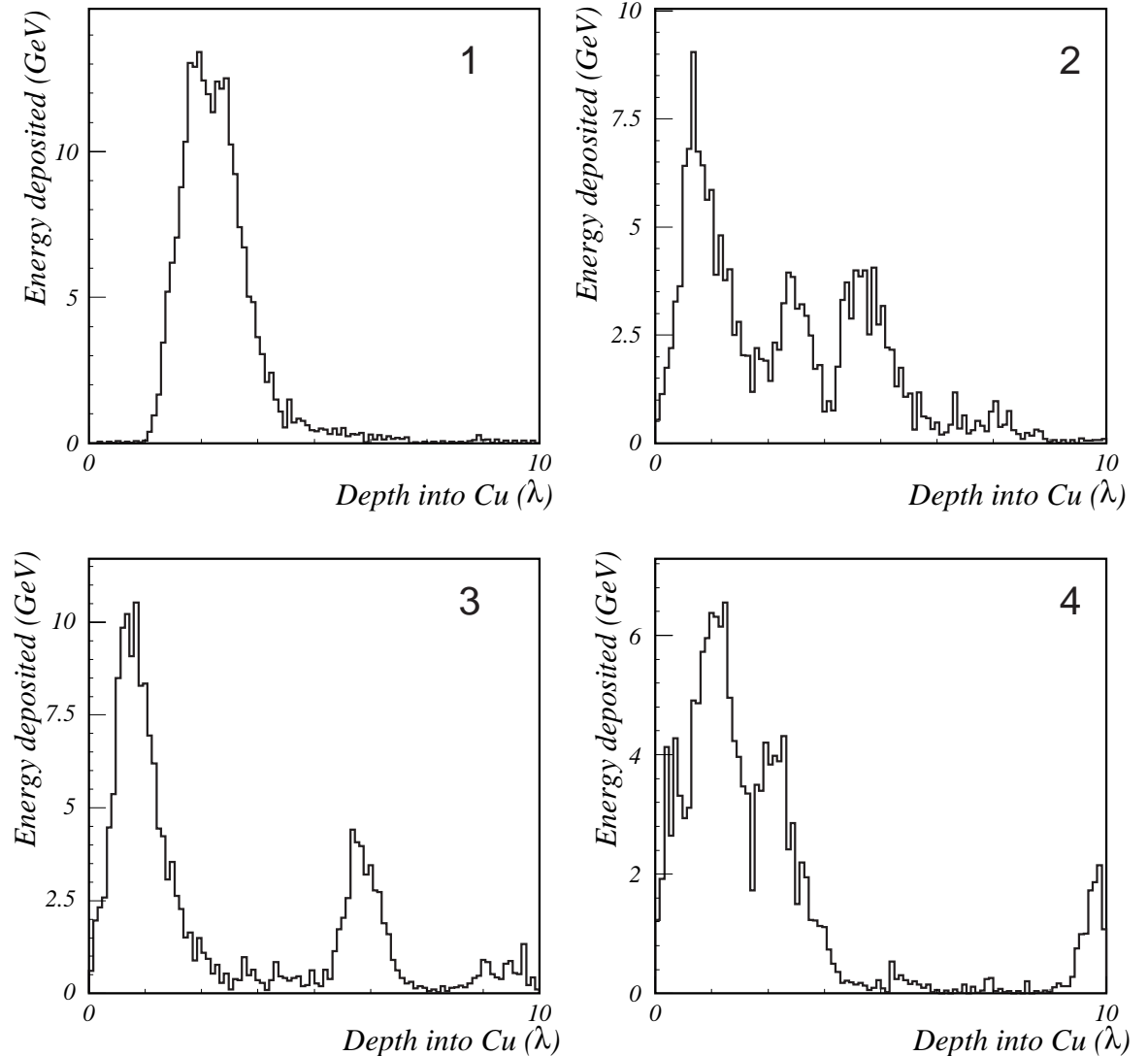
Hadr. Cascade - Intrinsic Fluctuation

- Hadron showers contain em component due to π^0 , η .
- Size of the em component (F_0) is essentially determined by the 1st interaction.
- Considerable event to event fluctuation in F_0 .

On average 1/3 of mesons ($\pi^0/\pi^++\pi^-\pi^0$) produced in the first interaction will be π^0 's.

The 2nd generation π^\pm 's also produce π^0 's if sufficiently energetic.

270 GeV Incident Pions in Copper





Hadronic Cascade Longitudinal Development

- It is convenient to describe the hadron shower development using scaled variables

$$v = x / \lambda \quad \text{and} \quad E_{th} \sim 2 m_{\pi} = 0.28 \text{ GeV}$$

λ , the nuclear interaction length, is the scale appropriate for longitudinal and lateral development of hadronic showers

$$\lambda \sim 35 A^{1/3} \text{ g cm}^{-2}$$

Consider a simplified model of hadronic shower development. The generation length can be taken to be λ . Assume that for each generation $\langle n \rangle$ secondaries/primary are produced. The cascade continues until no more pions can be produced.

in generation v
$$e(v) = \frac{E}{\langle n \rangle^v}$$

at shower max
$$e(v_{\max}) = E_{th} \quad \therefore E_{th} = \frac{E}{\langle n \rangle^{v_{\max}}}$$

$$n^{v_{\max}} = \frac{E}{E_{th}} \Rightarrow v_{\max} = \ln(E / E_{th}) / \ln \langle n \rangle$$

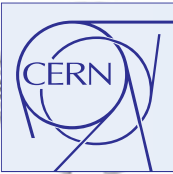
- Mean Longitudinal energy deposition profiles are characterized by a sharp peak near the 1st interaction point (from π^0 's produced in the 1st interaction) followed by a more gradual falloff with a characteristic scale of λ . The maximum, as measured from the front, occurs at

$$x / \lambda = v_{\max} \sim 0.2 \ln E + 0.7 \quad (E \text{ in GeV})$$

Total "path length" for hadronic showers is shorter by E_{th}/ϵ

hence

$$\frac{a_{intr}^{\pi}}{a_{intr}^{em}} \approx \sqrt{\frac{E_{th}}{\epsilon}} \approx 6$$



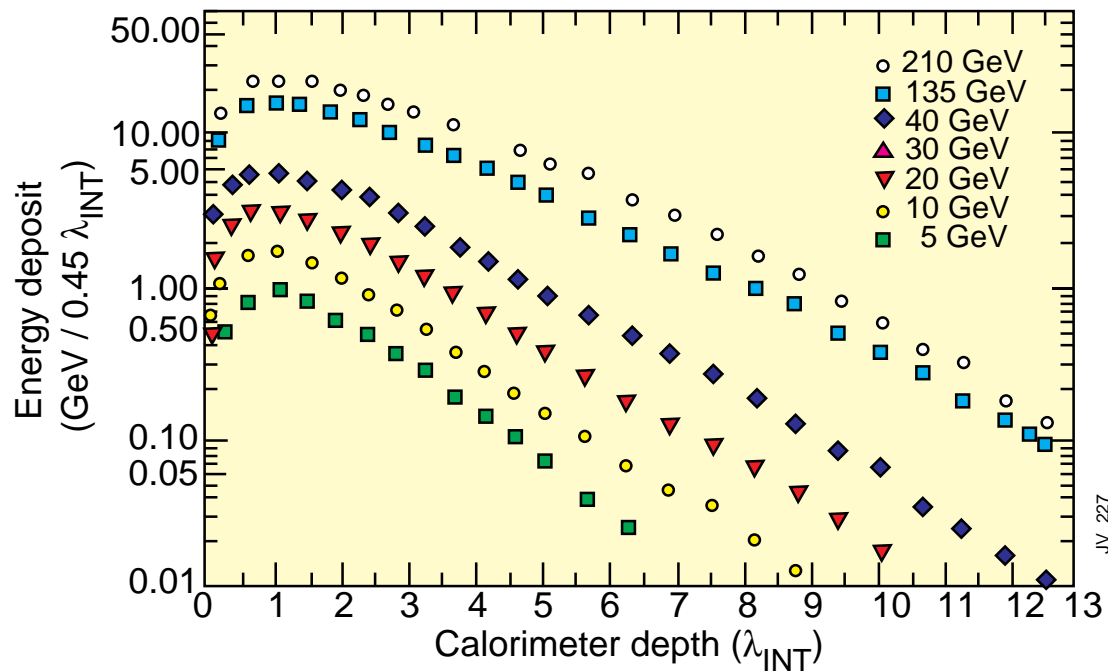
Hadronic Cascade - Profiles

Hadron shower profiles for single π^\pm

Longitudinal

- sharp peak from π^0 's produced in the 1st interaction
- followed by a more gradual falloff with a characteristic scale of λ .

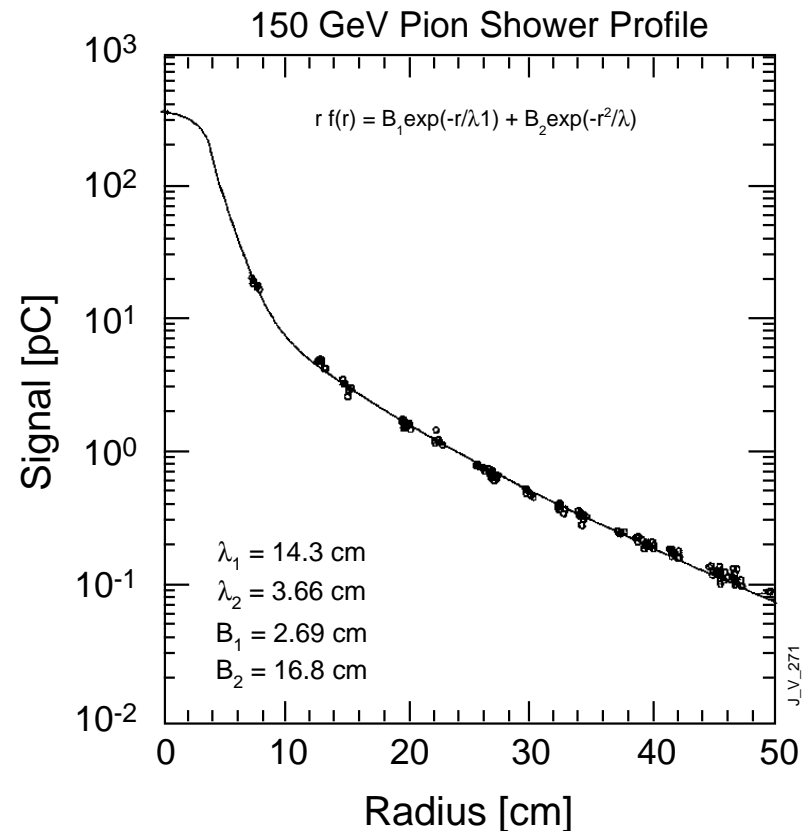
WA78 : 5.4λ of 10mm U / 5mm Scint + 8λ of 25mm Fe / 5mm Scint



Approx. 10λ required to contain 99% of the energy of ≈ 200 GeV pions

Lateral

- Secondaries produced with $\langle p_t \rangle \sim 300$ MeV - approx. energy lost in $\approx 1 \lambda$ in most materials.
- Characteristic transverse scale is $r_\pi \approx \lambda$.
- Pronounced core, caused by the π^0 component, .



Transverse radius for 95% containment is $R_{0.95} \approx 1 \lambda$



Energy Resolution

The energy resolution of calorimeters is usually parameterised as:

$$\frac{\sigma}{E} = \frac{a}{\sqrt{E}} \oplus \frac{b}{E} \oplus c$$

symbol \oplus implies the quadratic sum of the three terms on rhs

'stochastic or sampling' term (coeff. a) accounts for

- the statistical fluctuation in the number of primary and independent signal generating processes, or any further process that limits this number e.g. conversion of light into photo-electrons by a photodevice

'noise' term (coeff. b) includes

- the energy equivalent of the electronics noise and
- pileup - the fluctuation of energy carried by particles, other than the one(s) of interest, entering the measurement area

'constant' term (coeff. c) accounts for

- non-uniformity of signal generation and/or collection
- the cell to cell inter-calibration error
- the fluctuation in the amount of energy deposited in dead materials in front or inside the calorimeter
- the fluctuation in the amount of energy leakage from the front, the rear and the sides of the volume used for energy measurement.
- for hadronic showers contribution from the fluctuation in the e.m. component (dependent logarithmically on energy)

There may be a correlation with the 'a' term

- The tolerable size of these three terms depends on the energy range involved in the experiment.
- Such parametrisations allow the identification of the causes of resolution degradation.
- Quadratic summation implies independent contributions which may not be the case.



em. Energy Resolution

- Intrinsic e.m. Energy Resolution
- Energy Resolution of e.m. Sampling Calorimeters
- Energy Resolution of e.m. Sampling Calorimeters
- Longitudinal Non-Uniformity
- Inter-Calibration Error



Intrinsic e.m. Energy Resolution

- It is instructive to look at homogeneous calorimeters in which all the energy is deposited in the active medium
- If shower is fully contained then the only fluctuation is one due to the produced no. of ion-pairs or photons, n .
- If W is mean energy required to produce an ion pair (or a photon) then

$$n = \frac{E}{W} \quad \text{and} \quad \frac{\sigma}{E} = \frac{\sqrt{n}}{n} = \sqrt{\frac{W}{E}}$$

Fluctuation is reduced as total energy deposited does not fluctuate
Improvement in resolution is characterised by the Fano factor, F ,

$$\frac{\sigma}{E} = \sqrt{\frac{FW}{E}}$$

F is a function of all processes that lead to energy transfer in the detector including reactions that do not lead to ionisation e.g. phonon excitations

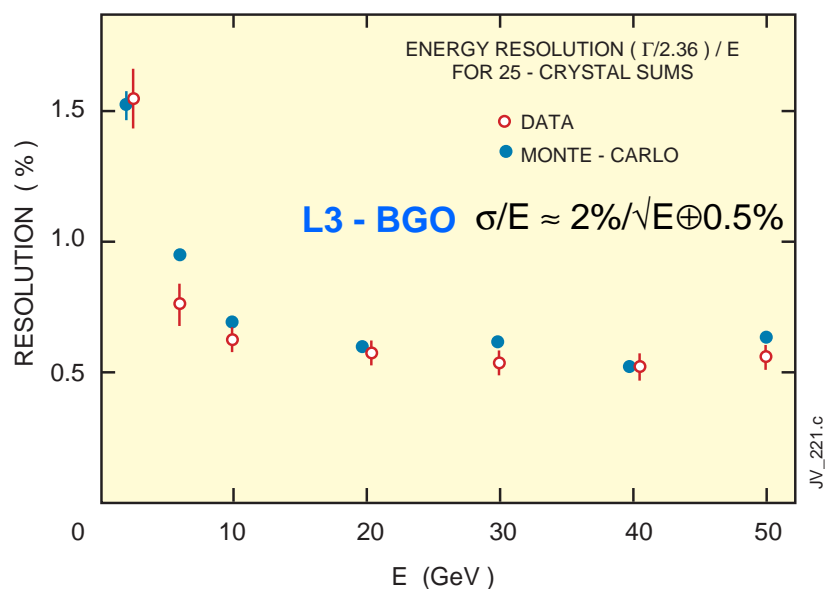
In Ge (77°K) measure $\sigma = 178$ eV for γ of 100 keV

Deduce $\sigma = \sqrt{FWE} = \sqrt{(0.13 \cdot 2.96 \cdot 10^5)} \approx 195$ eV

NB : Without Fano factor $\sigma = 540$ eV !

The difference between the band gap energy and the W -value goes into production of phonons.

Scintillating crystal/
homogeneous noble
liquid calorimeters can
give excellent energy
resolution at high
energies





Energy Resolution of e.m. Sampling Calorimeters

- Shower develops in a sandwich of high-Z absorber and low-Z active layers
- only a fraction of the shower energy is dissipated in the active medium,
- the energy resolution is dominated by the fluctuation in the energy deposited in the active layers

Consider a picture of shower development where

$$\left. \frac{dE}{dx} \right|_{act} \ll \left. \frac{dE}{dx} \right|_{abs}$$

(act-active, abs-absorber)

then no. of charged particles 'crossing' an active layer is

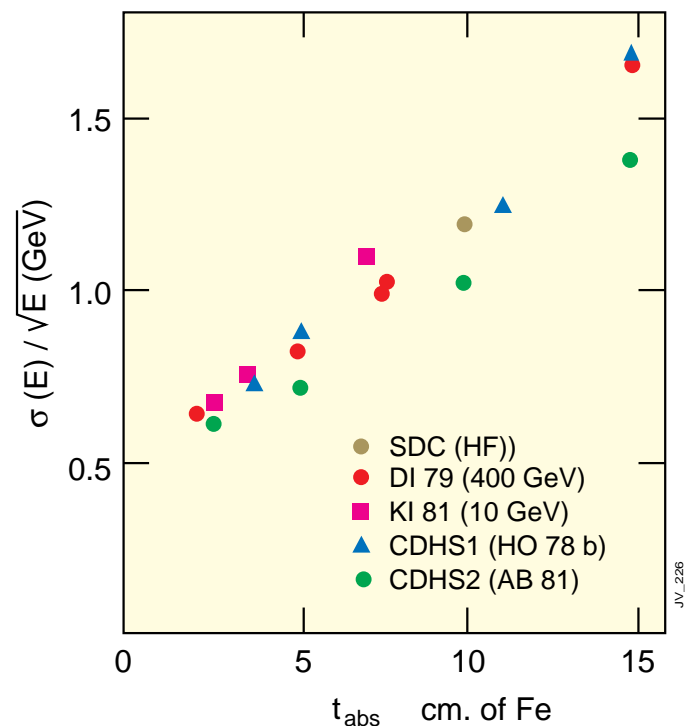
$$n = \frac{E}{\Delta E_{abs}}$$

where ΔE_{abs} is energy lost by a m.i.p. in the absorber layer with a thickness t_{abs} measured in units of X_0 :

$$\Delta E_{abs} = t_{abs} \frac{dE}{dx}$$

$$\frac{\sigma}{E} = \frac{\sqrt{n}}{n} = \frac{\sqrt{\Delta E_{abs}}}{\sqrt{E}}$$

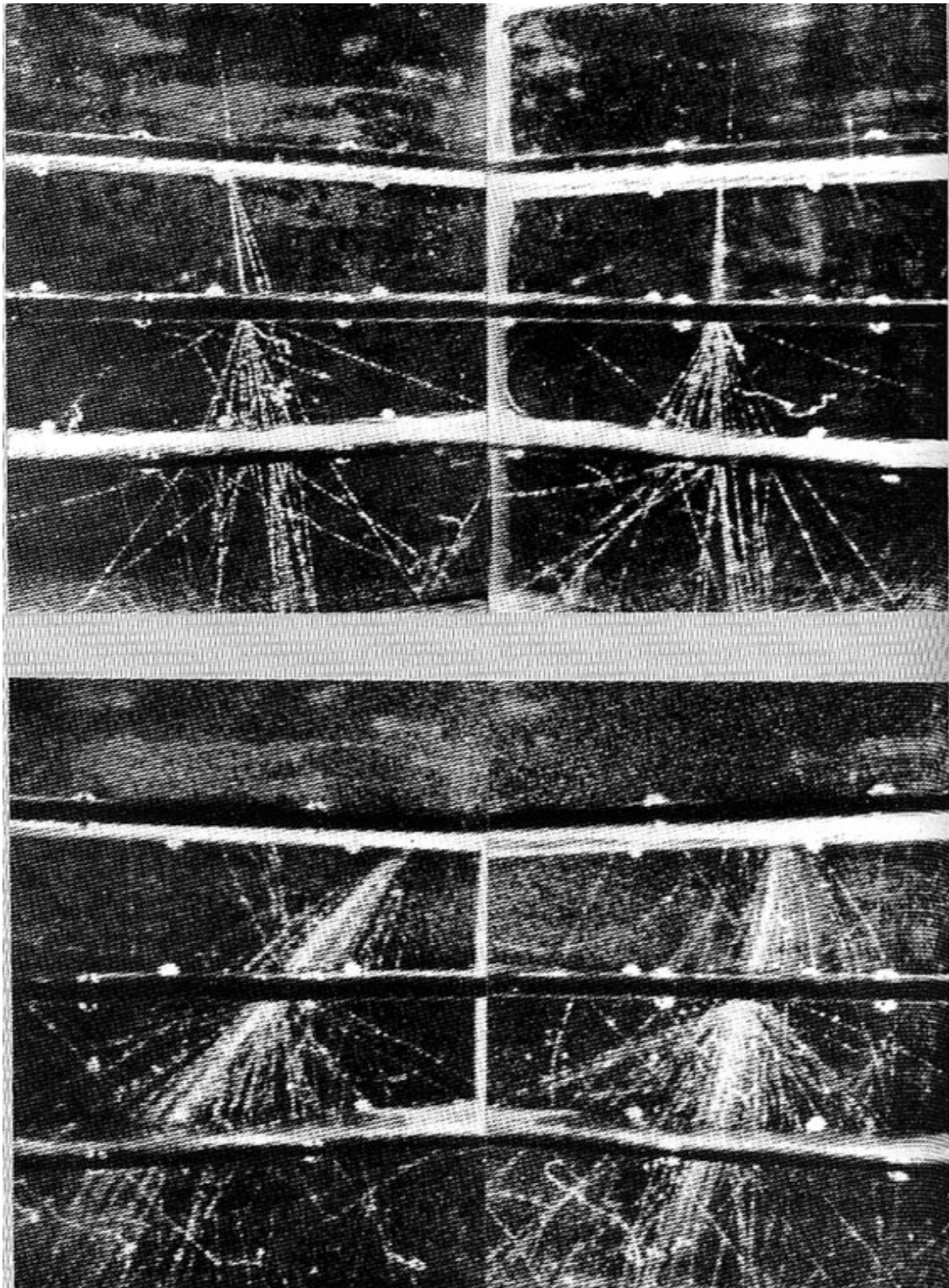
$$\therefore \frac{\sigma}{E} \propto \frac{\sqrt{t_{abs}}}{\sqrt{E}}$$



For fixed active layer thickness the energy resolution should improve with decreasing absorber thickness

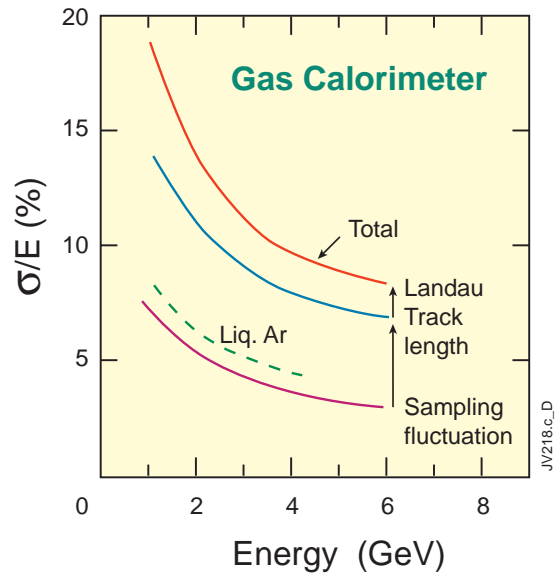
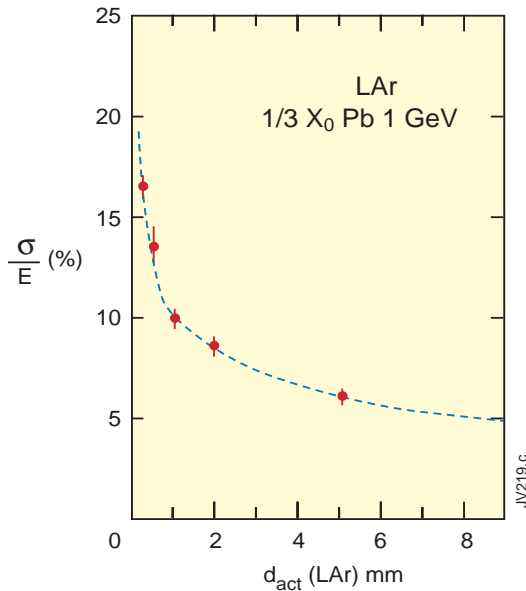
e.m. Showers in Sampling Calorimeter

Two cloud-chamber photographs of e.m. showers developing in lead plates (thicknesses from top down 1.1, 1.1, 0.13 X0) exposed to cosmic radiation at sea-level. There are two views in each photo.



Energy Resolution of e.m. Sampling Calorimeters

If active layers become too thin (e.g. gas calorimeters) then energy resolution is degraded through path length and in gases through Landau fluctuations in addition.



- large fraction of the energy is deposited by low energy electrons
- bremsstrahlung photons emitted by electrons are soft (energies below 1 MeV)
- energy lost, mainly in absorber, by electrons produced via Compton or photoelectric effect.
- resulting electrons have a short range in the absorber layer

energy resolution can be improved by decreasing the absorber thickness (or increasing the sampling frequency)

A universal parametrisation for the energy resolution is

$$\frac{\sigma_s}{E} = \frac{5\%}{\sqrt{E}} (1 - f_{samp}) \Delta E_{cell}^{0.5(1-f_{samp})}$$

where ΔE_{cell} is the energy deposited in 1 absorber and 1 active layer and f_{samp} is the fraction of energy deposited in the active layers

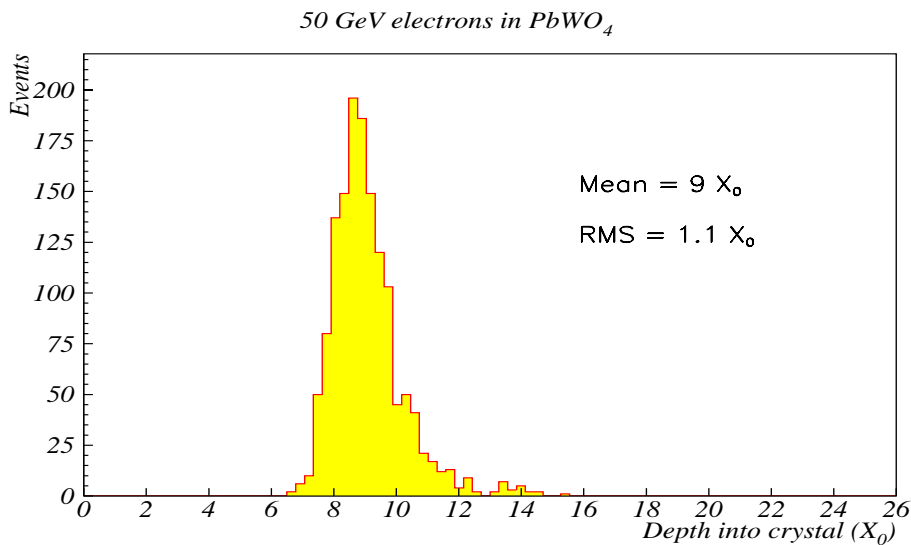
$$f_{samp} = 0.6 f_{mip} = 0.6 \frac{d \left(\frac{dE}{dx} \right)_{act}}{\left[d \left(\frac{dE}{dx} \right)_{act} + t_{abs} \left(\frac{dE}{dx} \right)_{abs} \right]}$$

d - thickness of active layer
 e.g. 1 cm Pb / 1 cm Scint
 $f_{mip} \approx 2/(12.75+2) \approx 13.5\%$

Longitudinal Non-Uniformity

Longitudinal non-uniformity of signal generation and/or collection, either intrinsically or through radiation damage, when folded with the fluctuation in the longitudinal profile from one shower to another (at a fixed energy) leads to a loss of energy resolution (contribution to constant term)

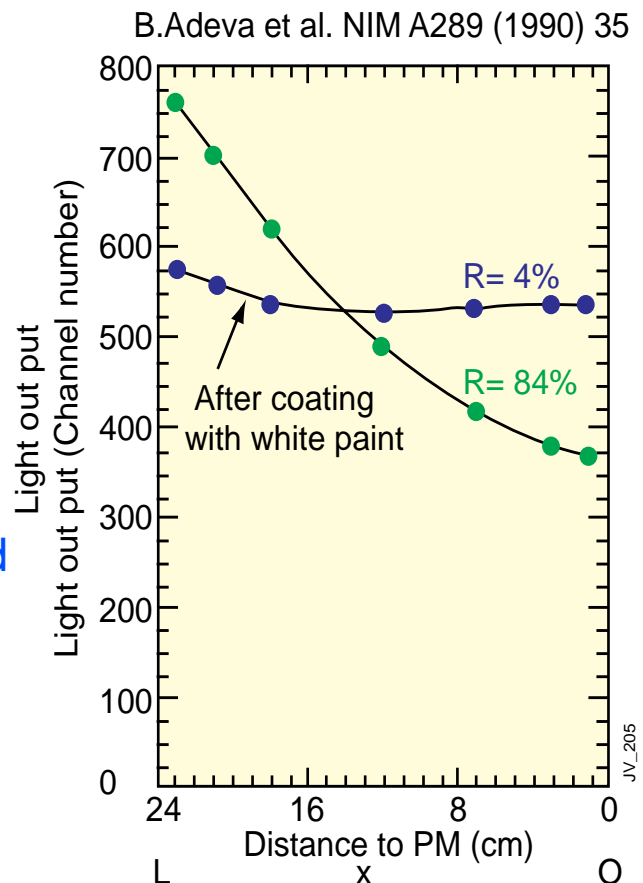
At a given energy the shower max fluctuates with $\sigma \approx 1 X_0$.



e.g. BGO crystals in L3 expt.

- scintillation light is generated isotropically and is detected by Si photodiodes mounted on the rear face
- efficiency of light collection from the front is much increased due to the taper of the crystals.

- non-uniformity is greatly reduced by coating the polished crystals with 40-50 μm thick layer of high reflectivity NE560 white paint.



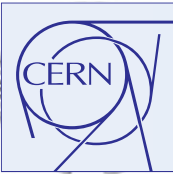


Inter-Calibration Error

- e.m. showers are narrow
usually central cell, or at most, central 4 cells contain $\approx 80\%$ of shower energy
- lateral shower shape is independent of energy
any effect on resolution will end up in constant term
- Measured energy is;

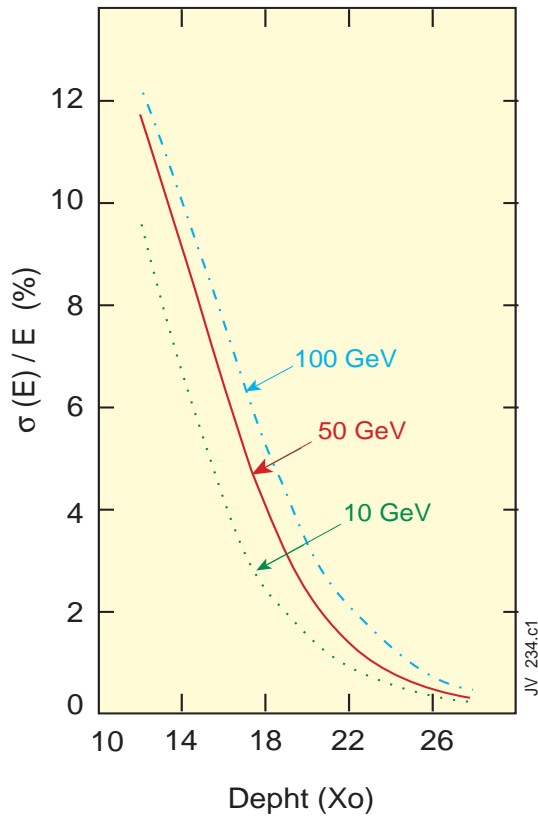
$$E = \sum g_i E_i$$

- if r.m.s. error on g_i is δ then $c \approx \delta / \sqrt{n}$ ranging from $\delta/2$ to δ
- cell to cell inter-calibration should be substantially better than the desired constant term

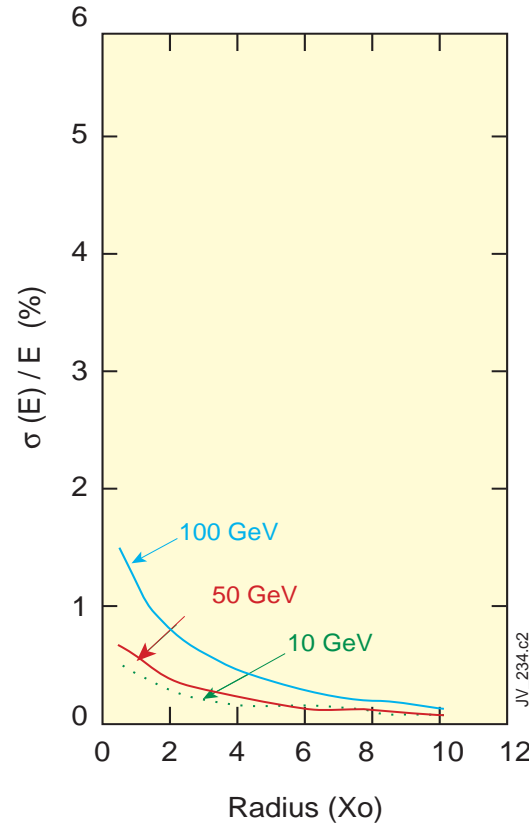


Energy Leakage

Degradation due to longitudinal and lateral leakage for a totally active LXe calorimeter



JV_234.c1



JV_234.c2

Longitudinal leakage has more serious consequences.

At fixed energy, profile of longitudinal energy deposition differs from one shower to another. For a fixed depth of calorimeter, fraction of energy leakage (f) and its fluctuation increases with energy

$$\frac{\sigma_{rms}}{\langle E_{dep} \rangle} = \frac{f}{2} \quad \text{for } f < 20\%$$

Lateral profile of energy deposition differs much less from one shower to another and energy dependence is weak
Lateral shape is almost independent of energy especially at high energies



Energy Resolution of Hadronic Calorimeters

- Energy Resolution of Hadronic Calorimeters
- Hadr. Cascade - em Component
- Energy Resolution of Hadronic Calorimeters
- Hadr. Cascade - Role of e/h
- Compensation
- Sampling and Intrinsic Fluctuations



Energy Resolution of Hadronic Calorimeters

Hadronic calorimeters, because of large depth required ($\sim 10\lambda$) are by necessity sampling calorimeters

Response of em sampling calorimeter is $E_{\text{vis}} = e E$
where E , E_{vis} are incident and visible energies resp. and $e = f_{\text{samp}}^e$

Response of a hadronic sampling calo is

$$E = E_{\text{em}} + E_{\text{ch}} + E_{\text{n}} + E_{\text{nucl}}$$

where E_i is energy deposited by i th component

E_{em} - em component (π^0 s)

E_{ch} - charged pions or protons

E_{n} - low energy neutrons

E_{nucl} - energy lost in breaking nuclei (binding energy)
sometimes labelled 'invisible' energy

Each component has its own sampling fraction

$$E_{\text{vis}} = eE_{\text{em}} + \pi E_{\text{ch}} + nE_{\text{n}} + NE_{\text{nucl}}$$

N is normally v. small but E_{nucl} can be large ($\sim 40\%$ in Pb) and hence $e/h > 1$ for non-compensating calorimeters

Fluctuations in the visible energy have two sources

- sampling fluctuation as in em case. Can be reduced by finer absorber plates
 - intrinsic fluctuation in shower components (δE_{em} , δE_{ch} etc.)
- \therefore stochastic term

$$a_h = \frac{a}{\sqrt{E}} \oplus \left(\frac{a_{\text{intr}}}{\sqrt{E}} + c \right)$$

c , the constant term, depends on e/h and vanishes for compensating calo.



Hadr. Cascade - em Component

- Hadron showers contain an electromagnetic component (due to π^0, η).
- Size of the em component (F_0) is essentially determined by the 1st interaction.
- Considerable event to event fluctuation in F_0 . On average 1/3 of mesons ($\pi^0/\pi^+\pi^-\pi^0$) produced in the first interaction will be π^0 's. The 2nd generation π^\pm 's may also produce π^0 's if sufficiently energetic.

Assume that for each generation $\langle n \rangle$ secondaries/primary are produced with a fraction $f_0 = 1/3$.

At shower max an energy fraction F_0 has been deposited by neutrals

$$\begin{aligned} v=1, & \quad F_0 = f_0 \\ v=2 & \quad F_0 = f_0 + f_0 (1-f_0) \\ v=3 & \quad F_0 = f_0 + f_0 (1-f_0) + f_0 (1-f_0)^2 \end{aligned}$$

$$\begin{aligned} & \dots\dots \\ \Rightarrow & \quad F_0 = f_0 \sum_1 (1-f_0)^{v-1} \\ \Rightarrow & \quad F_0 = [1 - (1-f_0)^v] \end{aligned}$$

- at low energies $F_0 \rightarrow f_0$ whereas
- at very high energies v_{\max} is large and hence $F_0 \rightarrow 1$.

Neutral pions, developing as em showers, do not produce any hadronic interactions and hence drop out of the hadronic cascade.



Energy Resolution of Hadronic Calorimeters

It usually turns out that the response of the calorimeter to electrons and photons i.e. em component (labelled as e) may differ from that of charged hadrons i.e. non-em (labelled h).

Hence response to electrons (E_e) and charged pions (E_π) is

$$E_\pi = e F_0 + h (1-F_0) \quad \frac{e}{\pi} = \frac{(e/h)}{[(e/h)F_0 + (1-F_0)]}$$

$$E_e = e$$

If $e/h = 1$ the calorimeter is said to be compensating.

If $|e/h| \geq 10\%$ calorimeter performance is compromised :

- i) measured energy distribution is non-Gaussian
- ii) an e/π ratio different from unity and dependent on energy
- iii) a non-linear energy response to hadrons
- iv) an additional contribution to the relative energy resolution $(\sigma/E)^*$ due to fluctuation in f_0 .

σ/E does not improve as $1/\sqrt{E}$ with increasing energy.

$$* \quad dE_\pi = (e - h) dF_0 \quad \frac{dE}{E} = \frac{dF_0 |(e/h) - 1|}{[(e/h)F_0 + (1-F_0)]}$$

Hence the fractional error depends on e/h , F_0 and dF_0 .

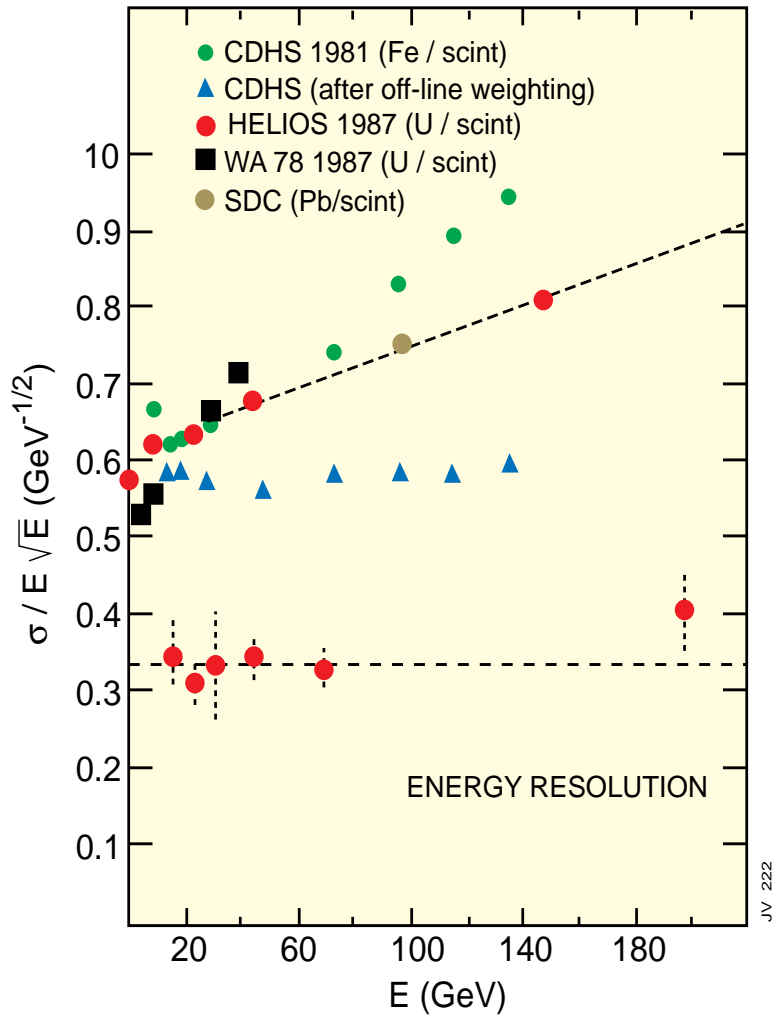
If $e/h = 1$, then there is no contribution due to the fluctuation dF_0 .

Assuming $dF_0/F_0 = df_0/f_0 \sim 1 / \sqrt{\langle n \rangle}$

\Rightarrow for a 200 GeV hadron with $\langle n \rangle \approx 9$,

$dF_0 \approx 0.6 \Rightarrow (dE/E)_{\text{comp}} \approx 3.5\%$

$(dE/E)_{\text{comp}} \sim 1/\sqrt{\ln E}$, and $\rightarrow 0$ as $E \rightarrow \infty$ since $\langle n \rangle \propto \ln E$.





Compensation

- Degree of (non-)compensation is given by the energy independent e/h ratio
- e/h cannot be measured directly but can be inferred from the energy dependent e/π signal ratios.
- Two relations between the signal ratio e/π (E) and e/h

$$\frac{e}{\pi} = \frac{e/h}{1 + (e/h - 1)F_0}$$

$$F_0 = 1 - (E/0.76)^{-0.13} \quad D. Groom$$

$$\text{and } F_0 = 0.11 \ln E \quad R. Wigmans$$

It is instructive to see how the energy is dissipated by a hadron in a Pb absorber. The breakdown is as follows :

- 42 % invisible energy (nuclear breakup)
- 43% charged particles
- 12% neutrons with KE ~ 1MeV
- 3% γ 's with 1 MeV

The sizeable amount of invisible energy loss means that hadronic calorimeters tend to be undercompensating ($e/h > 1$).

Compensation can be achieved in three ways :

- boost the non-em response by using depleted uranium.
- suppress e.m. response
- boost the response to low-energy neutrons



Sampling and Intrinsic Fluctuations

Use the technique of 'interleaved calorimeters'

2 independent calorimeters - L (R) - sum of odd (even) numbered scintillator layers

NIM A277(1989)42

	Pb	U
absorber thickness (mm)	10	3.2
Scint. thickness (mm)	2.5	3.0
lateral segmentn. (cm ²)	20×20	5×60
no. of towers	9	12
total lateral size (cm ²)	60×60	60×60
long. segmentn.	1λ+4λ	4×1.5 λ
total depth	5λ	6λ

1 λ deep tail catcher to veto late starting showers

Deduce for showers

hadrons	Pb calo.	$\sigma_{\text{samp}} = 41.2 \pm 0.9\%/\sqrt{E}$	$\sigma_{\text{intr}} = 13.4 \pm 4.7\%/\sqrt{E}$
	U calo.	$\sigma_{\text{samp}} = 31.1 \pm 0.9\%/\sqrt{E}$	$\sigma_{\text{intr}} = 20.4 \pm 2.4\%/\sqrt{E}$
electrons	Pb calo.	$\sigma_{\text{samp}} = 23.5 \pm 0.5\%/\sqrt{E}$	$\sigma_{\text{intr}} = 0.3 \pm 5.1\%/\sqrt{E}$
	U calo	$\sigma_{\text{samp}} = 16.5 \pm 0.5\%/\sqrt{E}$	$\sigma_{\text{intr}} = 2.2 \pm 4.8\%/\sqrt{E}$

Conclude for compensating Pb and U calorimeters

- energy resolution is dominated by sampling fluctuations

$$\sigma_{\text{samp}} = \frac{11.5\% \sqrt{\Delta E_{\text{cell}}(\text{MeV})}}{\sqrt{E(\text{GeV})}}$$

- sampling fluctuations for hadrons are larger than those for e's by a factor of 2

very good e.m. energy resolution is incompatible with e/h=1



Energy Measurement of Jets

- Jet Energy Measurement
- Jet Energy Resolution
- Di-jet Mass Resolution
v/s Calorimeter Segmentation



Jet Energy Measurement

Factors that determine the required performance of hadronic calorimetry are

jet energy resolution and linearity
missing transverse energy resolution

Jet energy resolution is limited by effects from

jet algorithms (cone radius, lateral segmentation)
fluctuation in fragmentation
underlying event and energy pileup at high luminosity
magnetic field

Figure of Merit : di-jet mass resolution

Use results from study in context of an LHC experiment

A. Beretvas et al., CMS TN/94-326

Physics input

low p_T di-jets	$50 < p_T < 60 \text{ GeV}$
high p_T di-jets	$500 < p_T < 600 \text{ GeV}$
high mass di-jets	$3 < m_Z < 4 \text{ TeV}$
minbias	QCD di-jets, $2 < p_T < 500 \text{ GeV}$

Typical Calorimeter parameters

geometric coverage	$ \eta < 1.5$
magnetic field	4T
compensation	$e/h = 1$
e.m. resolution	$\sigma/E = 3\%/\sqrt{E} \oplus 0.5\%$
had. resolution	$\sigma/E = 60\%/\sqrt{E} \oplus 3\%$
had. lateral segmentation	$\Delta\eta \times \Delta\phi = 0.1 \times 0.1$
tower thresholds	low p_T events - $E_T > 0.3 \text{ GeV}$ high p_T events - $E_T > 1 \text{ GeV}$

Stochastic Term for Jets

$$\frac{\sigma(E)}{E} = \frac{a}{\sqrt{E}} \oplus c$$

$$\sum_i z_i = 1, \quad \sum_i k_i = E \quad \frac{dk_i}{k_i} = \frac{a}{\sqrt{k_i}} \oplus c$$

If stochastic errors dominate

$$dk_i = a \sqrt{k_i}$$

$$dE_J = \sqrt{\sum_i (dk_i)^2} = \sqrt{\sum_i a^2 k_i} = a\sqrt{E}$$

$$\therefore \frac{dE}{E} = \frac{a}{\sqrt{E}}$$

an ensemble of particles act, w.r.t. errors, as a single particle

Constant Term for Jets

in high energy regime where constant term dominates

$$dE_J \approx \sqrt{(cz_i E)^2} = cE\sqrt{z_i^2}$$

assuming that there is a leading particle, l, with fraction z_l , then

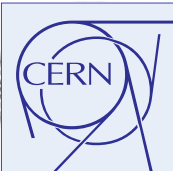
$$\frac{dE_J}{E} \approx c E z_l$$

For fragmentation function

$$zD(z) = (1-z)^2 \quad \langle z_l \rangle \approx 0.23$$

\Rightarrow constant term is reduced

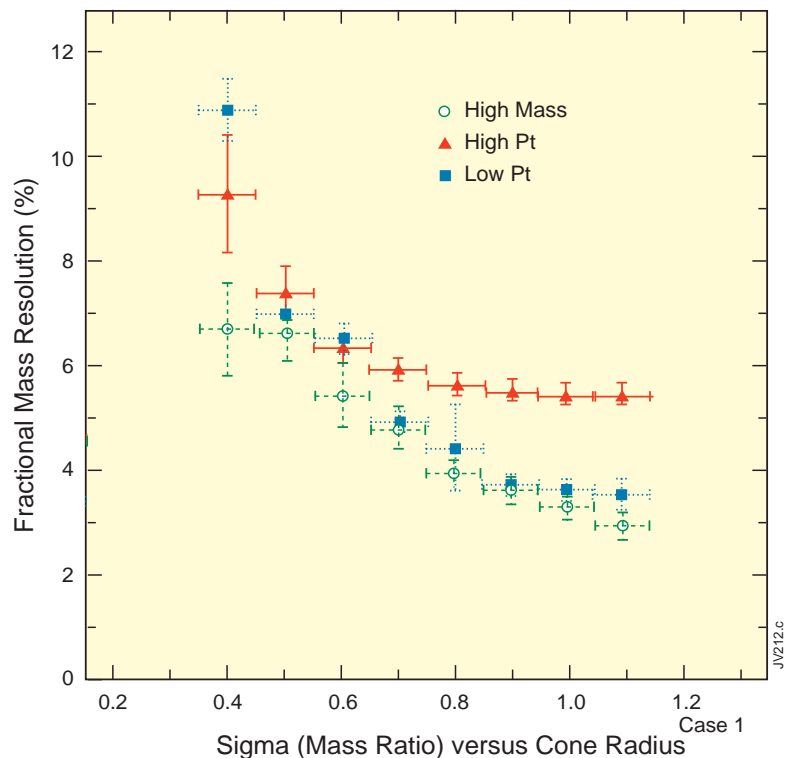
e.g. for a calorimeter with $a=0.3$ and $c=0.05$, in which a 1 TeV jet fragments into 4 hadrons of equal energy the error on the energy decreases from 50 GeV to 25 GeV



Di-jet Mass Resolution v/s Cone Size

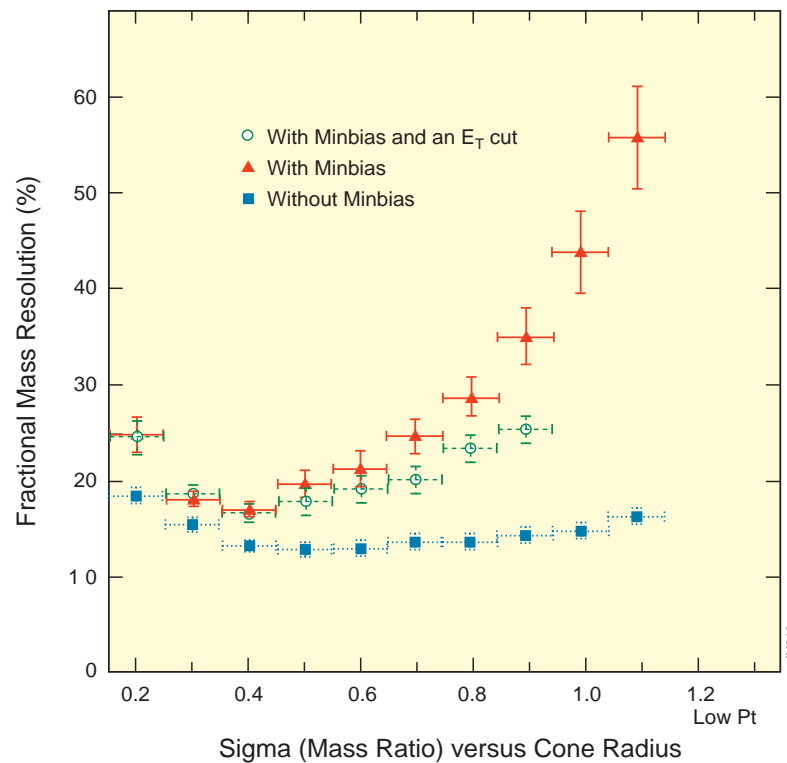
Assume perfect calorimeter, no magnetic field, no underlying event

Low and High p_T and High Mass Di-jets
Fractional Mass Resolution (%) v/s Cone Radius



mass resolution decreases with increasing cone size

Low p_T di-jets
perfect calorimeter +overlapping minbias



worsened mass resolution for

- a smaller cone size - excludes some signal energy
- a larger cone - pick up significant pileup energy

optimize cone size to obtain best mass resolution for each physics process and instantaneous luminosity

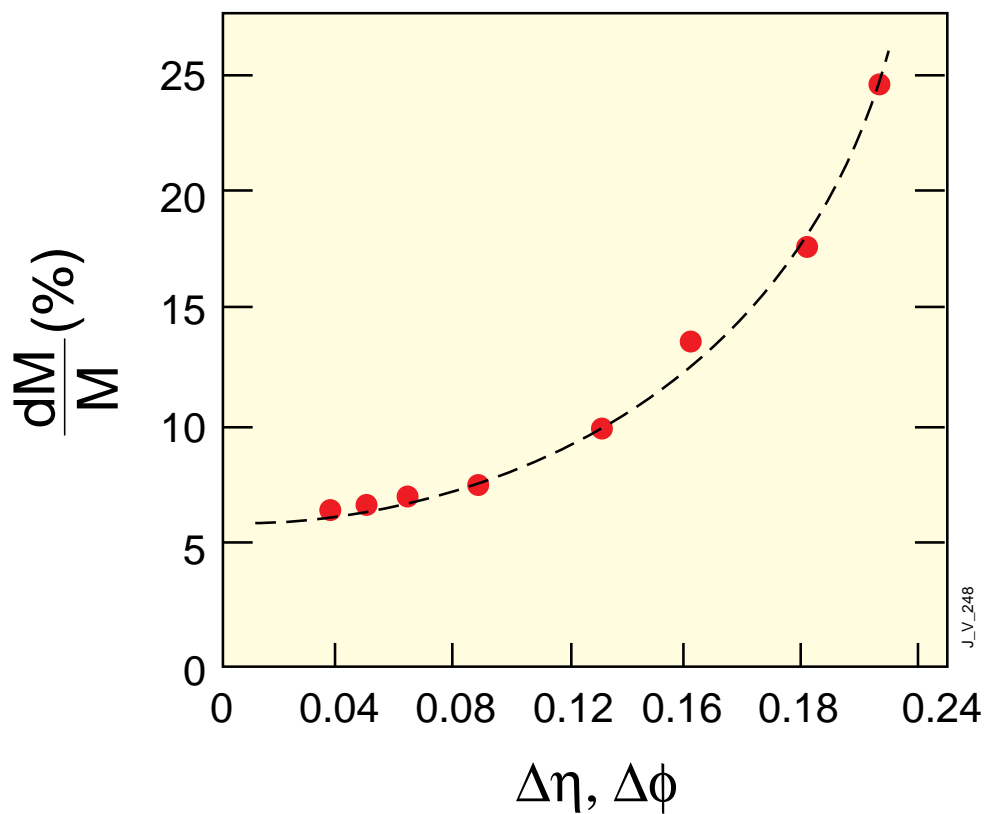


Di-jet Mass Resolution v/s Calorimeter Segmentation

Mass Resolution due to angular error $d\theta$ is given by

$$\frac{dM}{M} = \frac{p_T}{M} d\theta$$

only highly boosted and low mass di-jets (eg. boosted Zs from $H \rightarrow ZZ$) will have a significant contribution from angular error



dM/M worsens dramatically when $\Delta\eta, \Delta\phi > 0.1$



Experimental Measurements

Measurement of Momentum

Charged particle in a magnetic field

Multiple scattering

Measurement of Energy

characteristics of e.m. cascades

characteristics of hadronic cascades

e.m energy resolution

homogeneous calorimeters

sampling calorimeters

hadronic energy resolution

energy measurement of jets

Identification of Particles

electrons, photons -using calorimeters, inner tracker,
TRDs

pions / kaons / protons using Cherenkovs

b-jets

neutrinos (and jets)

muons

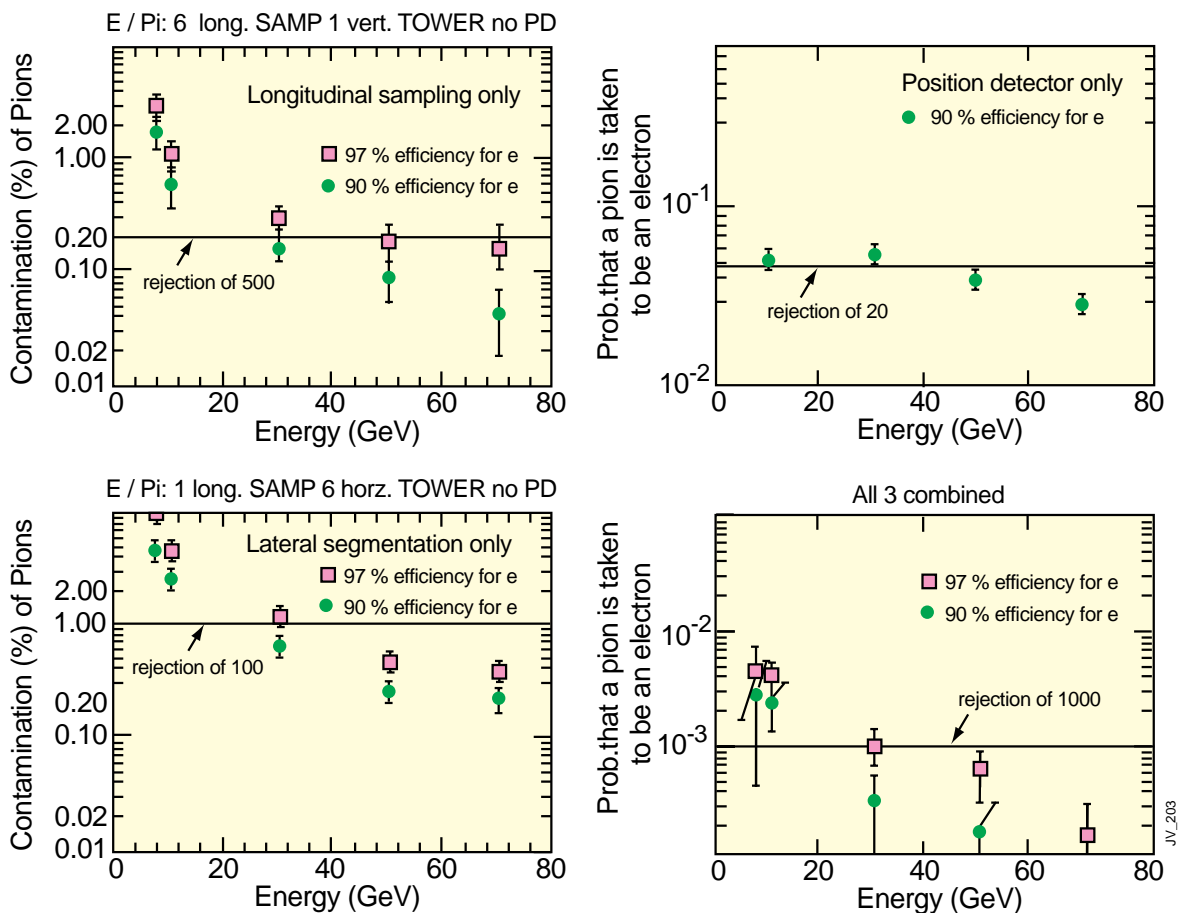
Exploit the differences in longitudinal and lateral development of showers initiated by electrons and hadrons

- preshower detector placed between $\approx 1.5 - 4 X_0$
- lateral segmentation and longitudinal segmentation (veto on HCAL)
- energy-momentum matching

An appropriate combination of these can lead to rejection power of $\approx 10^4$ at high energies Ultimate rejection power is limited by

- charge exchange processes eg. $\pi^+n \rightarrow \pi^0p$, $\pi^-p \rightarrow \pi^0n$
- first hadronic interaction leading to anomalously large π^0 multiplicity or energy

UA1 U/TMP Calorimeter R. Apsimon et al NIM A305(1991)331



Lateral Segmentation
Longit. Segmentation
Preshower Detector

towers of $11 \times 11 \text{ cm}^2 (\approx 14 \times 14 X_0)$
3, 6, 10, 7 $X_0 / 2 \times 0.7\lambda / 2 \times 2.5\lambda$
at $3X_0$ with orthogonal strips of pitch 9mm



γ / jet Separation

γ /jet separation

Physics motivation - observation of $H \rightarrow \gamma\gamma$ signal in range

$80 < m_H < 150$ GeV. Look for single isolated γ 's. σ is small and backgrounds are large. Large uncertainties in jet production and fragmentation

$$\frac{jet - jet}{\mathcal{W}_{irreducible}} \approx 2 \cdot 10^6 \quad \frac{\gamma - jet}{\mathcal{W}_{irreducible}} \approx 8 \cdot 10^2$$

Rejection of ≈ 5000 against jets is needed

Use isolation cuts and fine lateral and/or longitudinal segmentation

γ /jet separation in ATLAS

$$E_{\text{HCAL}} (\Delta\eta \times \Delta\phi = 0.2 \times 0.2) \leq 0.5 \text{ GeV}$$

EM isolation

$$\frac{E_{3 \times 5}}{E_{7 \times 7}} > 90\%$$

Lateral shower profile - look for an em core
: 4 towers contain $> 65\%$ of cluster energy

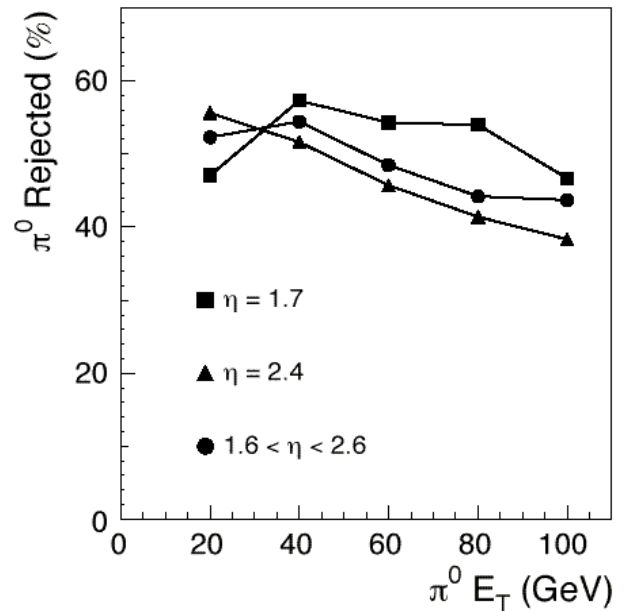
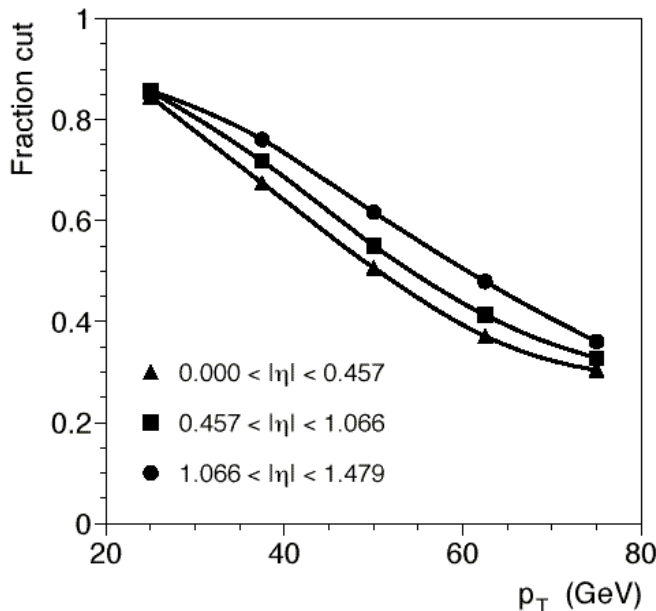
Shower width in η

For a photon efficiency of $> 90\%$, $R_{\text{jet}} \geq 1500$

Isolated π^0 's which take a large fraction of the jet energy can be rejected by detecting presence of 2 em showers.

CMS Barrel

- use fine transverse crystal granularity (2.18×2.18 cm²)
- γ s from π^0 with $p_T=25$ GeV have a minimum separation of 15 mm
- Neural net algorithm compares energy deposited in signal containing 3×3 crystal array - variables are constructed from 9-energies, x and y position, and a pair measuring the shower width



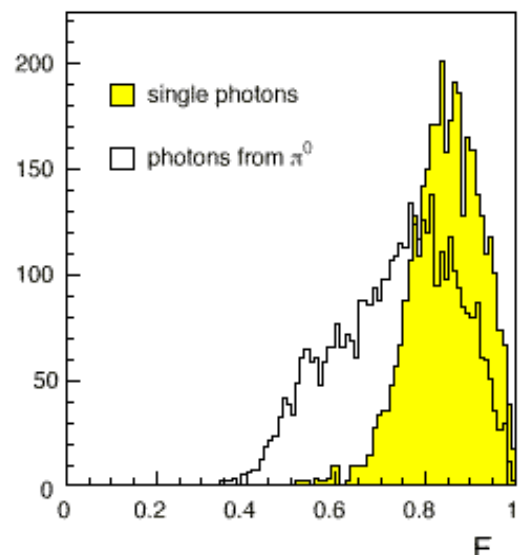
CMS Endcap

- use preshower - two planes of Si strips with fine pitch (≈ 2 mm)
- compare signal (summed in 1,2 or 3 adjacent strips with the total signal in 21 adjacent strips centred on strip with highest signal)

Use variable

$$F = \frac{\sum S_N}{\sum_{j=-m}^m S_{j_{\max}+j}}$$

F for $E_T=60$ GeV: 2nd Si plane





Electron Identification - Transition Radiation

Predicted by Ginzburg and Franck in 1946

$$p = \gamma m v \Rightarrow m = \frac{1}{\beta c \gamma} p$$
$$\therefore \left(\frac{\Delta m}{m} \right)^2 = \frac{1}{\beta^2 c^2} \left(\frac{\Delta \gamma}{\gamma} \right)^2 + \left(\frac{\Delta p}{p} \right)^2$$

If $\Delta p/p$ is small, mass resolution at high momenta is $\propto \gamma$

Transition radiation is emitted when a charged particle moves from a medium of refractive index n_1 to a medium of a different index n_2

This may be thought of as an apparent acceleration

- Radiated energy /boundary to vacuum

$$W = \frac{1}{3} \alpha \hbar \omega_p \gamma \quad \text{i.e. } W \propto \gamma$$

where $\hbar \omega_p$ is the plasma frequency (≈ 20 eV for polyethylene)

Hence can use it for particle identification

- X-rays are emitted at small angle ($\theta \approx 1/\gamma$). TR stays close to the charge particle track

$$E_{ph} = \frac{\gamma}{3} \hbar \omega_p$$

- Number of emitted photon/boundary is small

$$N_{ph} \approx \frac{W}{\hbar \omega_p} \propto \alpha \approx \frac{1}{137} !$$

- Need many transitions \rightarrow build a stack of many thin foils with high Z gas to absorb the X-rays
- Particle must traverse a minimum distance to efficiently emit TR. (typically $20\mu\text{m}$ for polyethylene)

ATLAS Transition Radiation Tracker

Straw tube proportional chambers embedded in polyethylene fibres

Diameter of staws 4mm

Gas 70% Xe + 20% CF₄ + 10%CO₂

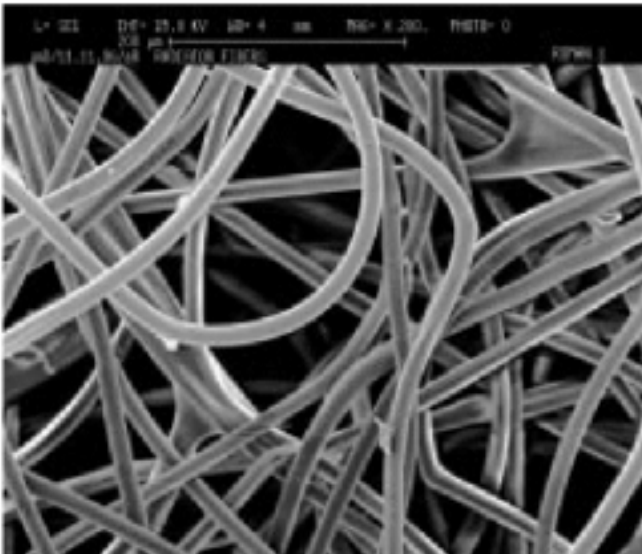


Figure 12-38 Micro-photograph of a sample of polyethylene fibre radiator (scale: 70 μm per 1 cm).

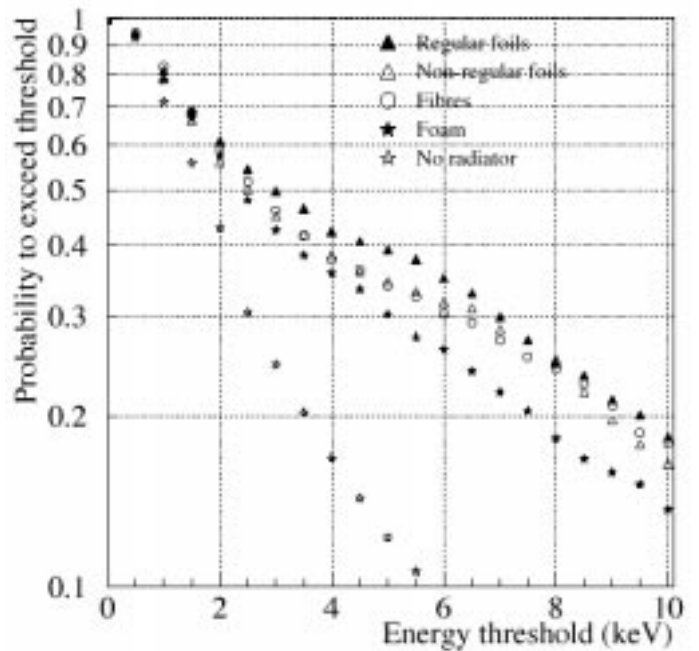


Figure 12-39 For 200 GeV electrons and for different types of radiators, probability per straw to observe an energy deposition above a given threshold.

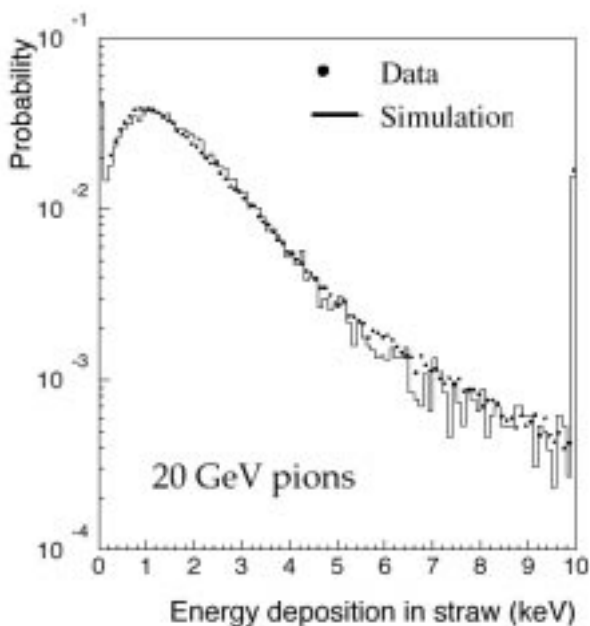


Figure 12-41 Normalised dE/dx spectra for 20 GeV pions for data and simulation.

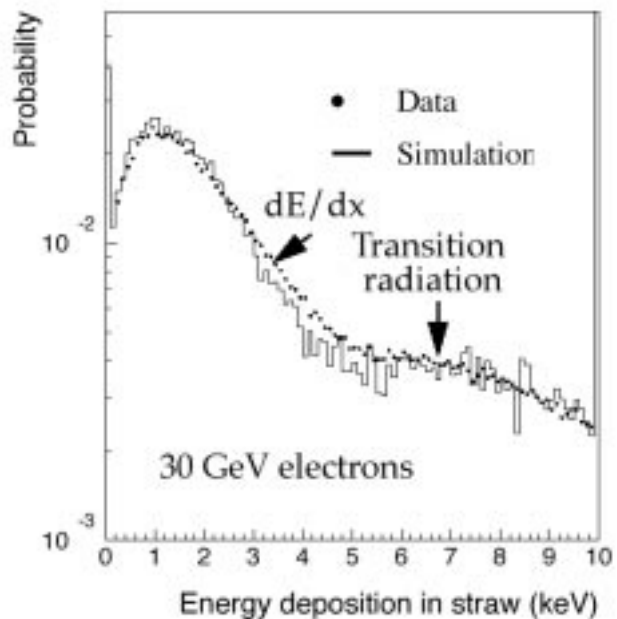
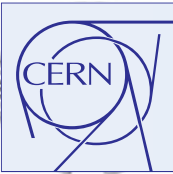
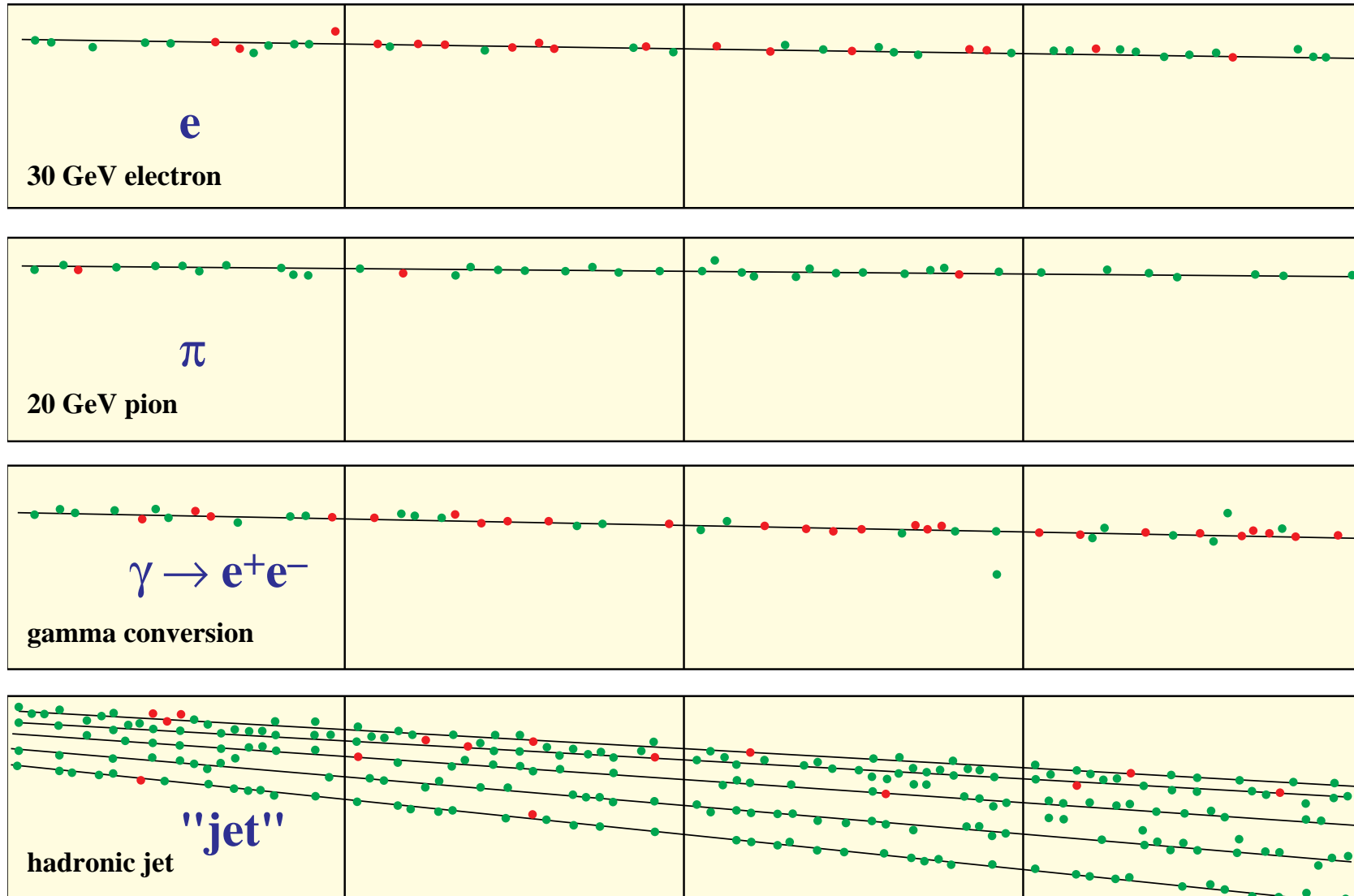


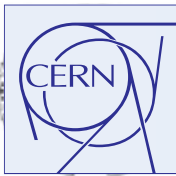
Figure 12-42 Normalised dE/dx and transition-radiation spectra for 30 GeV electrons for data and simulation.



Data from Test Beams

ATLAS TRD Test



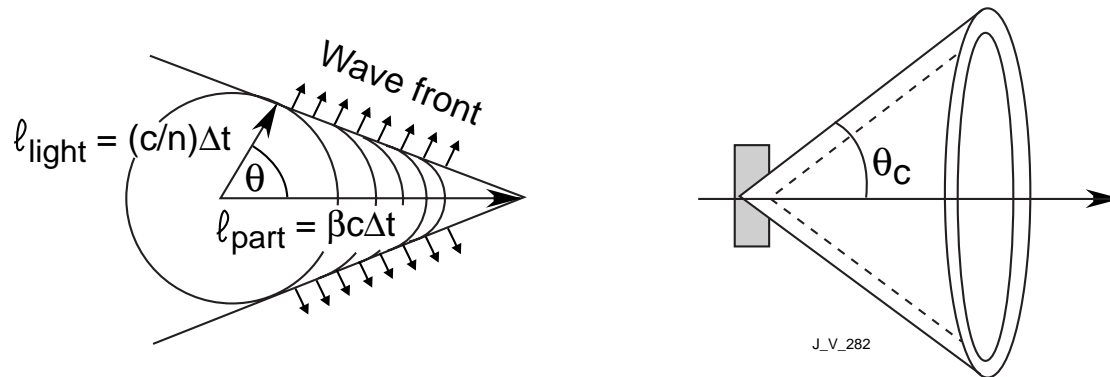


Identification of Particles using Cherenkov Radiation

Charged particle emits Cherenkov radiation when

$$v_{particle} > \frac{c}{n} \quad \text{or} \quad \beta \geq \beta_{thr} = \frac{1}{n} \quad (= \text{sonic shock wave induced by supersonic aircraft})$$

"Huygen's" wavelets add constructively along line defined by C ν angle



$$\cos \theta_C = \frac{1}{n\beta} \quad \text{with } n = n(\lambda) \geq 1$$

$$\theta_{max} = \cos^{-1}(1/n)$$

No. of γ 's emitted/unit length/ unit energy interval is:

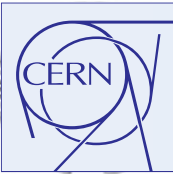
$$\frac{d^2 N}{dx dE} = \frac{\alpha}{\hbar c} \sin^2 \theta_C \approx 365 \sin^2 \theta_C \text{ eV}^{-1} \text{ cm}^{-1}$$

Energy loss by Cherenkov radiation is small compared to loss due to ionization ($\approx 1\%$)

Usually C ν radiation is detected by photomultipliers (sensitivity range 350-550 nm).

Then

$$\frac{dN}{dx} \approx 475 \sin^2 \theta_C \text{ photons/cm for } Z=1$$



Cherenkov Detectors

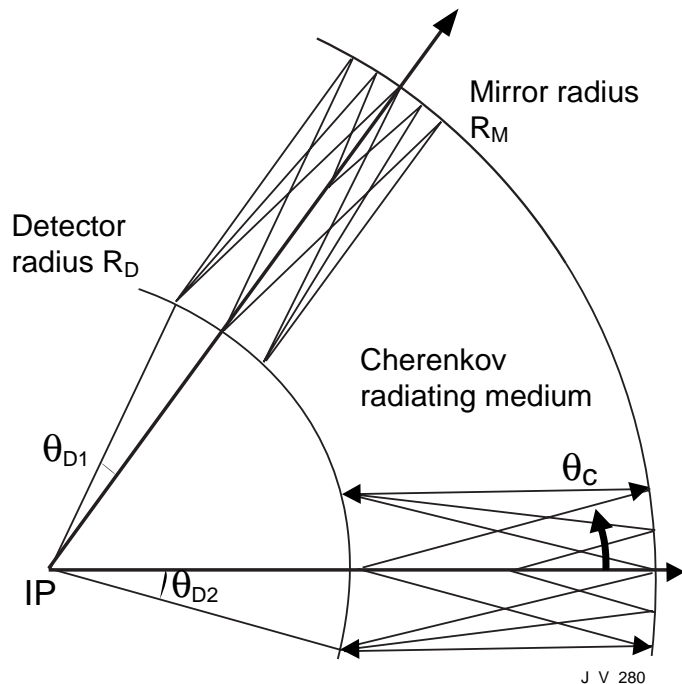
Detectors can exploit :

$N_{ph}(\beta)$ threshold detector (do not measure θ_c)
 $\theta(\beta)$ Ring Imaging Cherenkov (RICH)

Principle of Operation of Ring Imaging Cherenkovs

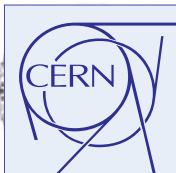
Optimal configuration - spherical mirror and spherical detector at $R_M = 2 R_D$

All photons emitted at the same angle are focused onto the same point i.e. no emission point error

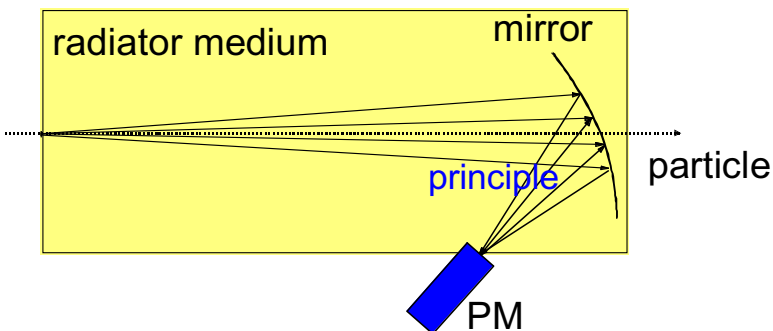


Parameters for some selected Cherenkov radiators.

Medium	$n-1$	θ_{max}	$\frac{\pi_{thr}(p)}{GeV/c}$	$N_\gamma (eV^{-1}cm^{-1})$
Air	1.000283	1.36°	5.9	0.21
Isobutane	1.00217	3.77°	2.12	0.94
Aerogel	1.0065	6,51°	1.23	4.7
Aerogel	1.055	18.6°	0.42	37.1
Water	1.33	41.2°	0.16	160.8
Quartz	1.46	46.7°	0.13	196.4



Threshold Cherenkov Detectors



Threshold Cherenkov detectors

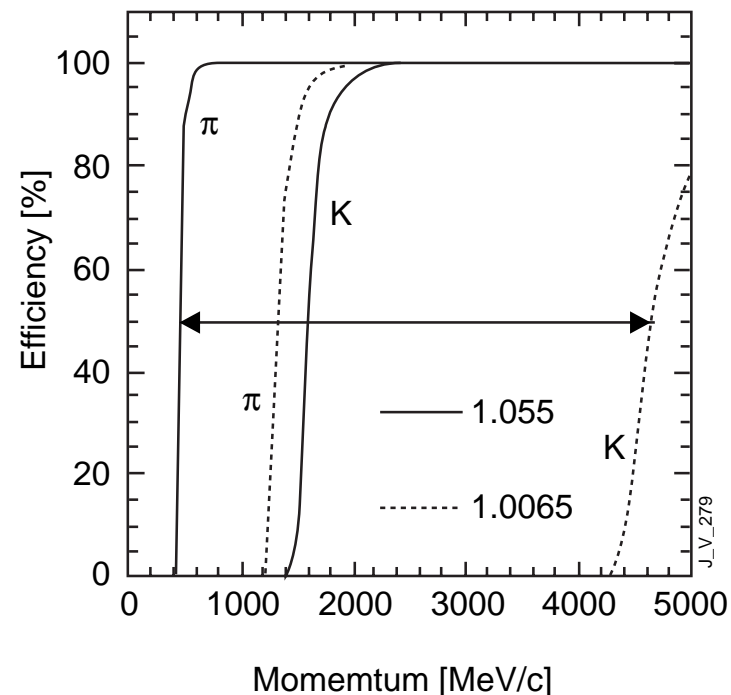
- a simple yes/no decision based on whether a particle is above/below a threshold velocity ($\beta=1/n$)

The no. of photons emitted depends on velocity and is:

$$N_\gamma \propto \sin^2 \theta_c = 1 - \frac{1}{\beta^2 n^2} = 1 - \frac{1}{n^2} \left(1 + \frac{m^2}{p^2} \right)$$

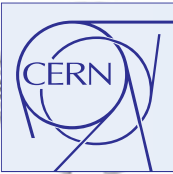
e.g. Aerogel threshold Cherenkov detectors in BaBar

A1: $n = 1.055$ and A2: $n = 1.0065$



- $p > 0.4 \text{ GeV/c}$ π in A1 gives light
- $p > 1.2 \text{ GeV/c}$ π in A1 and A2 gives light
- $p > 1.4 \text{ GeV/c}$ K in A1 gives light
- $p > 4.2 \text{ GeV/c}$ K in A1 and A2 gives light

π/K separation between 0.4 and 4.2 GeV/c



Ring Imaging Cherenkovs

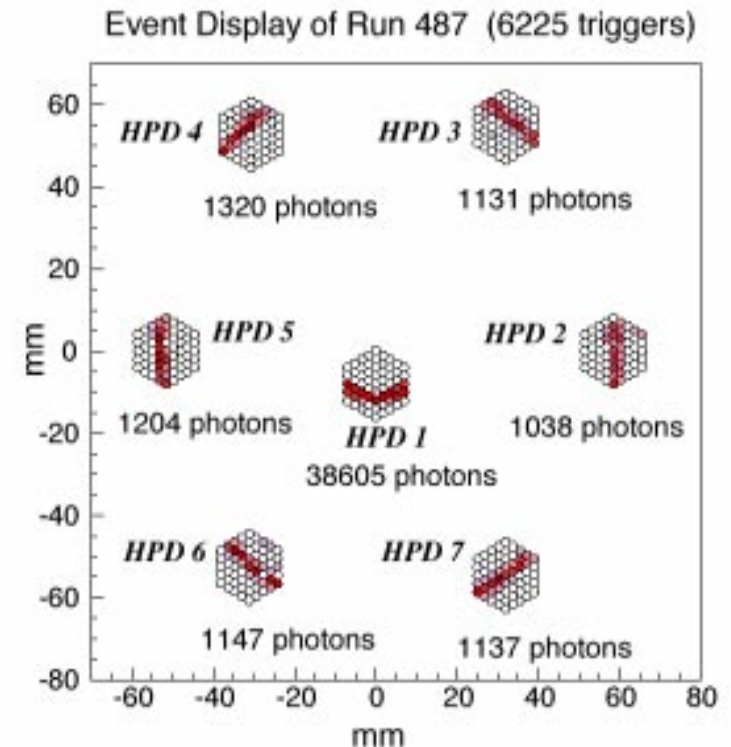
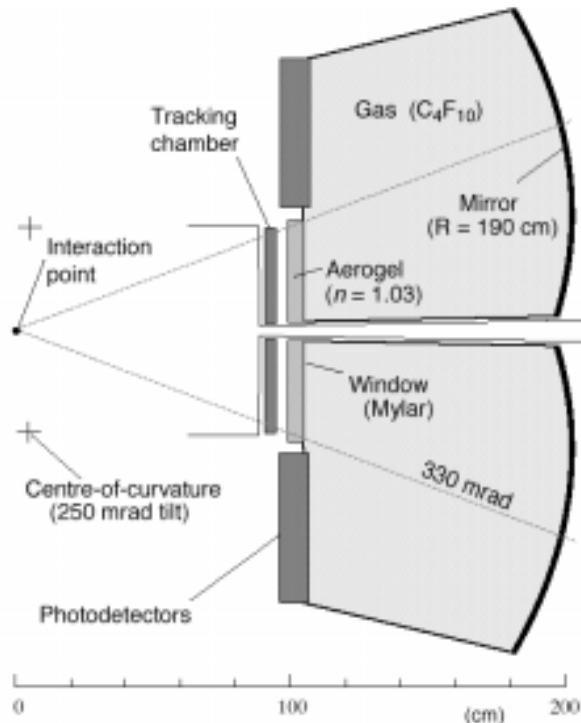
Ring Imaging Cherenkov (RICH) detectors determine identity of particles by measuring Cherenkov angle (θ_C) given by

$$\theta_C = \cos^{-1}\left(\frac{1}{\beta n}\right) = \cos^{-1}\left(\frac{E}{pc} \frac{1}{n}\right) = \cos^{-1}\left(\frac{\sqrt{p^2 + m^2}}{pc} \frac{1}{n}\right) \quad p = \frac{1}{\sqrt{n_\sigma}} \sqrt{\frac{(m_2^2 - m_1^2) \sqrt{N_{pe}}}{2 \tan \theta \times \sigma_\theta^{pe}}}$$

Two particles with masses m_1 and m_2 can be distinguished by n_σ up to a momentum p

e.g. **LHCb** use 2 RICHs, Photodetector : HPD

A1: combined gas (C_4F_{10}) and aerogel **A2:** gas



π/K can be distinguished (3σ) up to 75 GeV/c
 $N=20$ p.e. and $\sigma_e = 1$ mrad and $\omega = 31$ mrad (CF_4)

b-jets can be tagged using

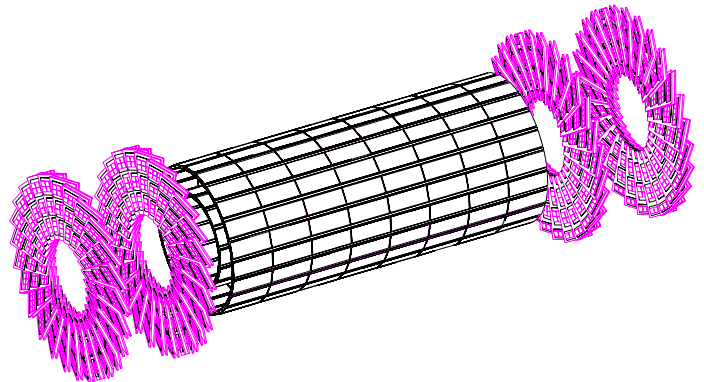
- electrons within a jet from the semi-leptonic decay of a b-quark
- looking for one or more tracks within a jet having a significant impact parameter
- reconstructing a secondary vertex consistent with the flight path of a B-meson

b-jets Tagging using Impact Parameter Measurement

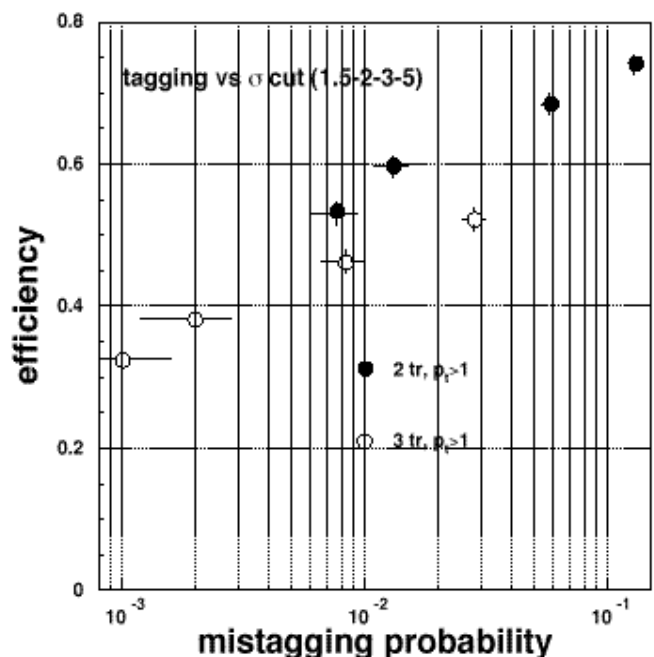
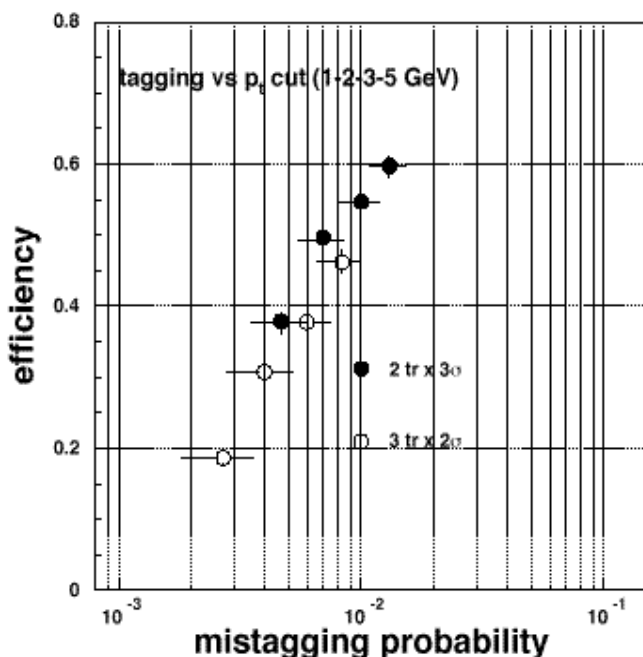
Important parameters

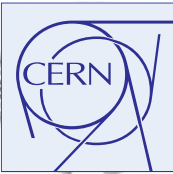
- distance of first measuring layer from interaction vertex
- spatial resolution
- number of points close to the interaction vertex
- low multiple scattering

e.g. using pixel detectors in CMS pixel barrel layers placed at $r=4.5$ and $r=7$ cm at low luminosity



b-tagging efficiency v/s mistagging rate





Identification of b-jets

b-jets can be tagged using

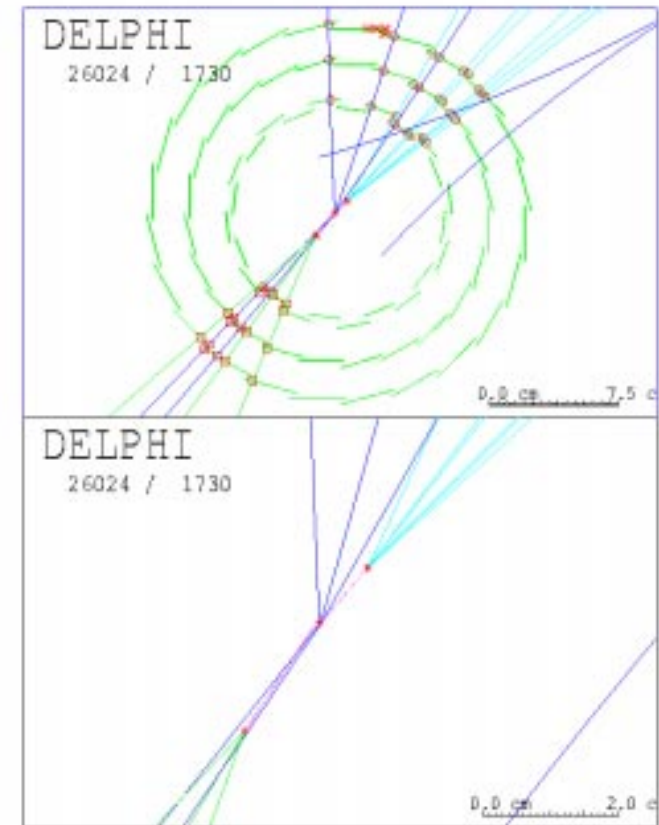
- electrons within a jet from the semi-leptonic decay of a b-quark
- looking for one or more tracks within a jet having a significant impact parameter
- reconstructing a secondary vertex consistent with the flight path of a B-meson

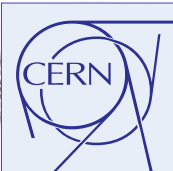
b-jets Tagging using Impact Parameter Measurement

Important parameters

- distance of first measuring layer from interaction vertex
- spatial resolution
- number of points close to the interaction vertex
- low multiple scattering

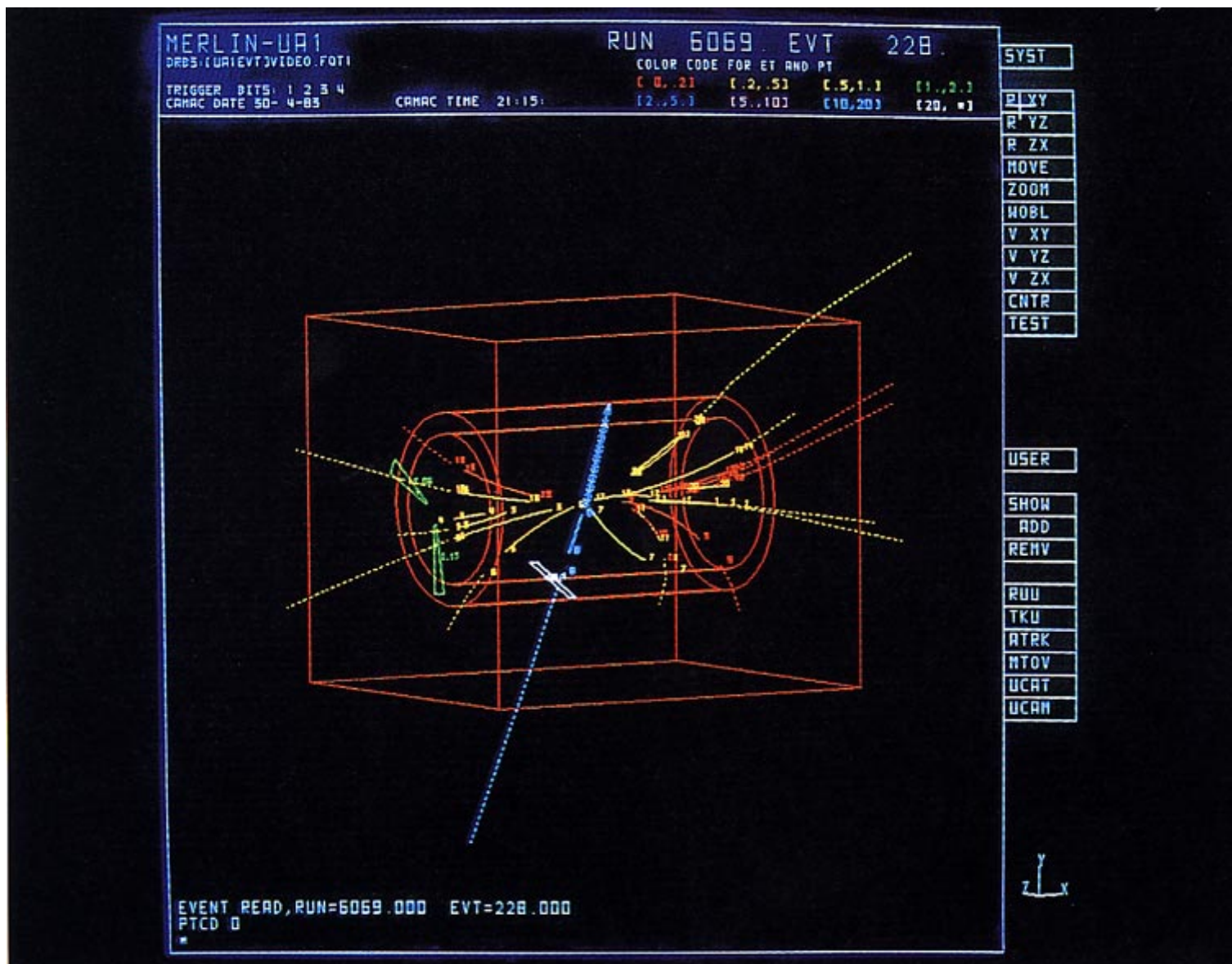
Typically can get a rejection against u, d, and s quarks of a factor of 100 for an efficiency of $\approx 50\%$

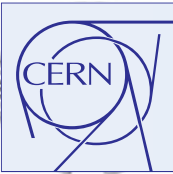




Identification of Neutrinos

The presence of neutrinos is deduced from the imbalance in the transverse energy





Identification of Muons

Muons identified by their penetration through about 10λ of calorimeter material
The material of calorimeters absorbs the e 's, γ 's and h^\pm .

Hadron Punchthrough

Energy Loss in Absorber

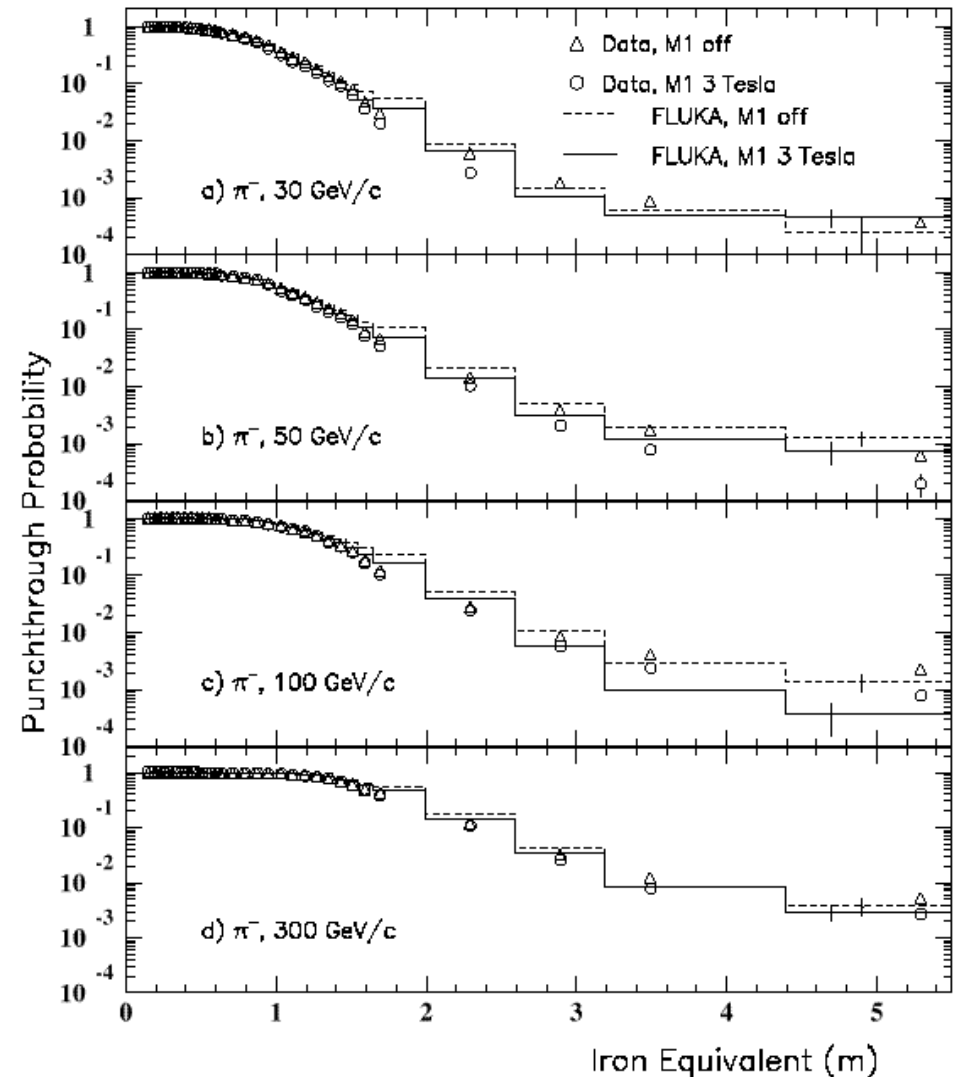
- for $E_\mu \leq 20\text{-}30 \text{ GeV}$ - energy loss fluctuations dominate
- high energy muons generate their own background.

Hard bremsstrahlung (catastrophic energy loss) can spoil μ -tracking. The critical energy for μ in Fe is $E_c \approx 350 \text{ GeV}$.

Hadron Punch-through

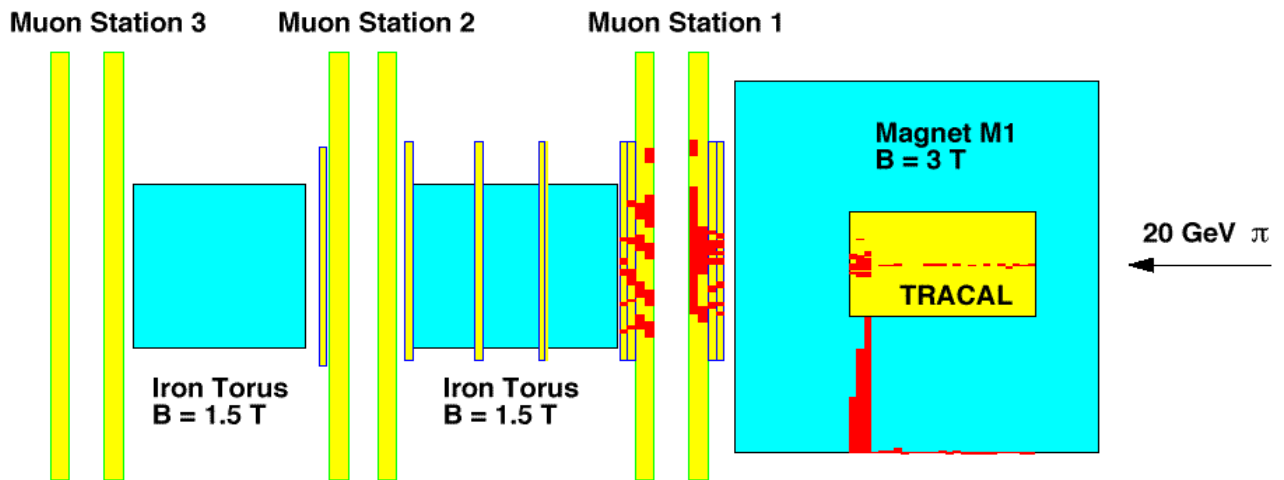
Debris from hadronic showers can accompany muons leading to:

- mis-identification of hadron as μ
- confusion and difficulty in matching μ -tracks (in jets)
- increase in μ trigger rate

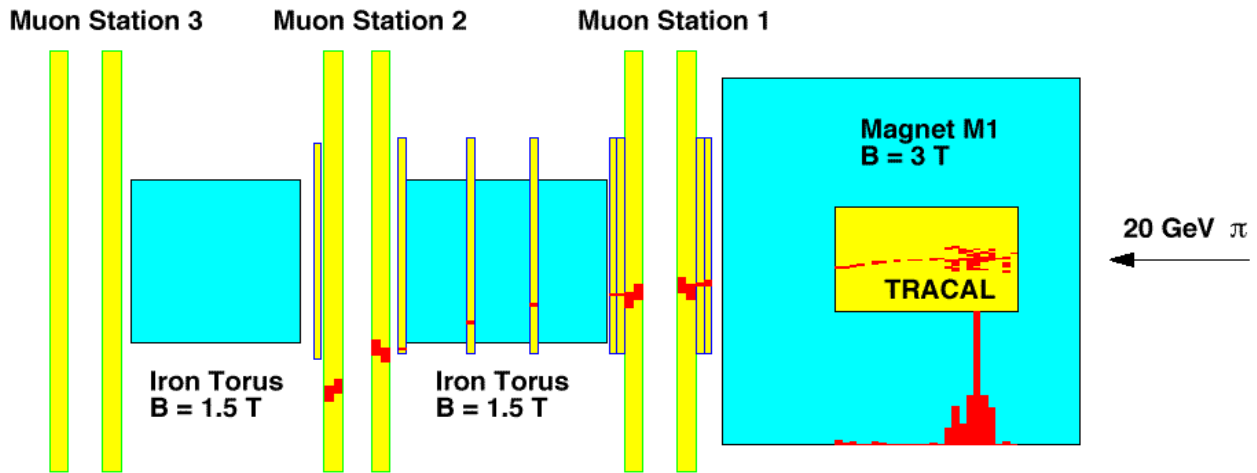


Punchthrough and Radiation

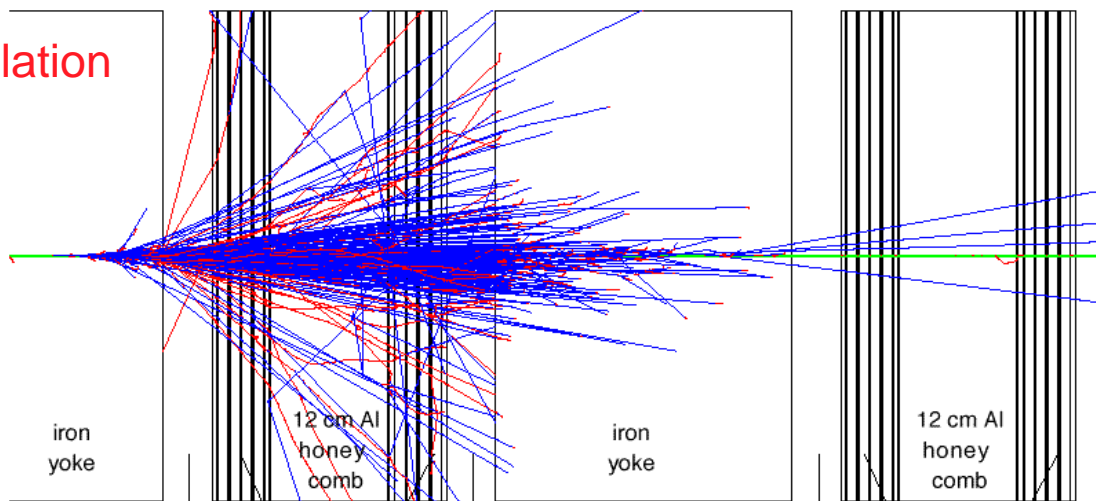
Examples of particles traversing calorimeters and magnetized Fe



RD5



Simulation



Lateral Segmentation
Longit. Segmentation
Preshower Detector

towers of $11 \times 11 \text{ cm}^2$ ($\approx 14 \times 14 X_0$)
3, 6, 10, 7 X_0 / $2 \times 0.7 \lambda$ / $2 \times 2.5 \lambda$
at $3X_0$ with orthogonal strips of pitch 9mm



LHC Experimental Challenge

LHC Machine Parameters

pp collisions at design luminosity	$\sqrt{s} = 14 \text{ TeV}$
bunch crossing interval	$L = 10^{34} \text{ cm}^{-2}\text{s}^{-1}$
pp interaction rate	25 ns
	$10^9 \text{ interactions/s}$

High Interaction Rate

data for only ~100 out of the $40 \cdot 10^6$ crossings can be recorded per second

1st level trigger decision will take ~2-3 μs

⇒ **front-end electronics needs pipelining**

Large Particle Multiplicity

~ $\langle 20 \rangle$ superposed minimum bias events in each crossing at design luminosity

~ 1000 tracks emerge from the interaction region every 25ns

need highly granular detectors with good time resolution for low occupancy

⇒ **large number of channels**

High Radiation Levels

⇒ **radiation hard detectors and electronics**



Muon System at LHC (pp)

Muon identification should be 'easy' at $L > 10^{34} \text{ cm}^{-2}\text{s}^{-1}$

Muons can be identified inside jets

b-tagging

control efficiency of isolation cuts

Can trigger on and identify muons down to $p_t \approx 4 \text{ GeV}$

acceptance for $H \rightarrow ZZ^* \rightarrow 4l$

CP Violation, top physics

Factors that Determine Performance

1st Level Trigger

rate from genuine muons ($b, c \rightarrow \mu X$) is very high

must make a p_t cut with v. high efficiency

large geometric acceptance ($|\eta| \geq 2$)

flexible threshold (p_t in the range 5 - 75 GeV)

Pattern Recognition

hits can be spoilt by

correlated backgrounds : δ 's, e.m. showers, punchthrough

un-correlated : neutrons and associated photons

Momentum Resolution

high momenta : large $\int B \cdot dl$,

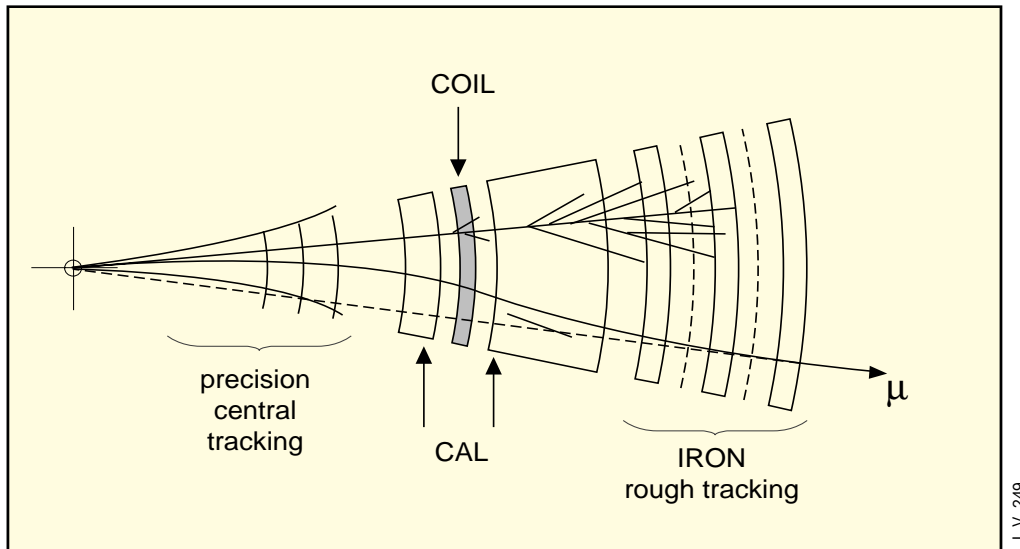
good chamber resolution ($< 100 \mu\text{m}$) & alignment

low momenta : inner tracking measurement is better than

best stand alone measurement

Magnetic Field Configurations Layout of Muon System

1. Measure μ momentum in Inner Tracker and Identify μ in calorimeter and a backing calorimeter / filter
ALEPH, DELPHI, OPAL

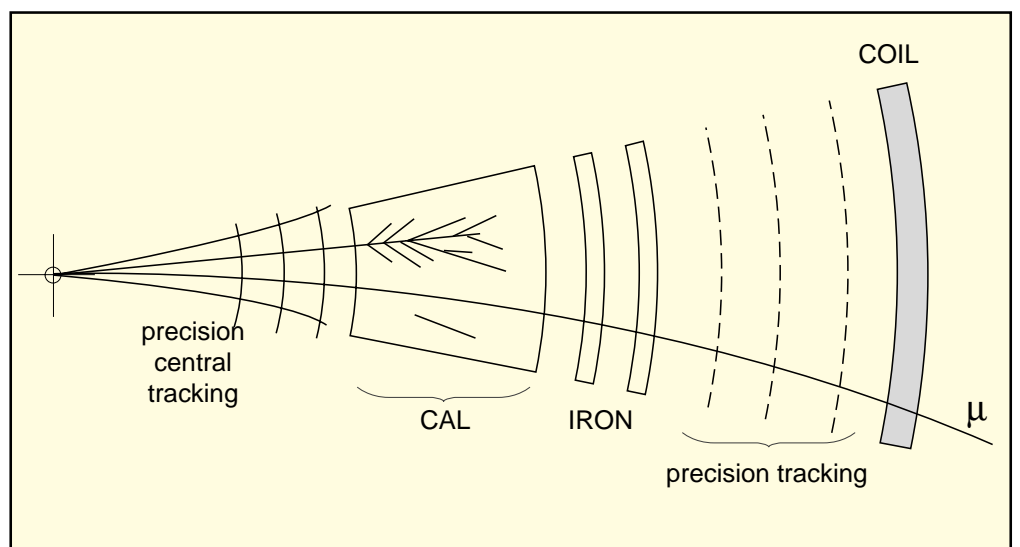


Cheap, but limited to low multiplicity, low rate

2. Identification and Measurement of muons after full absorption of hadrons

Absorb almost all hadrons in calorimeters. Measure μ momentum in relatively clean environment.

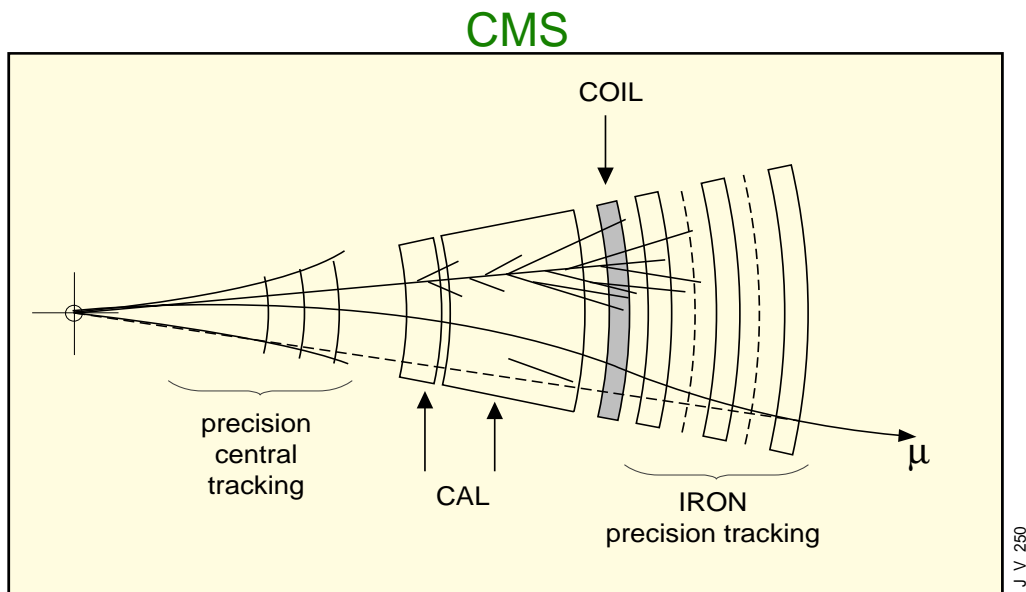
L3, ATLAS with a Toroid



Safe for high multiplicities, need high $BL^2 \rightarrow$ expensive, good stand-alone measurement
+ solenoid for inner tracking and precision measurement of low momentum muons

3. Combined measurement of μ momentum in Tracker and Flux Return - Identify μ after full absorption of hadrons

High field solenoid after calorimetry. μ momentum precisely measured in inner tracking and after $\approx 10\lambda$ of calorimetry.



combination of the two momentum measurements gives a resolution better than weighted sum of the two

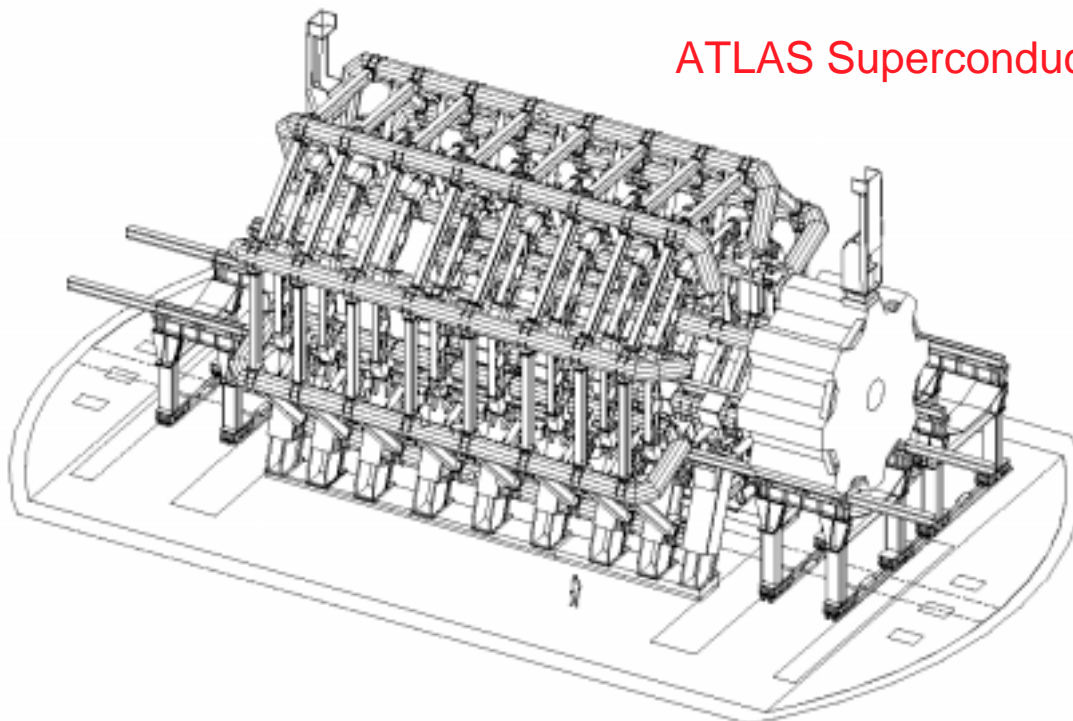
property of a solenoid
high momentum μ tracks point back to vertex after flux return

Advantages

- Constant resolution in p_t over wide η range (field decreases as $1/R$)
- $\int B \cdot dl \approx 1/\sin\theta$ compensating the Lorentz boost in forward direction
- good stand alone resolution - large BL^2
- reduce impact of muon radiation and soft hadron punchthrough

Drawbacks

- Bending not in transverse plane
- Need a solenoid to provide field for central tracker \Rightarrow 4 magnets
- Solenoid coil before or after ECAL ?



ATLAS Superconducting Toroids

For unambiguous sign measurement $\Delta p/p \leq 10\%$ measurement ,
 $\langle B \rangle \approx 0.6T$ over ≈ 4.5 m
 \Rightarrow sagitta of 0.5 mm for $p_t = 1$ TeV $\mu \Rightarrow$ measure sagitta to 50 μ m

Ampère's Theorem : $2\pi RB = \mu_0 nI \Rightarrow nI \approx 20 \times 10^6$ At
 $\Rightarrow 2.5 \times 10^6$ At for 8 coils, $2 \times 2 \times 30$ turns
 $\Rightarrow I \approx 20$ kA \Rightarrow **superconducting coils**

Challenge

- Design of structure capable of holding the magnetic forces
- How to dissipate energy (1.5 GJ) in case of a quench?
- Spatial and alignment precision over large surface area.

Muon Momentum Measurement

Tracking in air-core magnetic field (e.g. ATLAS)

$$\frac{\Delta p}{p} = 26.7 \sigma \sqrt{\left(\frac{1}{2N_1} + \frac{1}{N_2}\right)} \frac{p}{BL^2} \quad (\%)$$

p in GeV, B in T, σ and L in m

ATLAS : $\sigma \approx 70 \mu\text{m}$, $N_i \approx 6$, $B \approx 0.6 \text{ T}$, $L \approx 4.5 \text{ m}$

$\rightarrow \Delta p/p \approx 0.8\%$ at 100 GeV

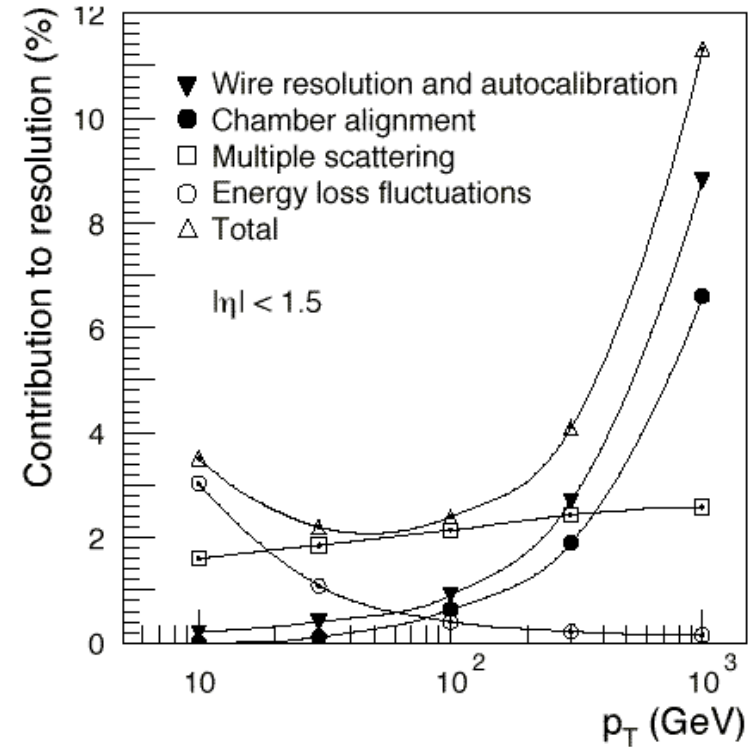
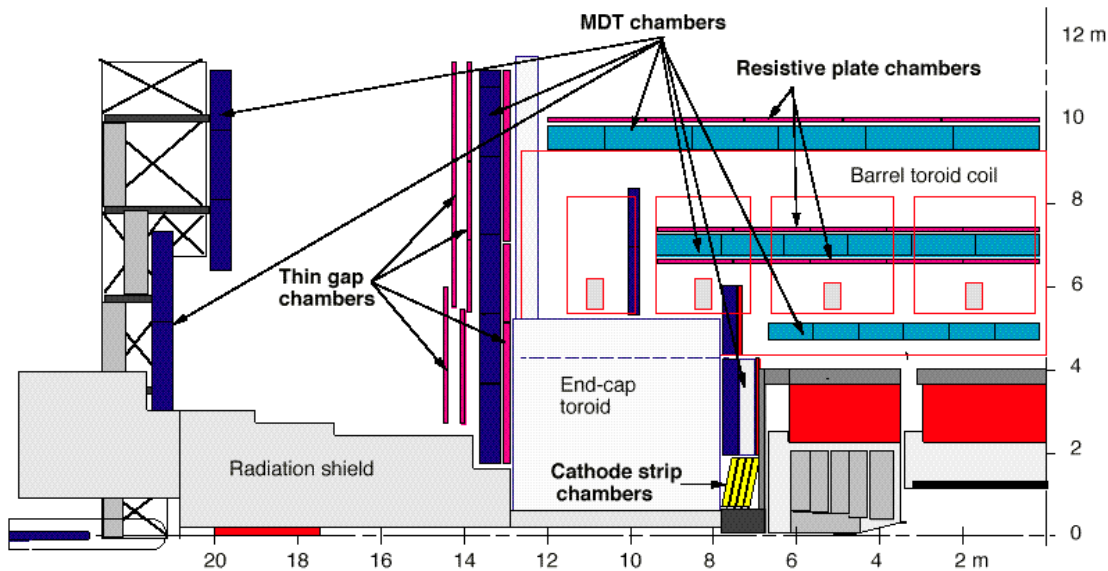


Figure 1-24 Contributions to the momentum resolution of the muon spectrometer, averaged over $|\eta| < 1.5$ and azimuthal angle, in a standard sector

Advantages

- Large $\int B \cdot dl$ for modest size
- bending in transverse plane ($r/\phi_{\text{beam}} \approx 20 \mu\text{m}$!) and starts at primary vertex

Drawbacks

- Momentum resolution worsens as $L_c \cdot \tan\theta/r_c$
- Large stored energy
- Conductor design for large fields

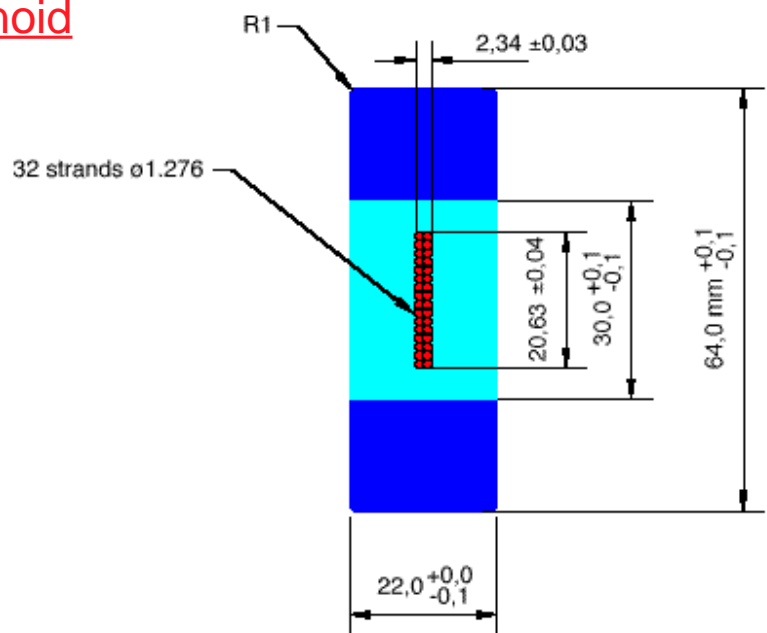
CMS Superconducting Solenoid

Field	4 T
Inner Bore	$\phi \approx 6 \text{ m}$
Length, L	13 m
Current	19.5 kA
Stored Energy	2.7 GJ
Hoop Force	$\approx 64 \text{ atm}$

$$\mathbf{B} = \mu_0 \mathbf{n} \mathbf{l}$$

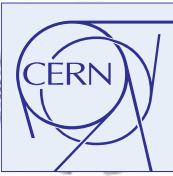
$$n - \text{no. of turns/m} = 2168$$

$$\Rightarrow I \approx 20 \text{ kA}$$

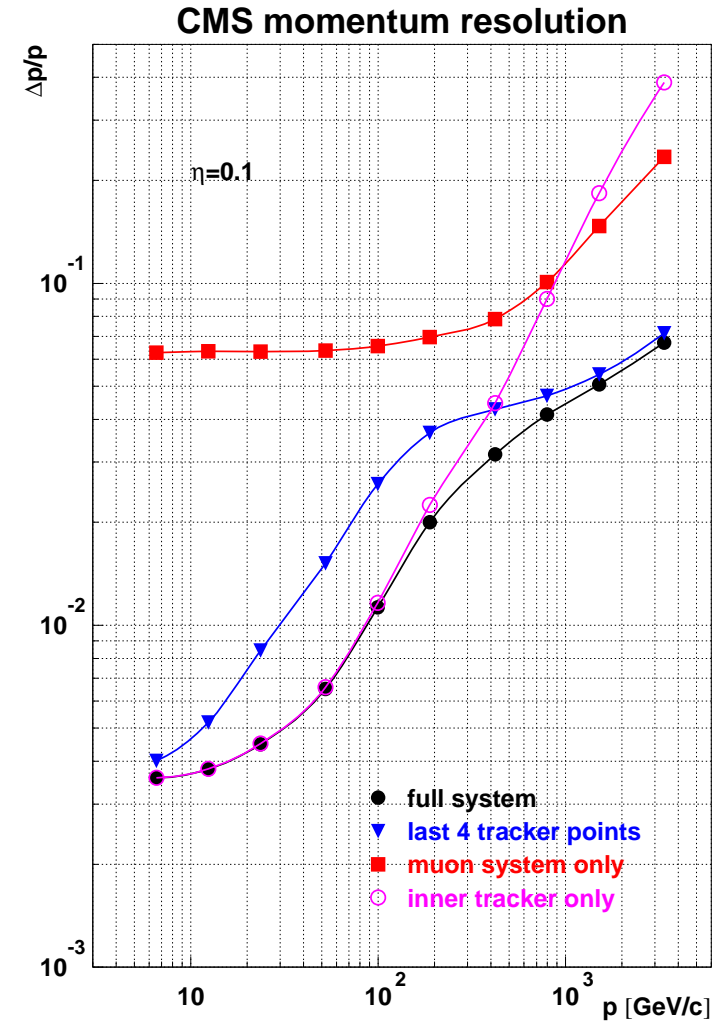
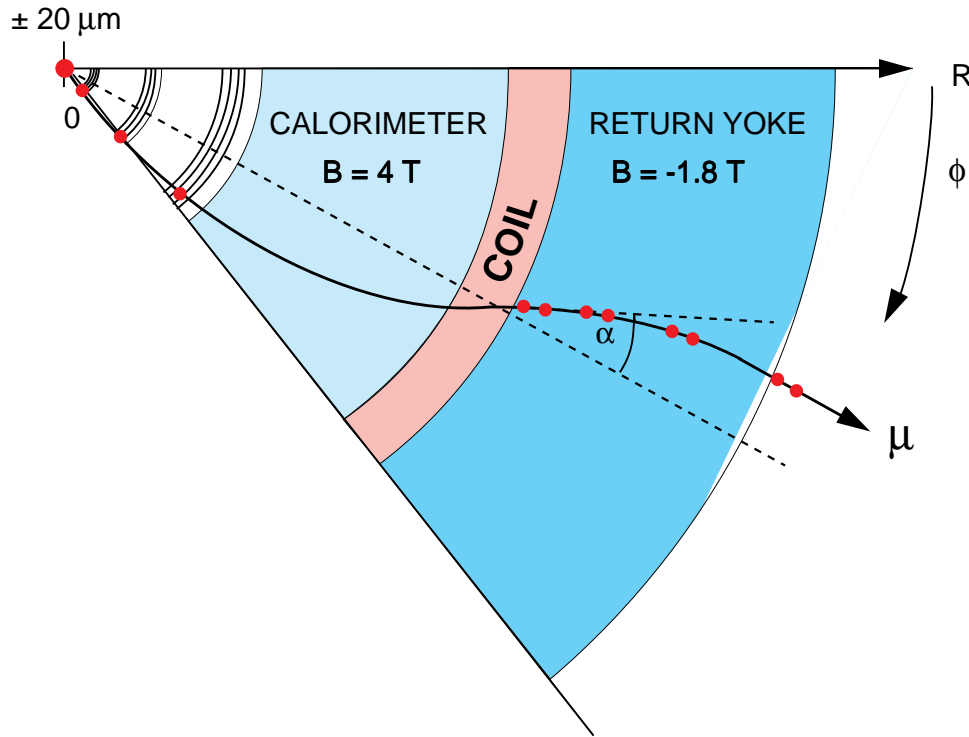


Challenge

- 4-layer winding needed to carry enough current to generate 4T
- Design of reinforced superconducting cable



CMS Solenoid

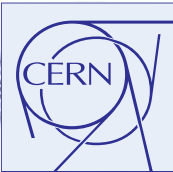


Tracking in Magnetized Iron (CMS)
(in multiple scattering dominated regime)

$$\frac{\Delta p}{p} \approx \frac{40\%}{B\sqrt{L}}$$

$B \sim 1.8\text{T}$, and $L \approx 1.5\text{ m}$

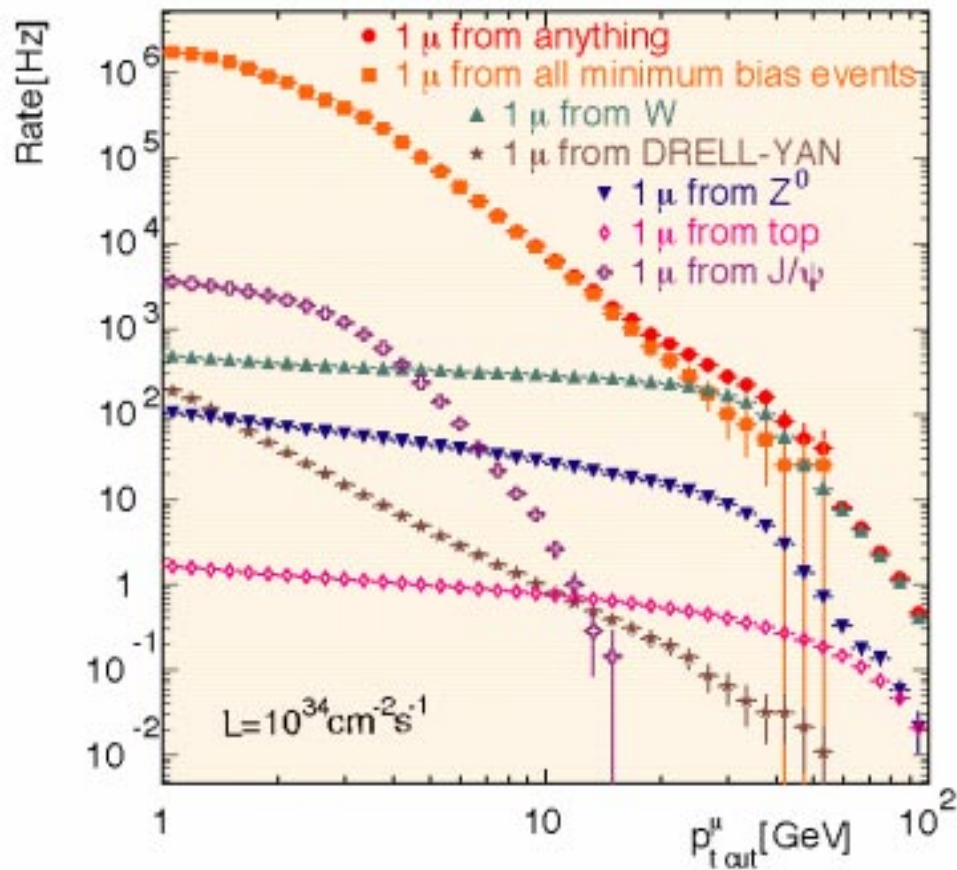
BUT stand-alone measurement is much better !



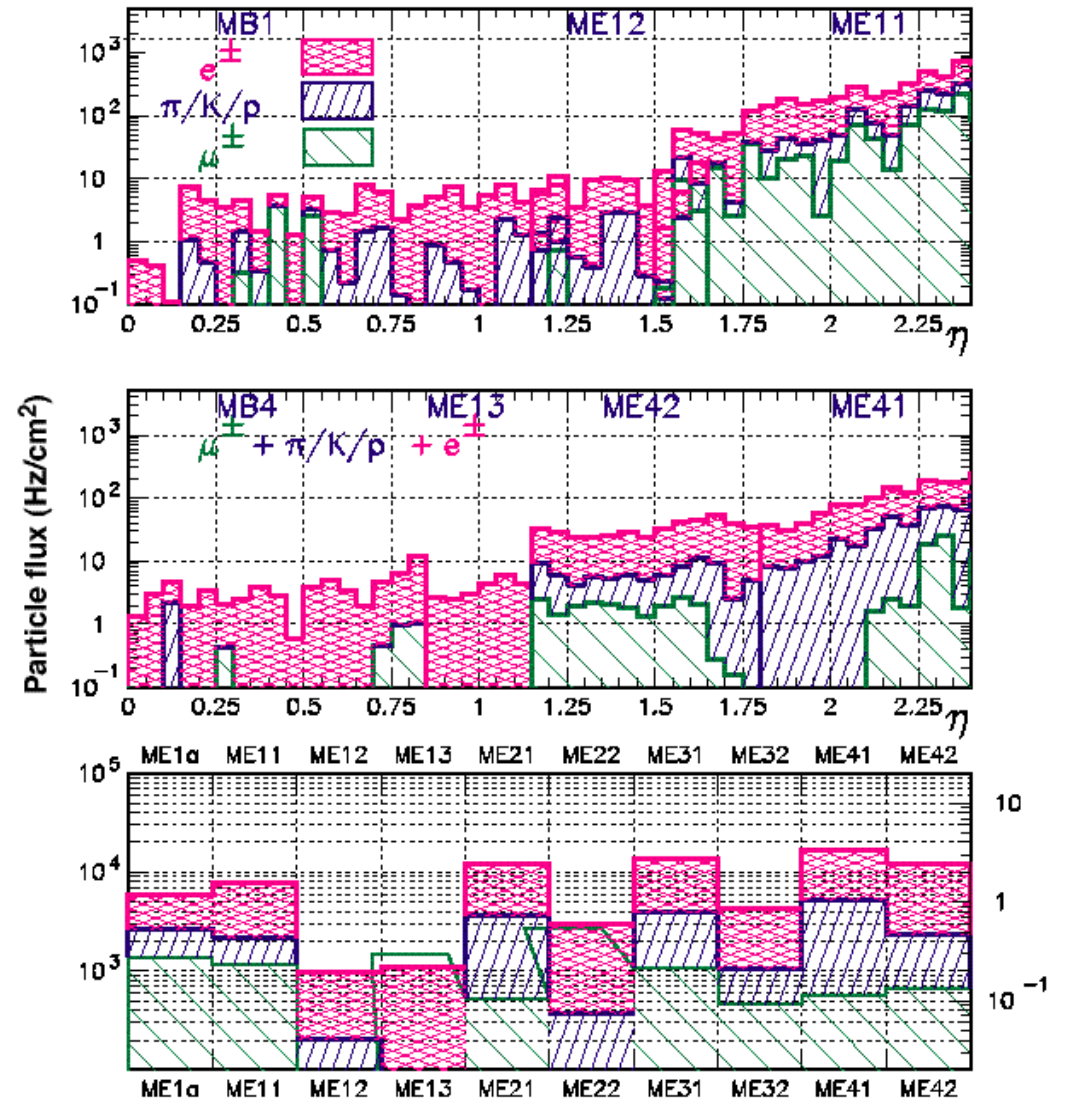
Rates in Muon System

Hit rates from various sources in CMS Muon System

Single muon rates for $|\eta| \leq 2.4$



Setup TDR: Madison baseline





Muon Detectors

Two kinds of chambers - complementary functions

Accurate position measurement for momentum determination
Level-1 Trigger

Drift Chambers - Low rate environment - Barrel ($t_{\text{drift}} \approx 400 \text{ ns}$)

Cathode Strip Chambers - High rate environment - Endcaps (fast)

Less accurate position measurement but fast response ($< 25 \text{ ns}$)

Level-1 Trigger

Resistive Plate Chambers / Thin Gap Chambers

Operating Parameters

Principle of Operation

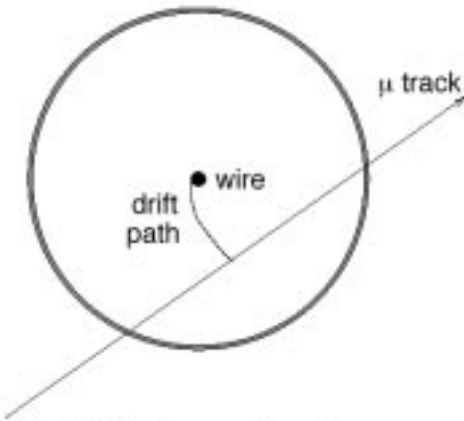


Figure 5-2 Drift tube operation in a magnetic field with curved drift path.

$$\begin{aligned} \phi_{\text{cathode}} &= 30 \mu\text{m} \\ \phi_{\text{wire}} &= 50 \mu\text{m} \text{ (W-Re)} \end{aligned}$$

Parameter	Design value
Gas mixture	Ar/N ₂ /CH ₄ (91%/4%/5%)
Gas pressure	3 bar absolute
Track ionization	330 / cm
Gas gain	2 × 10 ⁴
Wire potential	3270 V
Electric field at the wire	205 × 10 ³ V/cm
Electric field at the wall	340 V/cm
Maximal drift time	500 ns
Averaged drift velocity	30 μm/ns
Effective threshold	22 nd electron
Resolution	80 μm

Drift Time-Distance Measurement

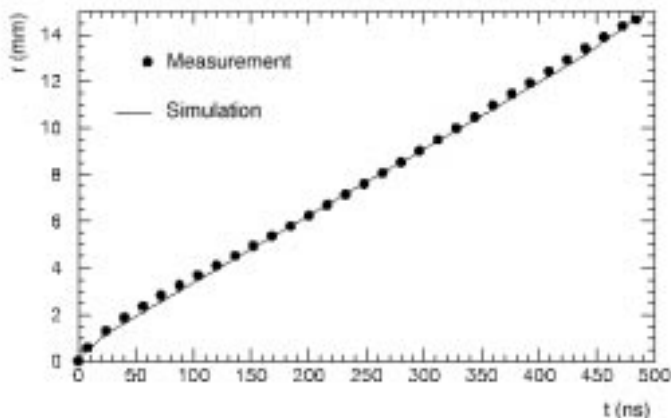


Figure 5-1 Relation between measured drift time and corresponding drift length in the absence of a magnetic field. Ar/N₂/CH₄ - 91 : 4 : 5 mixture.

Spatial Resolution as a function of drift distance

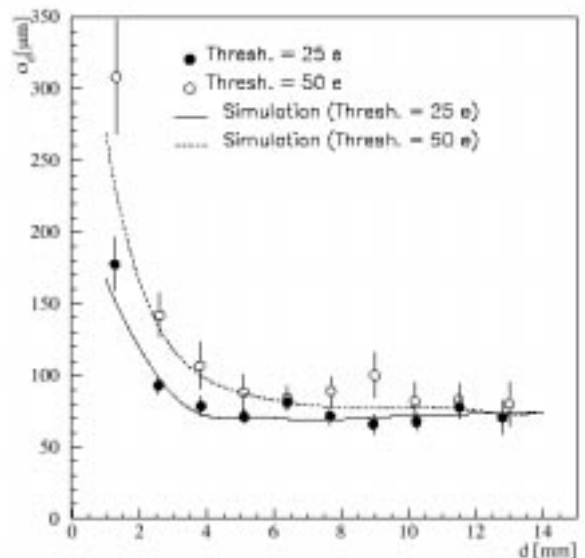
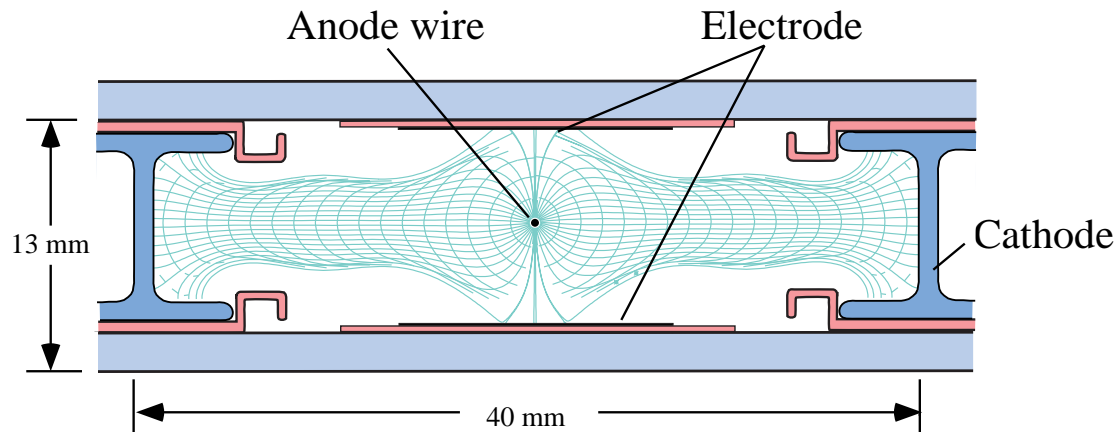


Figure 5-4 MDT resolution as a function of the drift distance, for an Ar/N₂/CH₄ (91/4/5 mixture). The curves correspond to two discriminator threshold settings.

Drift Cell Layout

3 field shaping electrodes assure a linear space-time relationship

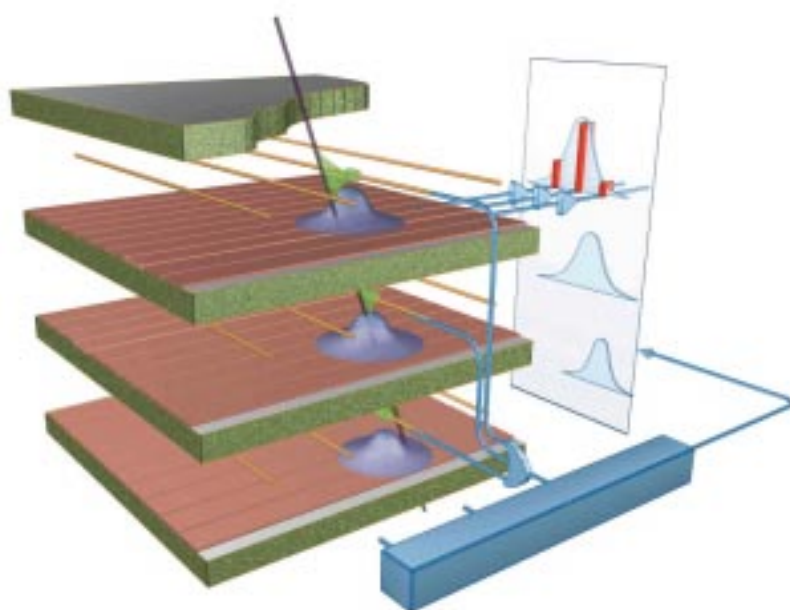


Operating Parameters

Nominal mixture	Ar - CO ₂ (85% - 15%)
Nominal voltages	strips at 1800 V, wires at 3600, I-beams at -1800V
Gain (nominal setting)	$9 \cdot 10^4$
Typical charge	1 pc
Cumulated charge	0.1 C/cm in 10 years of operation

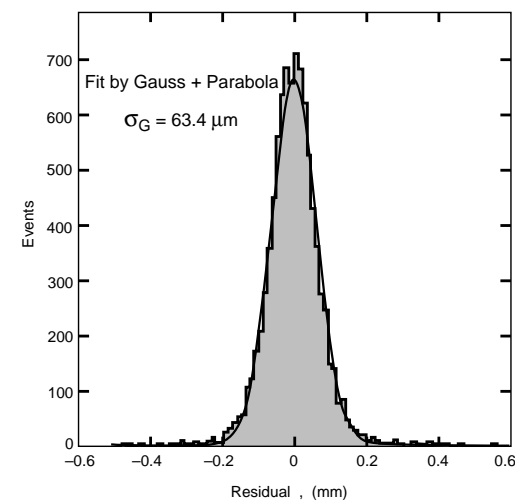
Cathode Strip Chambers

Principle of Operation



- Precise co-ord measured by interpolation of induced charge on strips
- Stereo coordinate is measured from signals on wires
- Closely spaced wires make CSC a fast detector

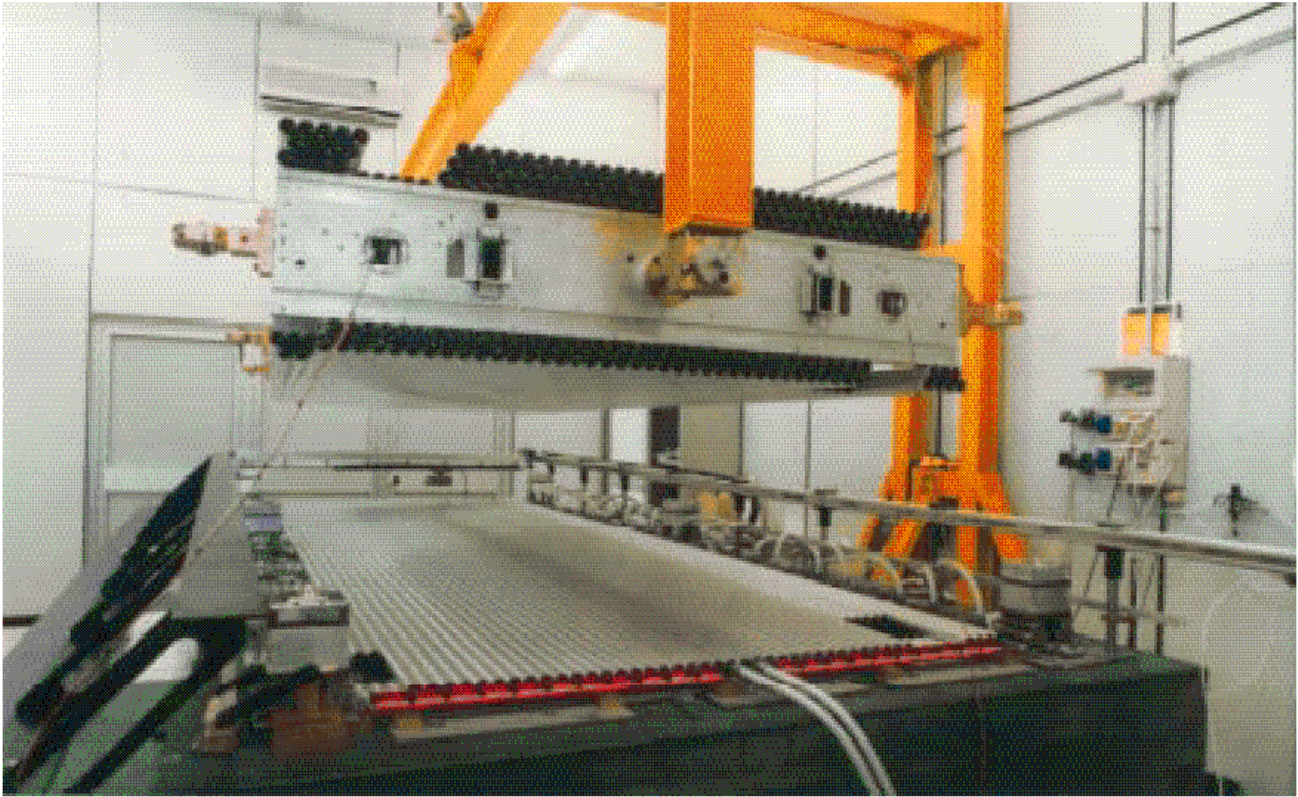
Spatial Resolution



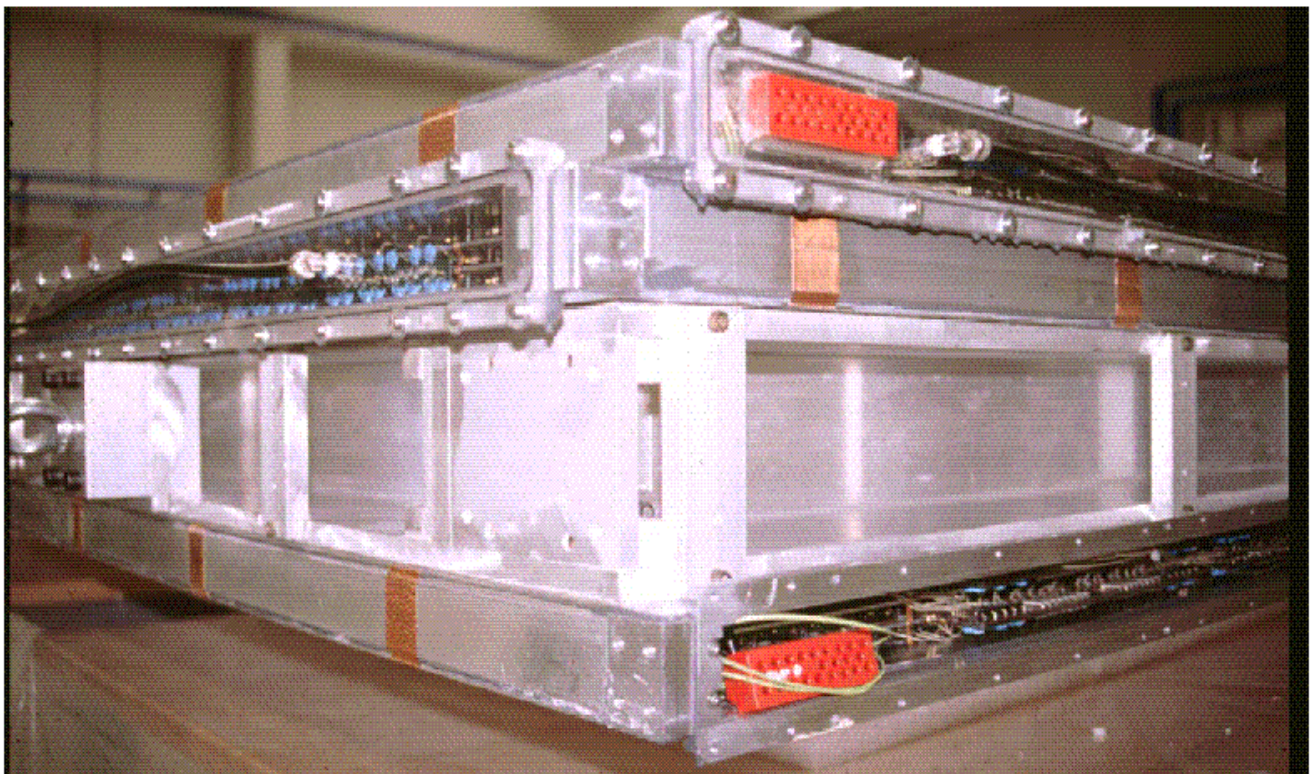
Operating Parameters

Nominal mixture	Ar-CO ₂ -CF ₄ (30:50: 20)
Nominal voltage	3-4 kV
Gain	7.10 ³

ATLAS : Station comprising 6 layers of MDT Tubes



CMS : Station comprising Barrel Drift Tubes



Role of a Tracker

measure the momentum and impact parameter of charged tracks with minimal disturbance

Factors that determine Performance

track finding efficiency - occupancy

momentum resolution

secondary vertex reconstruction

Benefits

precise momentum measurement

electron, τ and b-jet identification

secondary vertex and impact parameter measurement

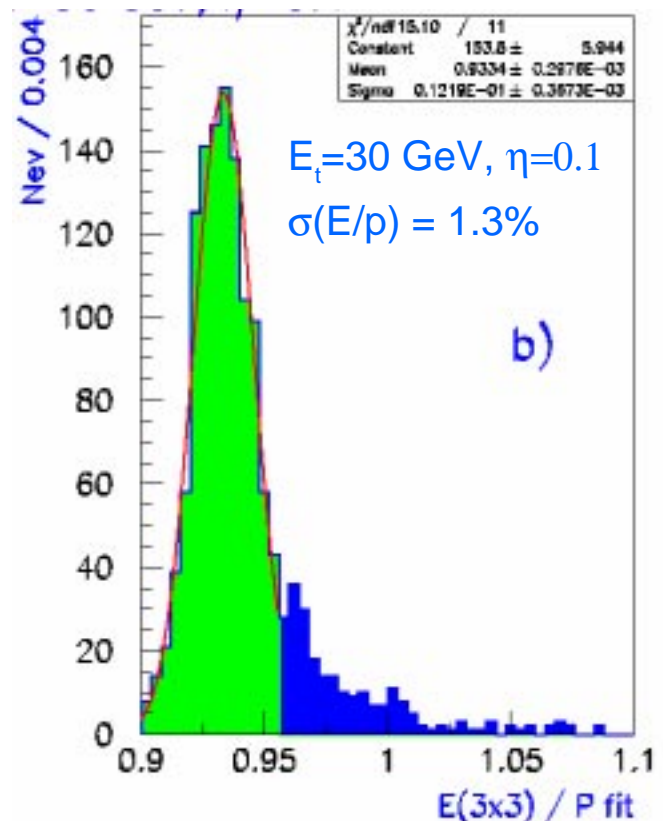
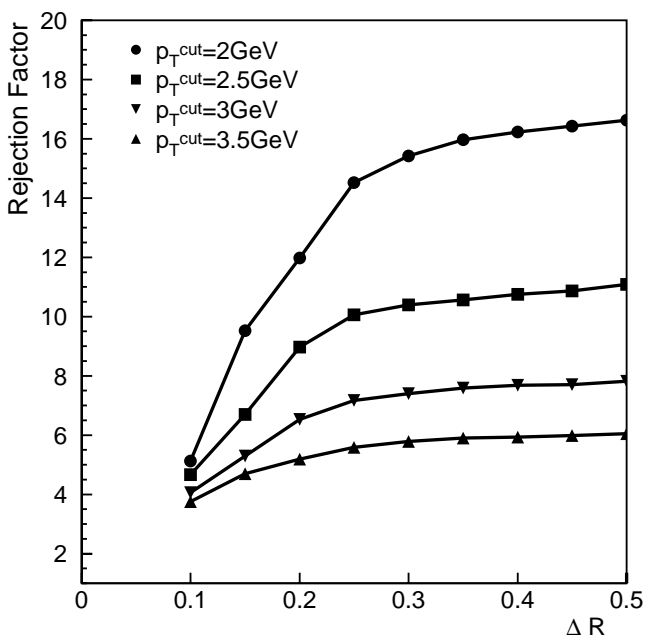
isolation using charged tracks ($p_t > 2$ GeV)

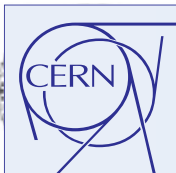
ECAL calibration using p-E matching

only way to "SEE" the event (topological information)

CMS: Isolation - $E(3 \times 3)/E(7 \times 11) > 0.92$

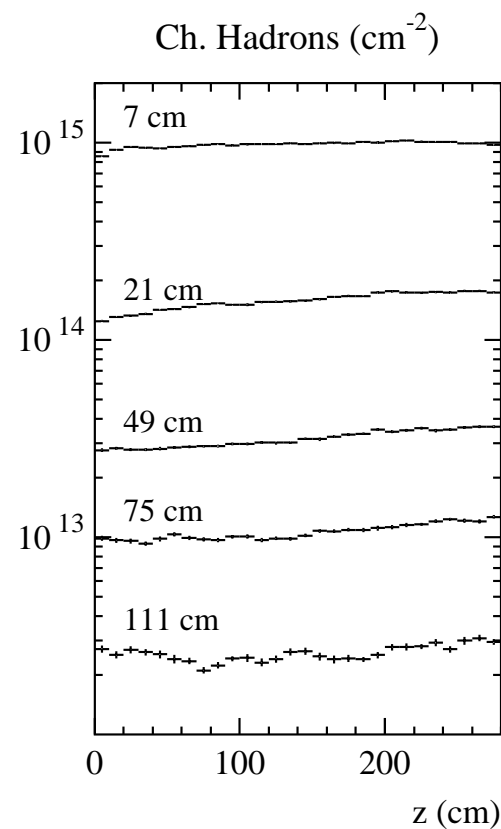
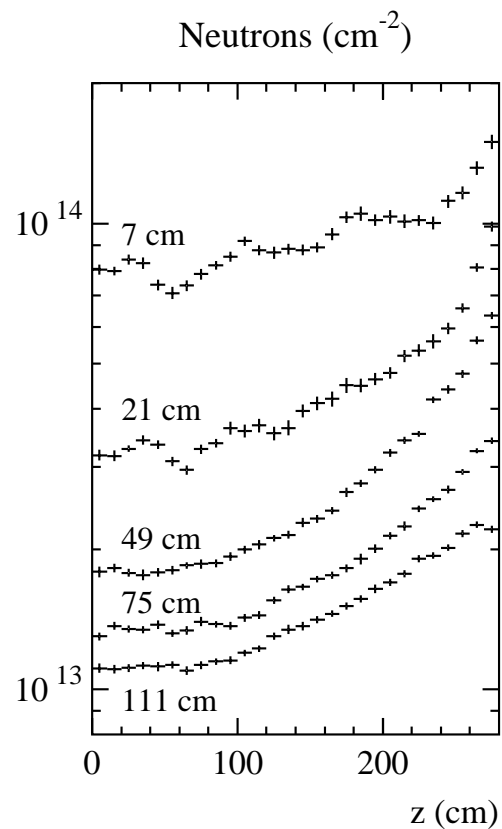
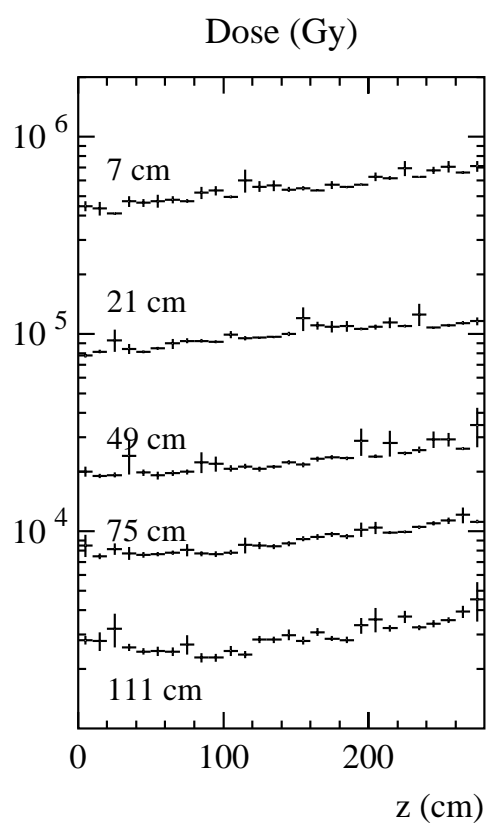
CMS : isolation using charged tracks





Radiation Levels in Inner Tracking

Radiation Levels in CMS Inner Tracker (integrated over 10 years of operation i.e. $5 \cdot 10^5 \text{ pb}^{-1}$)



$\leq 4 \cdot 10^7 \text{ h}^\pm/\text{cm}^2/\text{s}$
pixels ($\approx 10^4 \mu\text{m}^2$)
occupancy $\approx 10^{-4}$

$\leq 4 \cdot 10^6 \text{ h}^\pm/\text{cm}^2/\text{s}$
Si μ -strip det.
($\approx 10 \text{ mm}^2$)
occupancy $\approx 1\%$

$\leq 4 \cdot 10^5 \text{ h}^\pm/\text{cm}^2/\text{s}$
Gas detectors.
($\approx 1 \text{ cm}^2$)
occupancy $\approx 1\%$



Charged Particle Tracking Devices

Bubble Chambers

Many discoveries in the 60' and 70's

Now Obsolete

Low repetition rates (< 10 Hz)

HEP moved on to study of low σ processes

Lack of triggering capability

Electronic Bubble Chambers

Time Projection Chambers

3-D spatial information with high granularity

Some particle identification using dE/dx

Not used in pp experiments at LHC

Long drift times (25 - 45 μ s)

Suitable for LEP - low event rate (+ long bunch crossing time)

Tracking Detectors for LHC

Search for rare processes

very high particle rates ($4 \cdot 10^{10}$ particles/s emerging from interaction region)

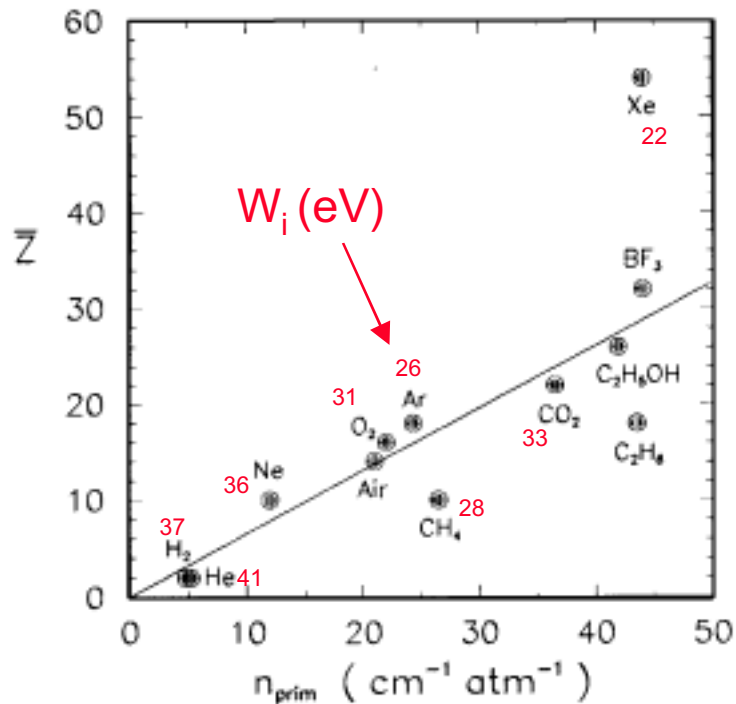
very short bunch crossing time (25 ns)

semi-conductor pixels, microstrip detectors

short drift time (< 50 ns) gaseous detectors (straws, MSGCs etc)

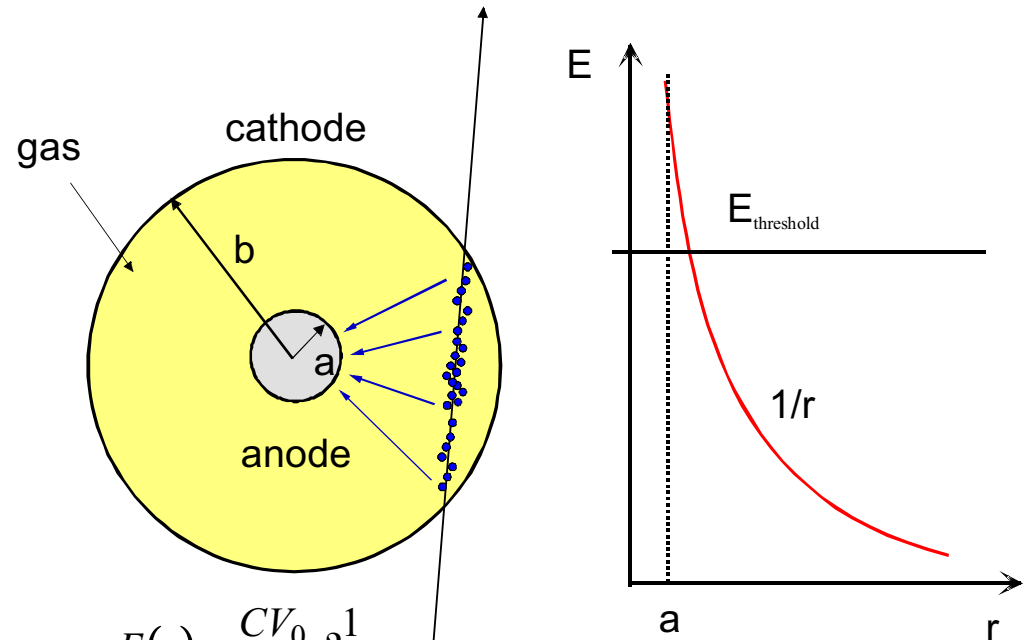
Proportional Wire Chambers

Fast charged particles ionise atoms of gas
 if $W =$ energy to create an e-ion pair then
 total ionisation $n_{\text{total}} = \Delta E/W = (dE/dx)\Delta x/W$
 $n_{\text{total}} \approx 3-4 n_{\text{primary}}$



≈ 100 electron-ion pairs are not easy to detect
 noise of a fast amplifier $ENC \approx 1000 e !$

Need amplification in gas



$$E(r) = \frac{CV_0}{2\pi\epsilon_0} \frac{1}{r}$$

$$V(r) = \frac{CV_0}{2\pi\epsilon_0} \ln \frac{r}{a}$$

$C =$ capacitance / unit length

Electric field close to the wire is sufficiently high
 for the electrons to gain enough energy to ionise
 further \rightarrow exponential increases in e-ion pairs



Gain in Wire Chambers

Prob. an electron will produce an ionising collision with an atom in distance dr is

$$N_a \sigma_i dr \quad \text{where } N_a = \text{no. of atoms/unit volume}$$

Increase in no. of electrons after dr is

$$dn = n N_a \sigma_i dr$$

Let $N_a \sigma_i = \alpha$ i.e. larger the value of α , the more the collisions per unit distance.

Define $\alpha = 1 / \lambda_{\text{coll}}$ λ - mean free path length

(a known as the 1st Townsend coeff. giving e-ion pairs/cm)

$$dn = n \alpha (r) dr$$

α is a function of r as it varies with electric field which usually varies with r

$$\therefore n = n_0 \exp \int_a^{r_c} \alpha(r) dr$$

where n_0 = no. of electrons present initially

$$\text{Gain } M = \frac{n}{n_0} = \exp \int_a^{r_c} \alpha(r) dr$$

$$\text{infact } M \propto e^{CV_0}$$

Consider what happens near a anode wire

r (μm)	E (kV/cm)	α (ip/cm)	$\lambda=1/\alpha$ (μm)
10	200	4000	2.5
20	100	2000	5
100	20	80	125
200	10	≈ 1	1 cm

50% (90%) of electrons produced ≈ 2.5 (10) μm from anode wire !



Detector Gas Mixtures

Avalanche multiplication occurs in all gases

BUT desire low working voltage, stable operation at high gain, high rate capability, long lifetime, fast recovery

Principal component of a desirable gas - noble gas (e.g. argon)

- allows multiplication at relatively low E-field
- does not have molecules, produces only elastic scattering (little loss of energy)

Argon gives more primary ionization than He or Ne (Kr and Xe give even more but are expensive)

Counter full of argon does not give stable operation

- during avalanche process many excited Ar atoms decay emitting UV photons (e.g. 11.6 eV for Ar)
- UV γ s strike cathode (usually Cu clad with ionization threshold of 7.7 eV) and eject photoelectrons which give rise to another avalanche

⇒ **positive feedback - continuous discharge**

Chamber filled with pure Ar suffers such breakdown at low gain

Polyatomic gases have many non-radiative vibrational and rotational excited states over a wide energy range

If chamber contains a fraction of such a gas, its molecules will absorb energy from excited argon atom by colliding with it or dissociating it into smaller molecules

Since $\tau_{\text{emission}} \gg \tau_{\text{collision}}$ **UV γ emission is 'quenched'**

Presence of **quenching gas** can give enormous increase in stable obtainable gain e.g. isobutane (C_4H_{10}), Methane (CH_4)

common property of hydrocarbon, alcohol families

Operation Modes of Chambers

At very low voltages, charges begin to be collected but recombination is still the dominant process

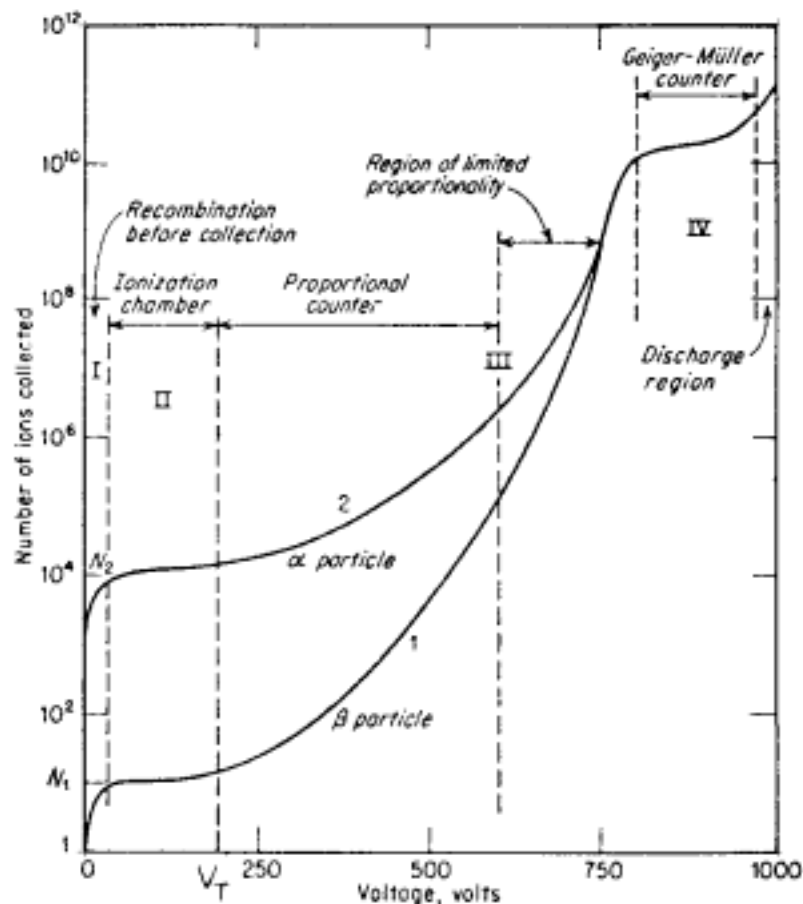
ionization mode - at higher voltage full charge collection begins

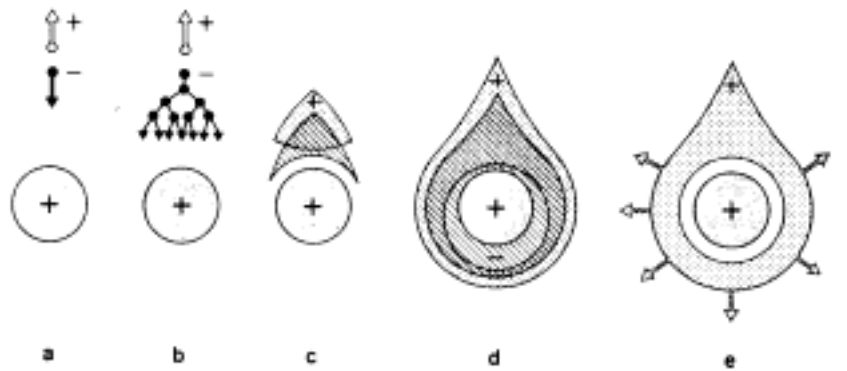
multiplication - at a certain voltage called the threshold voltage (V_T) the electric field close to the surface of the anode is large enough to begin process of multiplication

proportional mode - increasing V_0 above V_T results in gains $> 10^4$ with detected charge \propto primary deposited charge

limited proportionality - at even higher voltages proportionality is gradually lost - consequence of electric field distortions due to space charge around the anode

Geiger mode - the region of limited proportionality eventually ends in a region of saturated gain - same size of signal independent of original deposition





Consider a single primary electron drifting towards the anode (at ≈ 5 cm/ μ s) into region of increasingly high field

Typically at a radius of few wire radii, electric field is large enough and primary electron gains enough energy to cause ionisation

Due to lateral diffusion a drop-like avalanche surrounding the wire develops

Whole process of avalanche multiplication lasts ≈ 1 ns

Electrons are collected very fast (≈ 1 ns) as drift distance is few μ m

+ve ions drift slowly towards the cathode.

signal on anode and cathode is induced by the moving charges

- electrons move v. short distance and induce very little signal
- ion drift determines the time development and size of induced signal

$$I(t) = \frac{Q}{2t_0 \ln(b/a)} \left(\frac{1}{1+t/t_0} \right) \quad t_0 - \text{characteristic time}$$

Total drift time of ions for Ar at NTP, $a=10\mu\text{m}$, $b=8\text{mm}$, $C=8\text{pF/cm}$, $\mu^+=1.7 \text{ cm}^2 \text{ V}^{-1}\text{s}^{-1}$, $V_0=3 \text{ kV}$ is **550 μ s**.

Time growth is very fast ($\approx 1/1000$ if total drift time)

Normal practice to terminate counter with a resistor R such that signal is differentiated with a time constant RC allowing v. short pulses and high rate capability



Induced Charge

Suppose a charge q located at r from the wire moves a distance dr .
Change in P.E. is

$$dU = q \frac{d\phi}{dr} dr$$

For a cylindrical capacitor, length l , capacitance C /unit length,
electrostatic energy contained in electric field is

$$\frac{1}{2} l C V_0^2$$

$$dU = l C V_0 dV = q \frac{d\phi}{dr} dr$$

induced voltage change is $dV = \frac{q}{l C V_0} \frac{d\phi}{dr} dr$

Assume that <multiplication> occurs at a distance λ from the anode.
Total induced voltage on anode by the electrons is ($E = -d\phi/dr$)

$$V^- = \frac{-q}{l C V_0} \int_{a+\lambda}^a \frac{d\phi}{dr} dr = \frac{-q}{2\pi\epsilon l} \ln \frac{a+\lambda}{a}$$

while that by positive ions is :

$$V^+ = \frac{+q}{l C V_0} \int_{a+\lambda}^b \frac{d\phi}{dr} dr = \frac{-q}{2\pi\epsilon l} \ln \frac{b}{a+\lambda}$$

For $a = 10 \mu\text{m}$, $b = 3 \text{ mm}$ and $\lambda = 1 \mu\text{m}$

$$\frac{V^-}{V^+} = \ln \frac{a+\lambda}{a} \bigg/ \ln \frac{b}{a+\lambda} \approx \frac{0.095}{5.7} \approx 1.7\% !$$

The induced signal from electrons can be ignored. Then for total charge Q ,

$$V(t) = - \frac{Q}{2\pi\epsilon l} \ln \frac{r(t)}{a}$$



Time Development

Consider the drift of +ve ions with drift velocity

$$W^+ = \frac{dr}{dt} = \mu^+ \frac{E}{p} \qquad \frac{dr}{dt} = \mu^+ \frac{CV_0}{2\pi\epsilon} \frac{1}{r} \frac{1}{P}$$

where μ^+ the ion mobility ($\approx 1 \text{ cm}^2 \text{ V}^{-1}\text{s}^{-1}$), E is the electric field strength and P the pressure

Radius of shell at time t

$$\int_a^r r \, dr = \frac{r^2 - a^2}{2} = \int_0^t \mu^+ \frac{CV_0}{2\pi\epsilon P} dt$$

$$r(t) = \sqrt{a^2 + \mu^+ \frac{CV_0}{\pi\epsilon P} t} = a \sqrt{1 + \frac{t}{t_0}}$$

$$t_0 = \frac{a^2 \pi\epsilon}{\mu^+ CV_0} = \frac{a^2}{\mu^+} \frac{\ln(b/a)}{V_0}$$

Combining with (a)

$$V(t) = - \frac{Q}{2\pi\epsilon l} \ln \frac{r(t)}{a} = - \frac{Q}{4\pi\epsilon l} \ln \left(1 + \frac{t}{t_0} \right)$$

If voltage across counter is held constant, then charge must flow onto anode to provide a voltage across the capacitance lC which compensates the voltage between the anode and the +ve shell

$$Q(t) = -lC V(t) = l \frac{2\pi\epsilon}{\ln(b/a)} V(t)$$

The induced current then is

$$I(t) = \frac{Q}{2t_0 \ln(b/a)} \left(\frac{1}{1+t/t_0} \right)$$

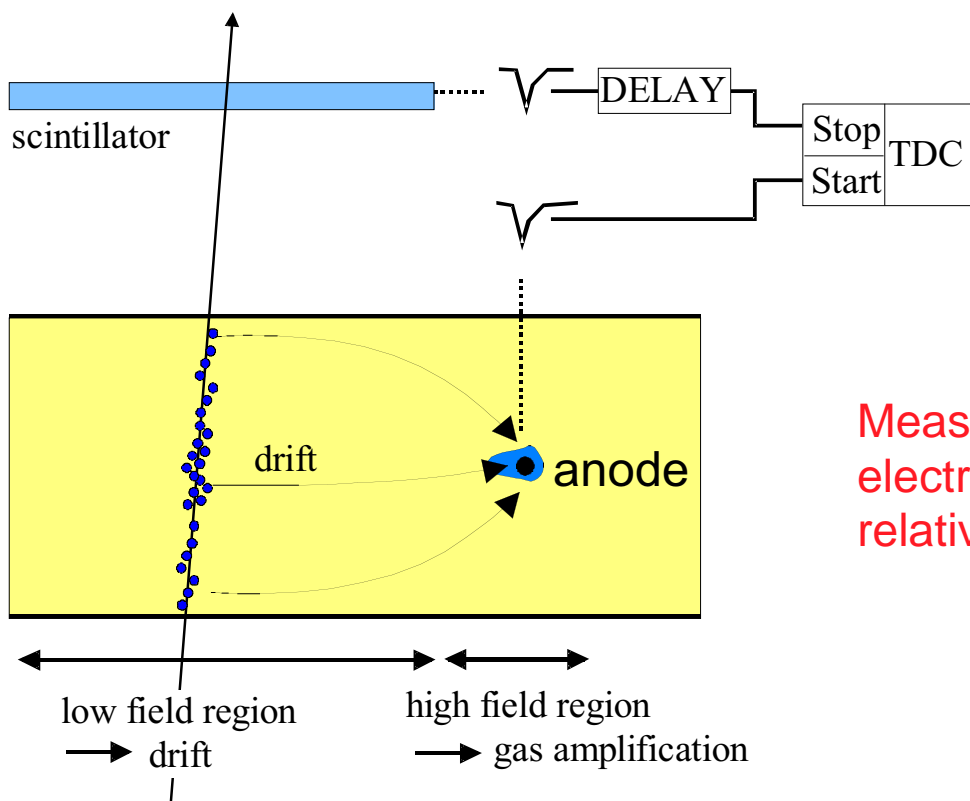
Total drift time of ions

$$T = \frac{t_0}{a^2} (b^2 - a^2)$$

E.g. Ar at NTP, $a=10\mu\text{m}$, $b=8\text{mm}$, $C=8\text{pF/cm}$, $\mu^+=1.7 \text{ cm}^2 \text{ V}^{-1}\text{s}^{-1}$, $V_0=3 \text{ kV}$ is **550 μs** .

Spatial information obtained by measuring time of drift of electrons

- need a trigger to signal the arrival of particles (bunch crossing or scintillator)



Measure arrival time of electrons at sense wire relative to a time t_0

Advantage

relatively small no. of wires and electronics needed

Choice of Gas

- high purity - electrons captured if electronegative impurity present the longer the drift path, the higher the required purity level
- gas exhibiting drift velocity saturation at not too high a field drift velocity less sensitive to field inhomogenities, operating voltage, temperature etc.
- fast gas - for high counting rates max. counting rate limited by drift time (10^4 count/s/mm of wire)



Time Projection Chamber

TPC → 3-D imaging drift chamber - electronic bubble chamber

Basic Structure

- large gas filled cylinder with a thin HV electrode middle plane
- uniform axial parallel electric and magnetic fields (along axis)
- ends of cylinder covered by sector arrays of prop. anode wires
- parallel to each wire is a cathode strip cut in rectangular pads

e.g. ALEPH TPC

Dimensions : $\phi = 3.6$ m, $L = 4.4$ m, (91%Ar:9%CH₄) at 1 atm

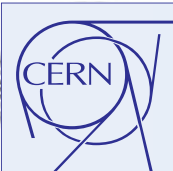
Electron drift time = 45 μ s

r- ϕ interpolating signals induced on precisely located cathode pads
z from drift time
dE/dx information

diffusion significantly reduced by B-field

performance improved by laser calibration + p, T corrections

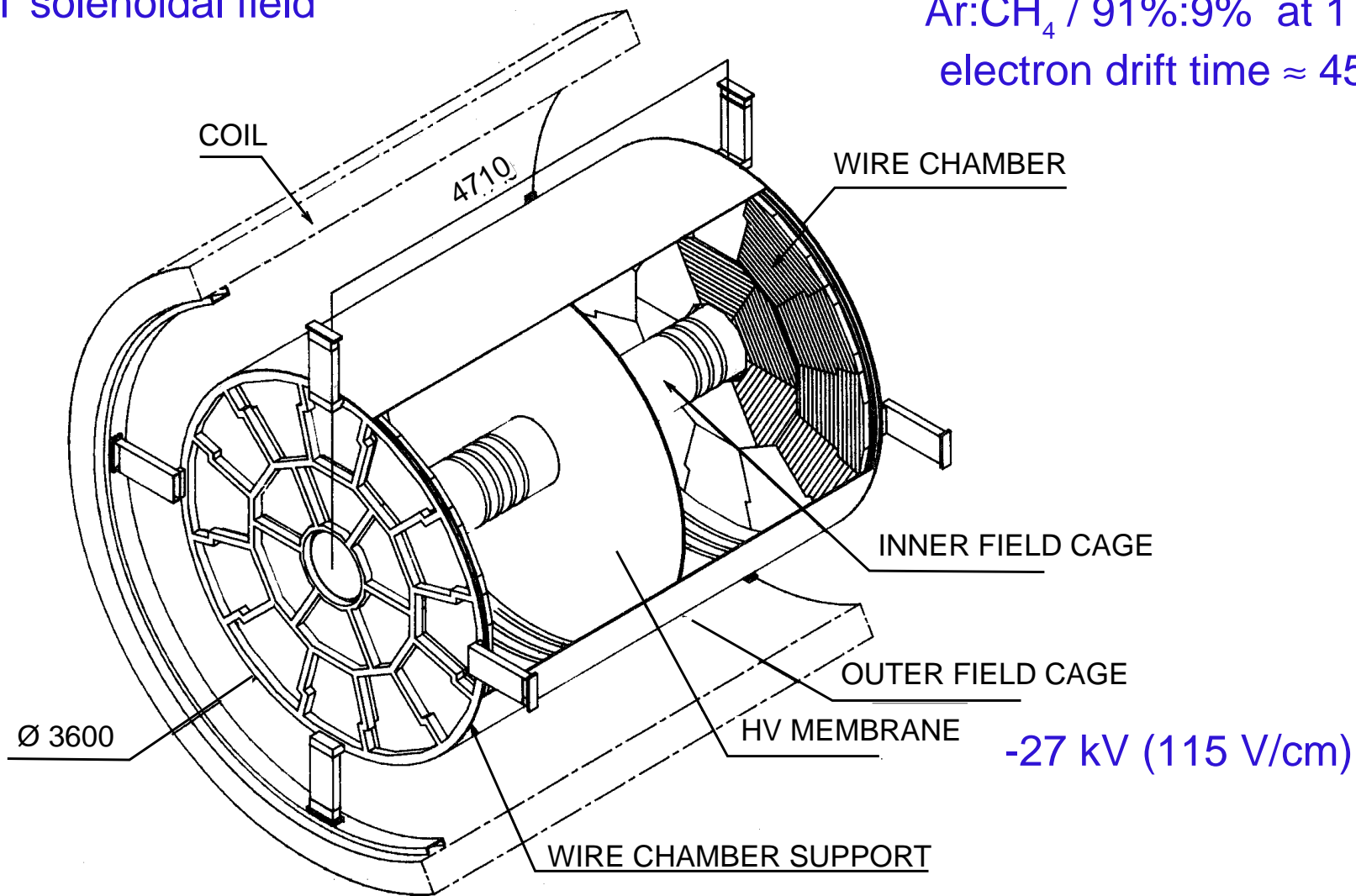
$$\sigma_{R\phi} \approx 170 \mu\text{m}, \sigma_z \approx 740 \mu\text{m} \quad \frac{\sigma_{p_t}}{p_t} \approx 0.1\% p_t \oplus 0.3\% (GeV)$$



Time Projection Chamber

1.2 T solenoidal field

Ar:CH₄ / 91%:9% at 1 atm
electron drift time $\approx 45 \mu\text{s}$



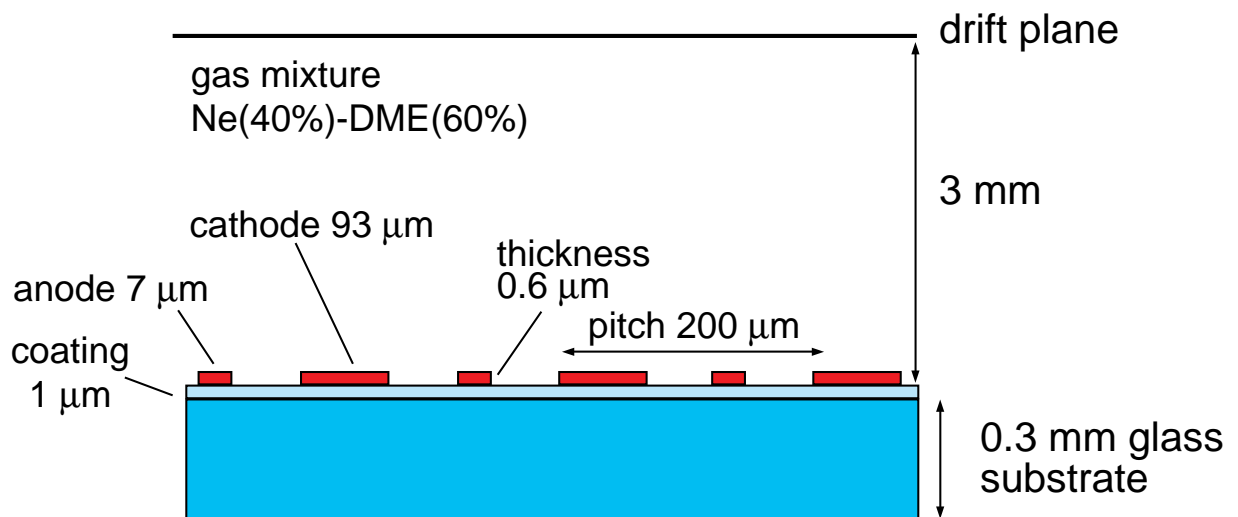
MSGCs are made with micro-electronics technology
 precision of lithographic techniques is $\approx 0.1 - 0.2 \mu\text{m}$

Overcome two major limitations of MWPCs

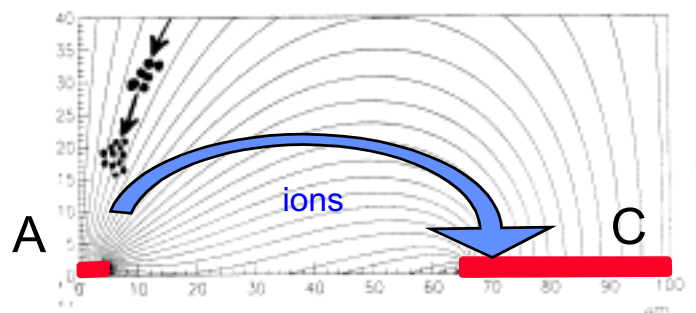
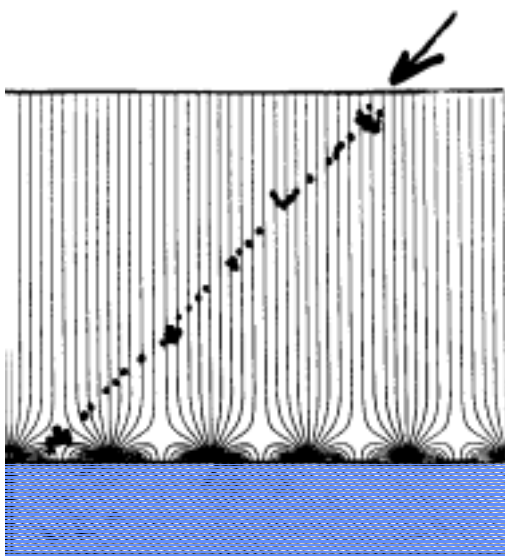
- spatial resolution orthogonal to the wire limited by wire spacing (typically $\approx 1 \text{ mm}$)
- rate capability is limited by long ion collection time (typically $\sim \text{mm}$ taking several tens of μs)

e.g. CMS : 225 m^2 , 6.6 M ch., $r\text{-}\phi$ pitch $200 \mu\text{m}$

Principle of Operation



J_V_255



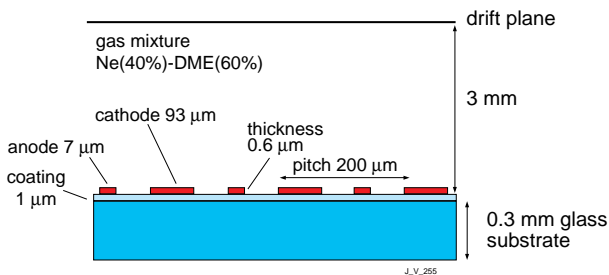
short ion drift distance - $60 \mu\text{m}$!



CMS Microstrip Gas Chambers

Characteristics of CMS MSGCs

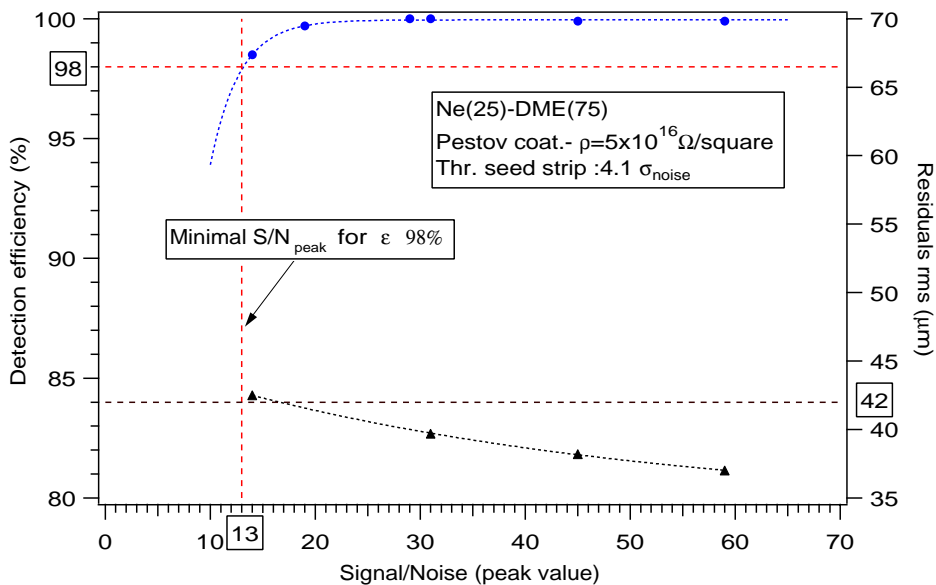
- Substrate 300µm thick Desag 263 glass
- Undercoating allows stable gain and rate independence
- Gold Strips to slow ageing, no attenuation of collected charge along the strip
- Advanced Passivation allows higher gain and robust operation



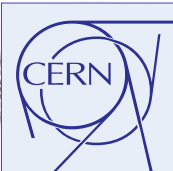
Nominal Operating Parameters

- Mixture Ne-DME (40%-60%)
- Voltage anode at ground
cathode strips at -520 V
drift cathode at -3500V
- Gain 2000
- Rates $\sim 10^6$ particles/mm²/s

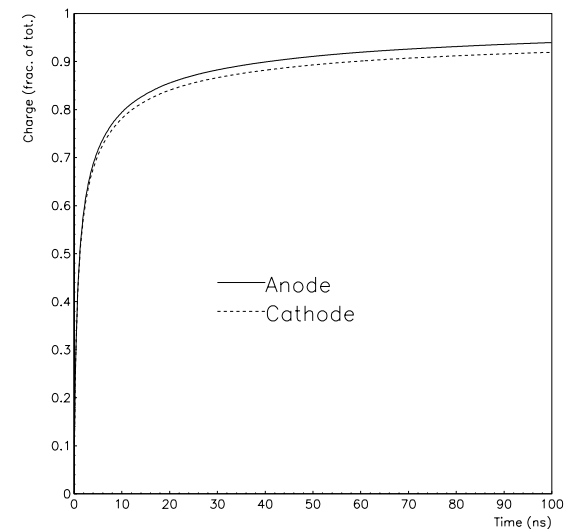
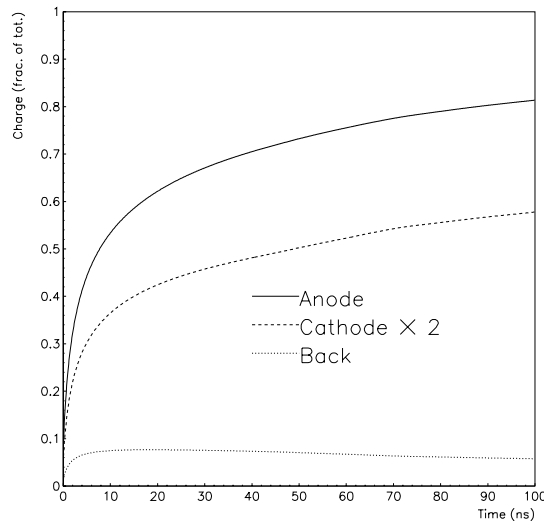
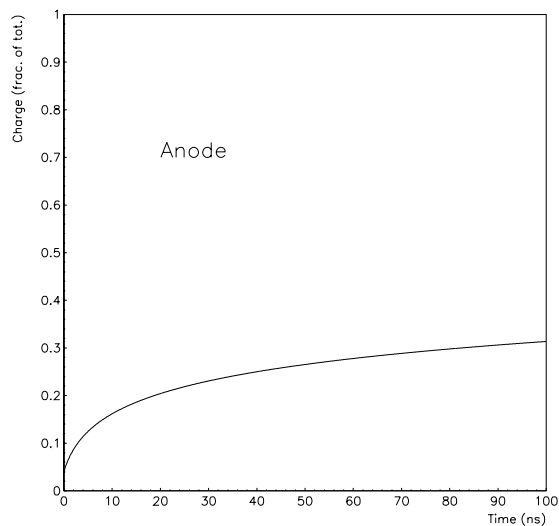
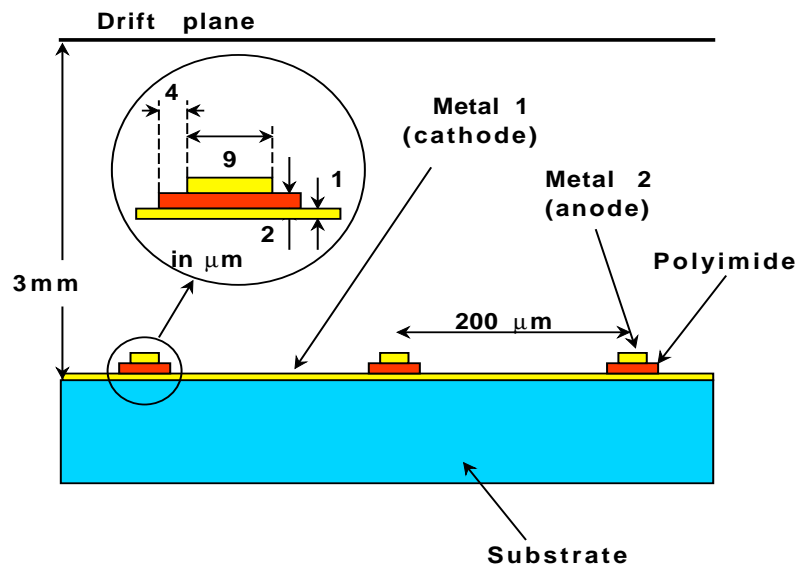
Detection Efficiency and Spatial Resolution



Robustness has been demonstrated on a few chambers in high intensity 400 MeV pion beam (10^4 Hz/mm²) over 161 hour sat PSI
Further tests at PSI on pre-production prototypes in 1999

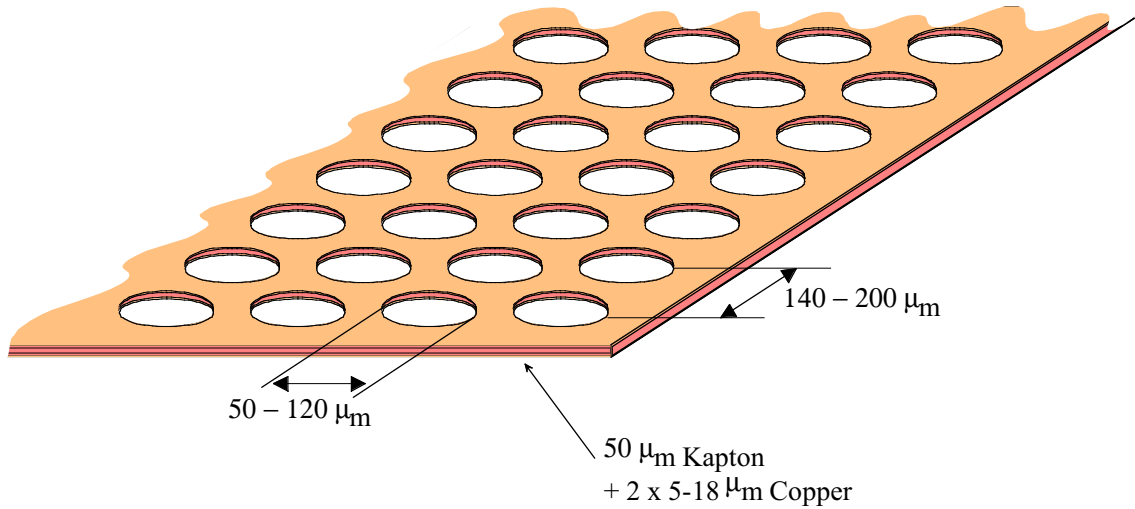


Micro-Gap Chambers

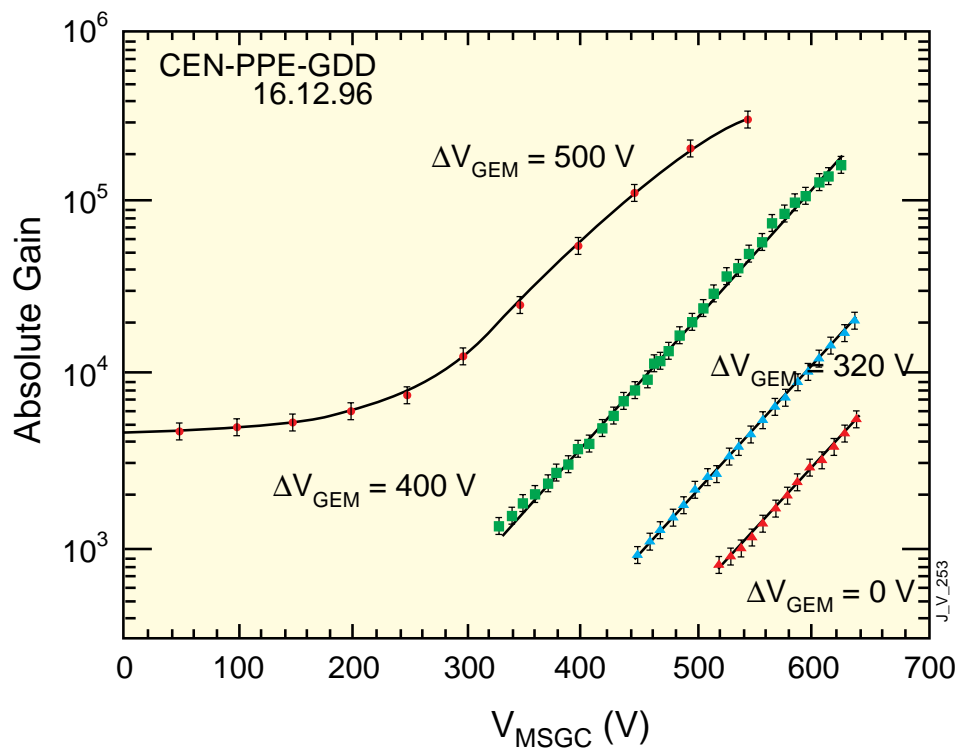
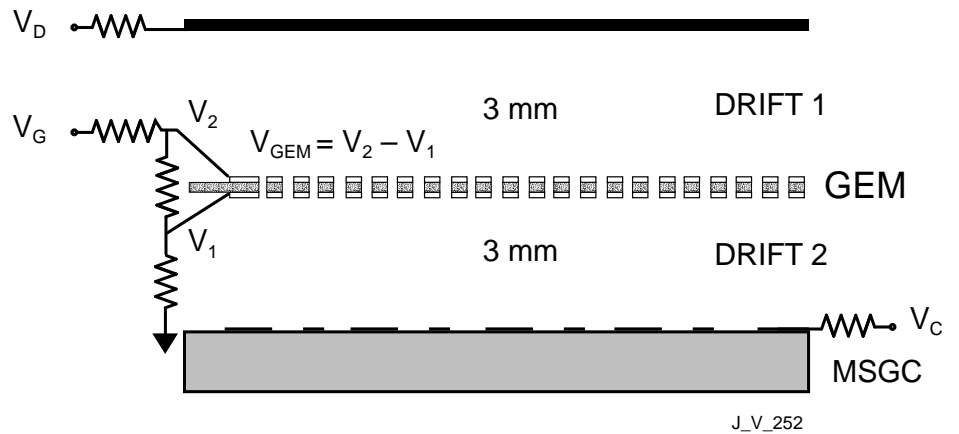


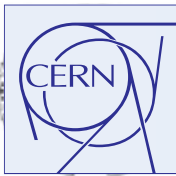
Time development of induced charge on the electrodes of a) MWPC, b) MSGC, c) MGC

R. Bouclier et al NIM A396 (1997)50.



GEM + MSGC





Silicon Detectors

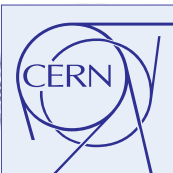
Characteristics of Silicon

- Basic information carriers are electron-hole (e-h) pairs
- Band-gap: $E_g = 1.2 \text{ eV}$
- Energy to create 1 e-h pair: $W = 3.6 \text{ eV}$ (NB $\approx 30\text{eV}$ in gas)
- High density (2.33 g/cm^3) - m.i.p. creates $\langle 30k \rangle$ e-h pairs in $300 \mu\text{m}$ thick silicon
- High mobility: $\mu_e = 1450$, $\mu_h = 450 \text{ cm}^2/\text{V.s}$ ($V_d = \mu E$) - fast signal collection ($\approx 10 \text{ ns}$ in $300 \mu\text{m}$ thick silicon)
- Both electrons and holes contribute to the signal

No charge multiplication - require v. good amplifiers

Performance degrades with radiation damage

Detectors produced using micro-electronic techniques
fine pitch ($\approx 50 \mu\text{m}$) but short strip lengths ($\approx 10 \text{ cm}$)



Signal in Silicon Detectors

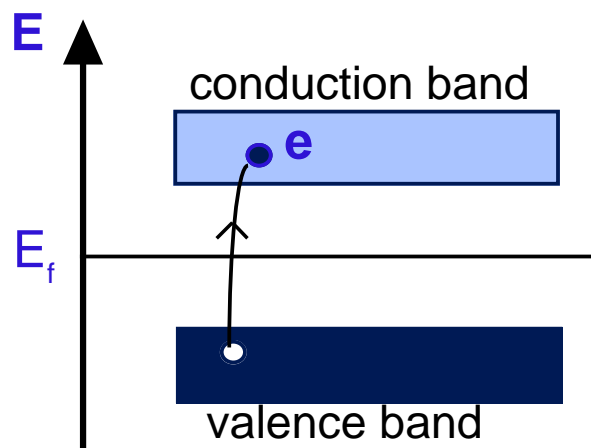
Energy levels in atoms become energy bands in regular assembly of atoms e.g. in crystals

Valence and conduction bands are formed in crystals due to the periodic lattice structure

Valence band: electrons bound to specific lattice site

Conduction band: electrons are free to migrate through crystal

At $T \neq 0$, valence electrons can get enough thermal energy to get into conduction band



In a pure intrinsic (undoped) material the electron density, n , and hole density, p , are equal

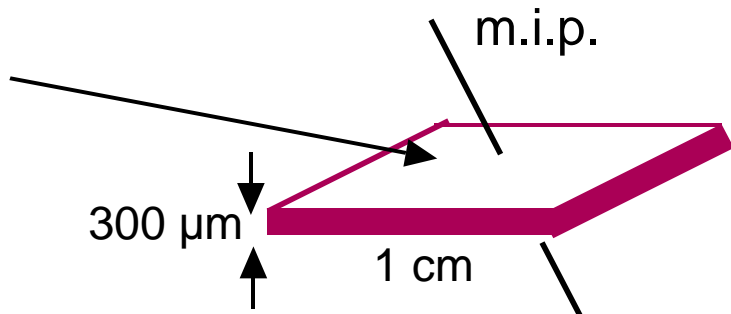
$$n_i = p_i$$

For Si: $n_i = 1.45 \cdot 10^{10} \text{ cm}^{-3}$

In this volume there are $4.5 \cdot 10^8$ free charge carriers, but only $\langle 32,000 \rangle$ e-h pairs are produced by a m.i.p.

Must reduce the number of free charge carriers i.e. **deplete the detector** of charge carriers

Most detectors make use of reverse biased p-n junction





n-type Semiconductor

Si sits in Group IV of the periodic table

i.e. it has 4 outer electrons and can form 4 covalent bonds

IF now a small concentration (few ppm) of pentavalent impurity is added (P, As)

- 1 valence electron left over after all covalent bonds formed
- It is very lightly bound and can easily be promoted to the conduction band without creating a corresponding hole

DONOR IMPURITY

- These electrons are not part of the regular lattice and can occupy a position in the normally forbidden gap (near top of gap)
- Thermal excitation is sufficient to ionize a large fraction of the donors (N_D)

$$n \approx N_D$$

Added concentration of electrons increases rate of e-h recombination, shifting equilibrium between electrons and holes. Concentration of holes decreased BUT

$$n p = n_i p_i$$

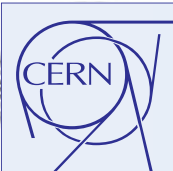
e.g. at room T, $n_i = p_i \approx 10^{10} \text{ cm}^{-3}$, if donor impurities $\approx 10^{17}$ atoms/cm³,

$n = 10^{17} \text{ cm}^{-3}$ and $p = 10^3 \text{ cm}^{-3}$

$$n \gg p$$

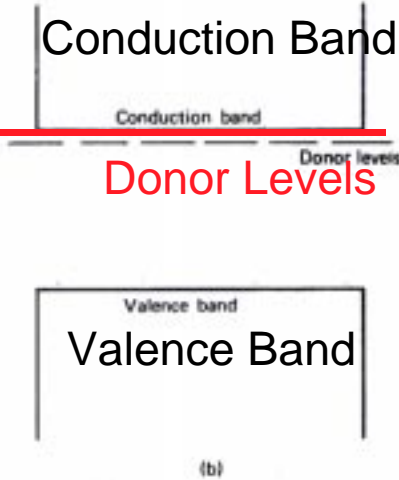
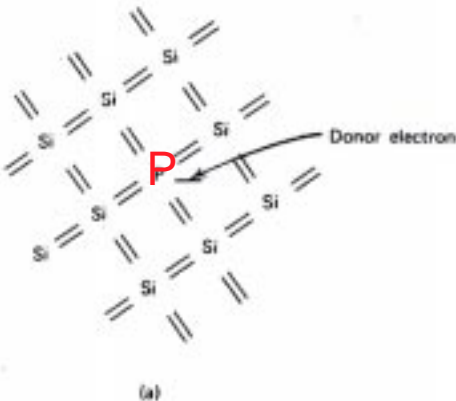
Charge neutrality is maintained by presence of ionized donor impurities which cannot migrate (fixed in the lattice)

electrons are majority carriers whereas holes are minority carriers

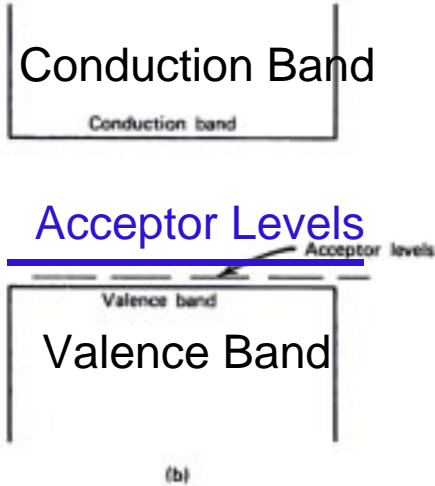
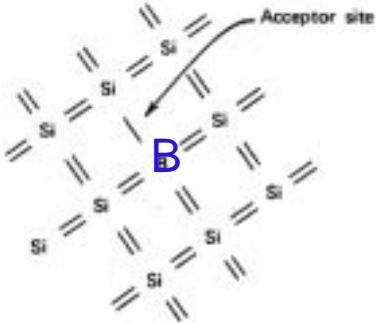


Donor & Acceptor Levels

n-type semiconductor
Donor site



p-type semiconductor
Acceptor site



$n p = n_i p_i$
e.g. at room T,
 $n_i = p_i \approx 10^{10} \text{ cm}^{-3}$,
if donor impurities
 $\approx 10^{17} \text{ atoms/cm}^3$,
i.e. $p = 10^3 \text{ cm}^{-3}$
 $n \gg p$

$p \gg n$



p-type Semiconductor

IF a small concentration (few ppm) of trivalent impurity is added (B)

- 1 fewer valence electron and 1 covalent bond left unsaturated
- vacancy represents a hole. Electrons can be captured to fill this vacancy
- electrons still bound to specific location but less firmly

ACCEPTOR IMPURITY

- These lie near bottom forbidden of gap - properties similar to sites occupied by normal valence electrons
- normal thermal excitation always assures electrons available to fill vacancies
- a large fraction of acceptor sites are filled

$$p \approx N_A \quad \text{with} \quad n p = n_i p_i \quad \text{and} \quad p \gg n$$

A measure of impurity level is electrical conductivity or its inverse resistivity

e.g. Si impurity conc. of 10^{13} atoms/cm³ \Rightarrow resistivity of 500 Ω .cm

Heavily Doped Material *

unusually high concentration of impurity labelled n⁺ or p⁺
has very high conductivity - often used in making electrical contact

*

Since there is very low minority carrier density - allows 'blocking' contacts

Ohmic contact - charges of either sign can flow freely

Steady state leakage currents using ohmic contacts are too high

Most appropriate type of blocking contacts are two sides of a p-n semiconductor junction



Properties of a p-n Junction

Bring into contact n- and p-type materials (done by doping a single crystal)

Begin with p-type crystal (original acceptor conc. N_A)

Assume surface left exposed to vapour of n-type impurity (left side becomes n-type material)

Density of electrons in n-type is much higher than in p-type

Net diffusion of conduction electrons into p-type material where they quickly recombine with holes

electrons moving out of n-type material leave immobile +ve charges and net -ve charge on p- side is established

Accumulated space charge creates electric field that diminishes tendency for further diffusion

Region over which charge imbalance exist is called the **depletion region** (conc. of e and h $\approx 100 /\text{cm}^3$!). In our case region will extend deeper into p- side than n- side

For electron-hole pairs created in depletion region, electrons swept toward n-type and holes toward p-type

Application of reverse bias (n- side made more +ve) extends the thin depletion region. The depletion depth is given by

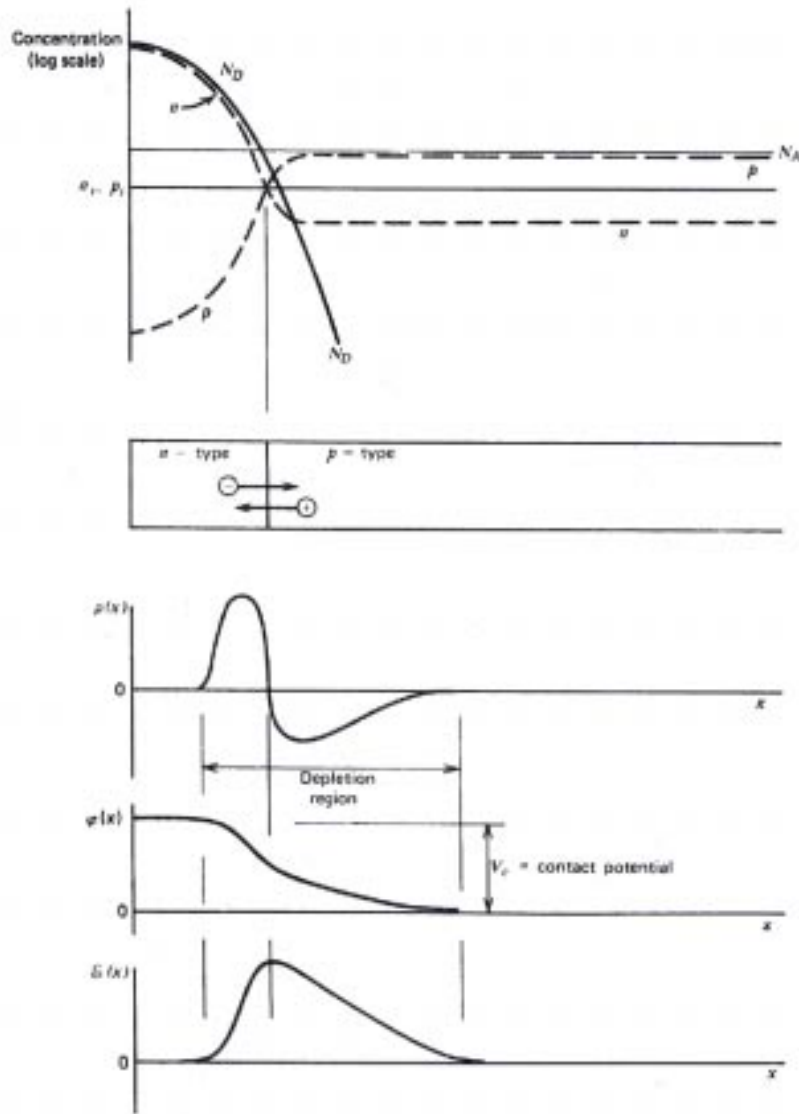
$$d \cong \sqrt{\frac{2\varepsilon V}{eN}}$$

$$PDG: d \approx 0.5 (0.3) \mu\text{m} \times \sqrt{\rho V} \quad \text{for } n\text{-type } (p\text{-type})$$

N - lower dopant conc. , ρ - resistivity (typically 1-10 k Ω .cm)

$d \approx 300 \mu\text{m}$ for $\rho=5 \text{ k}\Omega$.cm and Bias Voltage $\approx 70\text{V}$

Concentration Profiles



- In depletion region
conc. of e and h $\approx 100 / \text{cm}^3$!.
- Reverse bias (n- side made more +ve)
extends the thin depletion region.

$$d \cong \sqrt{\frac{2\epsilon V}{eN}}$$

PDG: $d \approx 0.5 (0.3) \mu\text{m} \times \sqrt{\rho V}$ for n-type (p-type)

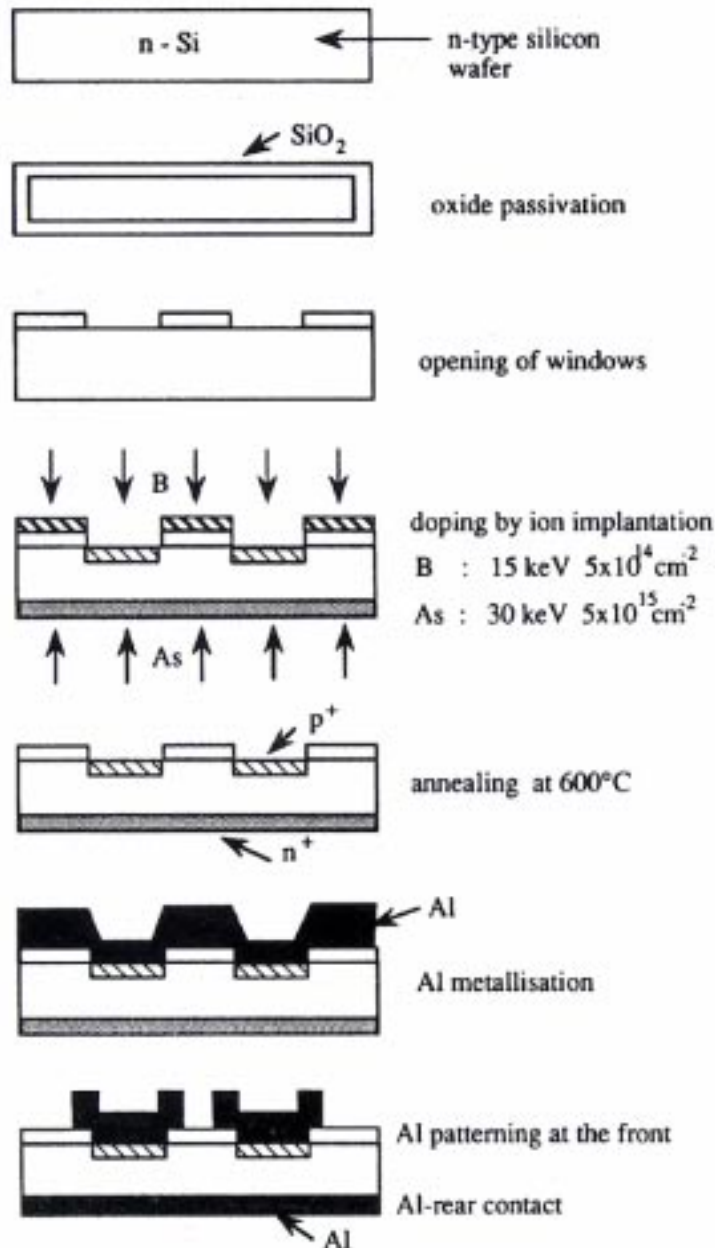
N - lower dopant conc. , ρ - resistivity
(typically 1-10 k Ω .cm)

$d \approx 300 \mu\text{m}$ for $\rho=5 \text{ k}\Omega$.cm and

Bias Voltage $\approx 70\text{V}$

The assumed concentration profiles for the n-p junction shown at the top are explained in the text. The effects of carrier diffusion across the junction give rise to the illustrated profiles for space charge $\rho(x)$, electric potential $\phi(x)$, and electric field $\mathcal{E}(x)$.

Fabrication Of Si Detectors



clean and polish wafer

oxidize at 1000°C, passivate

apply photosensitive polymer and bake
expose to UV light thru mask, develop

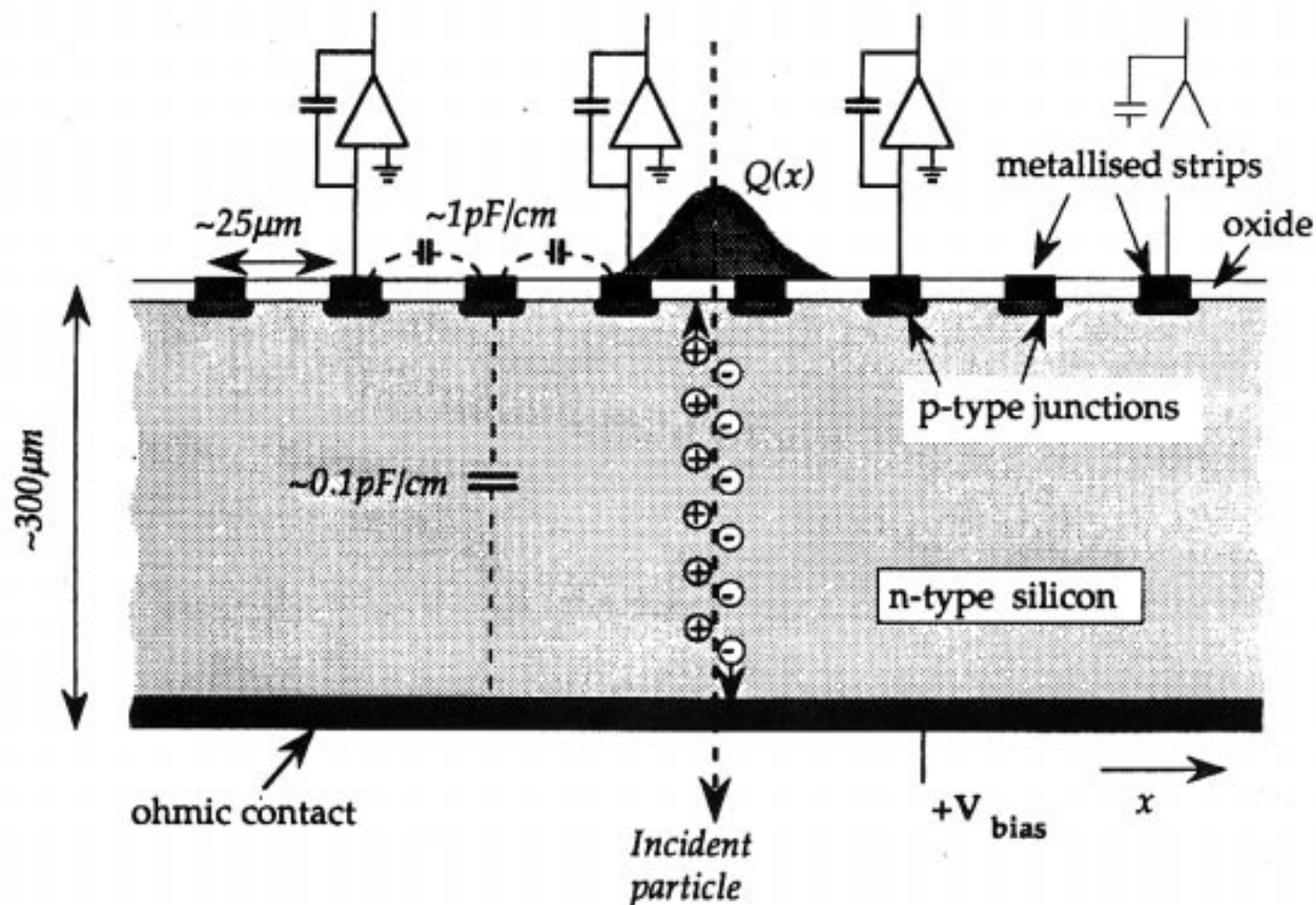
form diode junctions by implantation/diffusion

anneal - implanted ions take-up lattice positions

aluminize surfaces

final photolithographic steps to pattern metal
for diode contacts

Si Microstrip Detectors



Schematic cross-section through a silicon microstrip detector. Diffusion distributes charge over multiple strips and capacitive charge division between readout amplifiers allows position interpolation.



Radiation Damage in Silicon

Bulk damage effects more important than surface damage

High energy hadronic particles displace Si atoms from their lattice positions (only ≈ 15 eV is required)

Simplest defects

- vacancies where Si atom is absent from its site
- Si atom occupies a position intermediate between atomic sites

Disruption of the symmetry causes formation of unwanted energy levels in the forbidden gap

increased leakage current $\frac{\Delta I}{V} = \alpha \phi$

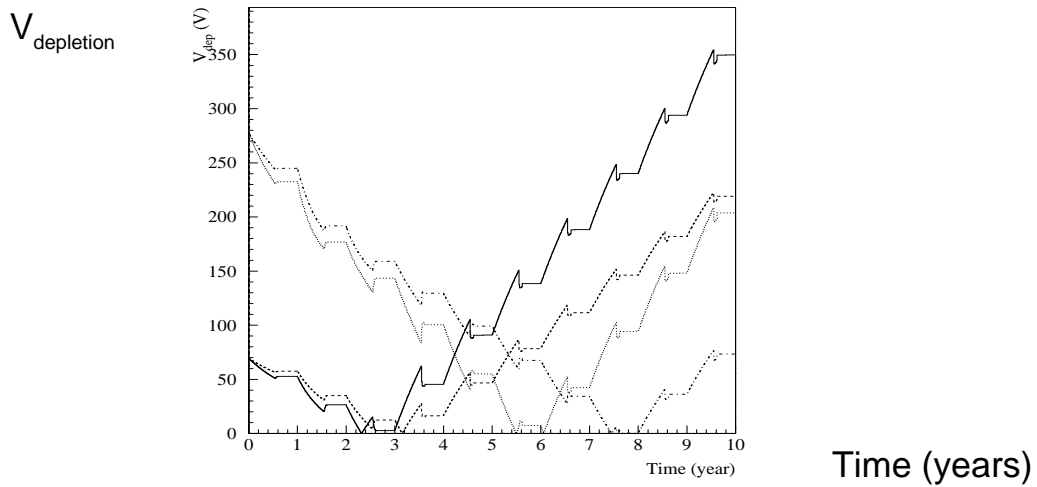
where $\alpha \approx 2 \cdot 10^{-17}$ A/cm for minimum ionizing protons and pions after long-term annealing and
 V is the volume (in cm^3), ϕ is fluence in particles/ cm^2

dopant density changes during and after irradiation

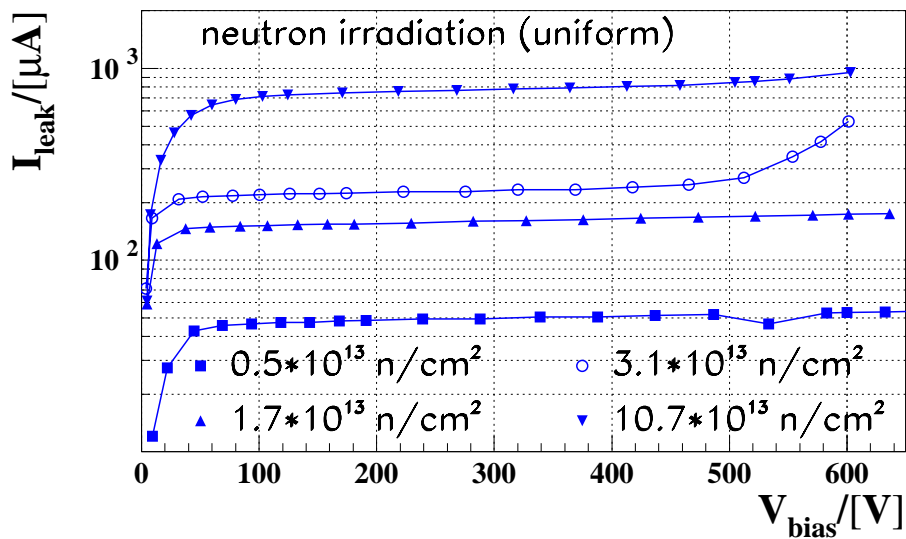
- effect is poorly understood
- n-type substrate eventually becomes p-type, whatever the initial type or resistivity
- dopant changes continue after irradiation has stopped BUT can be arrested if detectors kept below 0 °C.
- with increasing particle fluence the depletion voltage increases

Manufacturing of Si detectors has improved substantially and high voltage operation (≥ 500 V) is nowadays possible.

Evolution of voltage for full depletion

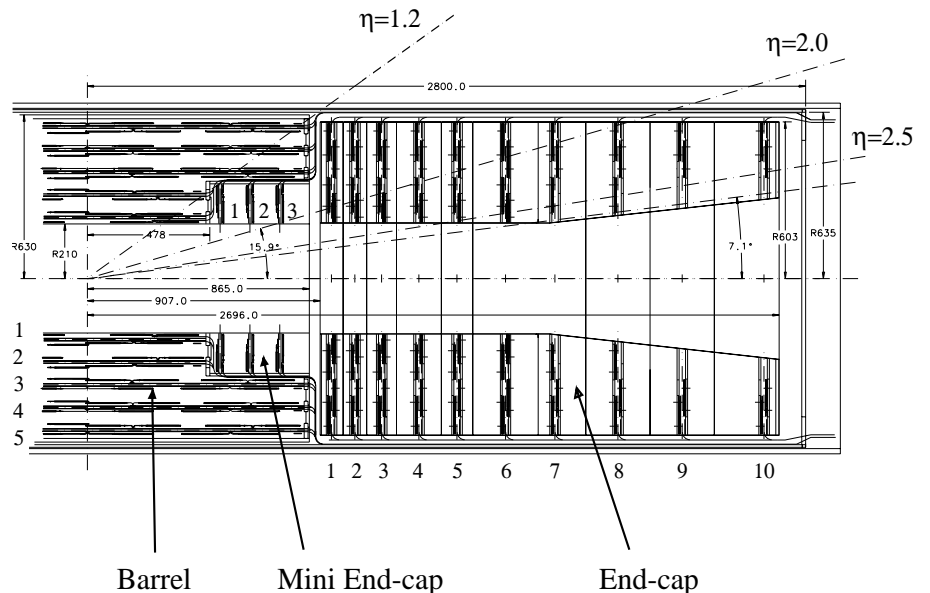


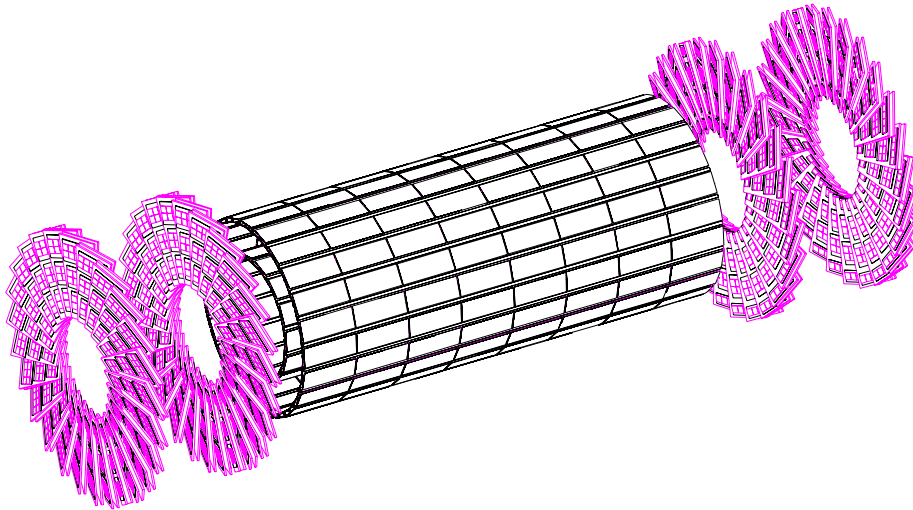
Results from neutron irradiation



e.g. CMS Silicon Tracker

Area 70 m²
 # ch 5.2 M
 r- ϕ pitch 62/83/125 μm
 stereo 125/250 μm

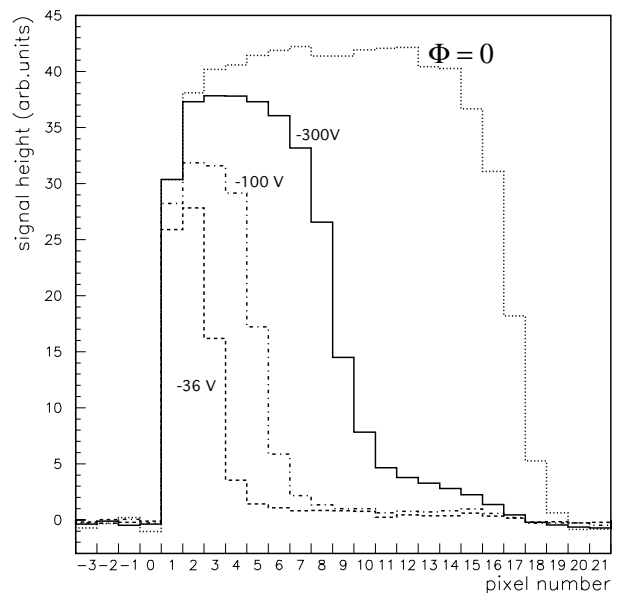
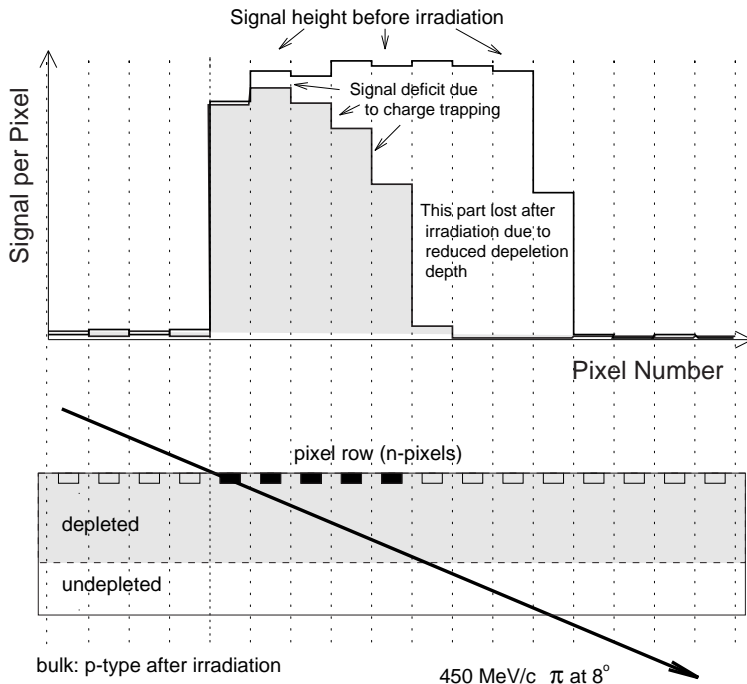




Characteristics of CMS pixel detectors

- Size: 150 μm x 150 μm
- n on n Si: large Lorentz angle (34°) allowing charge sharing
- 5 °C: low leakage current, arrest reverse annealing

Irradiation of Si Pixel Detectors



Depth profiles of charge collected from a pixel array irradiated with 6.10^{14} pion/cm²



Electronics

- Electronics Noise
- Generic LHC Readout System
- Electronics for LHC Detectors
- Electronics of Sub-detectors
- CMS Tracker Electronics
- CMS Tracker Front-end
- Analog Optical Links



Electronics Noise

Amplifier Noise

Noise is any unwanted signal that obscures the signal.

Noise degrades accuracy of measurement

Intrinsic Noise : noise generated in the detector or electronics and cannot be eliminated, though possibly reduced

Extrinsic Noise : noise due to pickup from external sources or unwanted feedback (e.g. ground loops, power supply fluctuations, etc.)

Intrinsic Noise

- Thermal noise (Johnson, Nyquist) - **series noise**

any resistor, R , will develop a voltage across its ends whose average value is zero but r.m.s. is

$$\langle v^2 \rangle = 4kTR.\Delta f$$

- Shot noise - **parallel noise**
fluctuation in charge carriers

$$\langle i_n^2 \rangle = 2eI.\Delta f$$

The equivalent noise charge (ENC) is given by

$$ENC^2 = \frac{4kTR_s(C_d + C_{in})^2}{\tau} I_s + I_n \tau I_p$$

where C_d is detector capacitance

C_{in} is input capacitance of amplifier

I_n is leakage current

τ is shaping time

I_s, I_p are series and parallel noise integral (≈ 1 for $(RC)^2$ shaping)

e.g. for $\tau=50$ ns, and a leakage current of 1 μ A, $ENC \approx 800$ e's



Electronics for LHC Detectors

Main components (systems) of Electronics

front-end, digital processing,
data transmission
power supplies, services,

What is different about electronics for LHC cf. e.g. LEP

high speed signal processing
signal pileup
high radiation levels
larger no. of channels (large data volumes)
new technologies

e.g. Challenge for Inner Tracker

- signals are small and fast response must be preserved
preamplifiers must be mounted on detectors themselves
- must hold data in pipeline memories awaiting Level-1 decision
- it is not feasible to transfer data off the detector at a rate of 40 million events/s for millions of channels
pipeline memories must be located on the detectors
how are the signals taken out ?
how are the electronics mounted on detectors ?
- several millions of channels will dissipate a considerable amount of heat (\approx several mW/ch)
how is the cooling of electronics accomplished ?

⇒ v. difficult engineering and systems challenge

accomplish above whilst keeping the amount of material to a minimum



Electronics of Sub-detectors

Tracking

large channel count (10's M)
limited energy precision
limited dynamic range (<8-bit)

low power (few mW/ch)
high radiation levels

Calorimetry

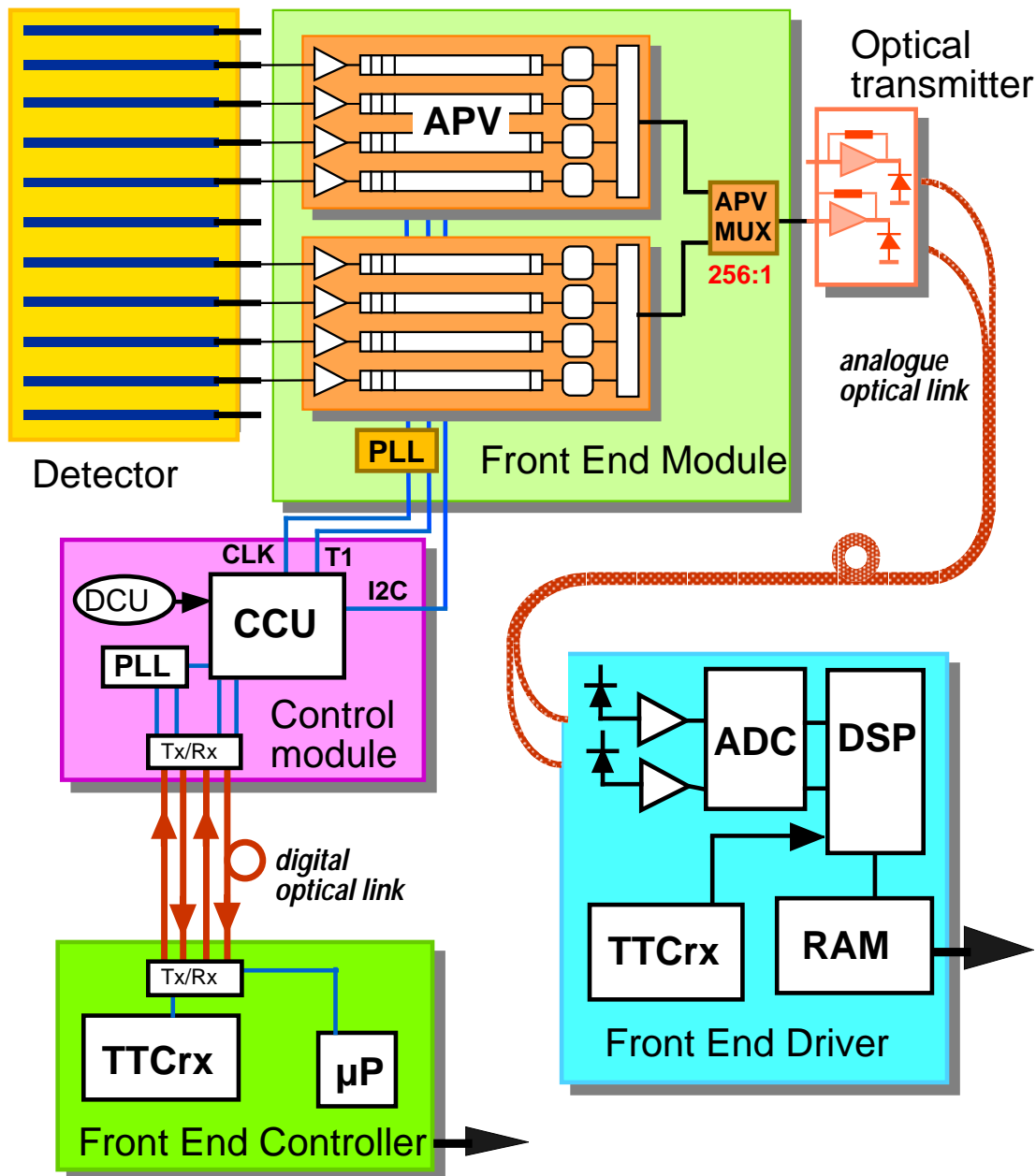
medium channel count (100's k)
high energy precision (12-bit)
large dynamic range (17-bit)
v. good linearity
v. good stability in time

power constraints
medium radiation levels

Muon System

distributed over large area

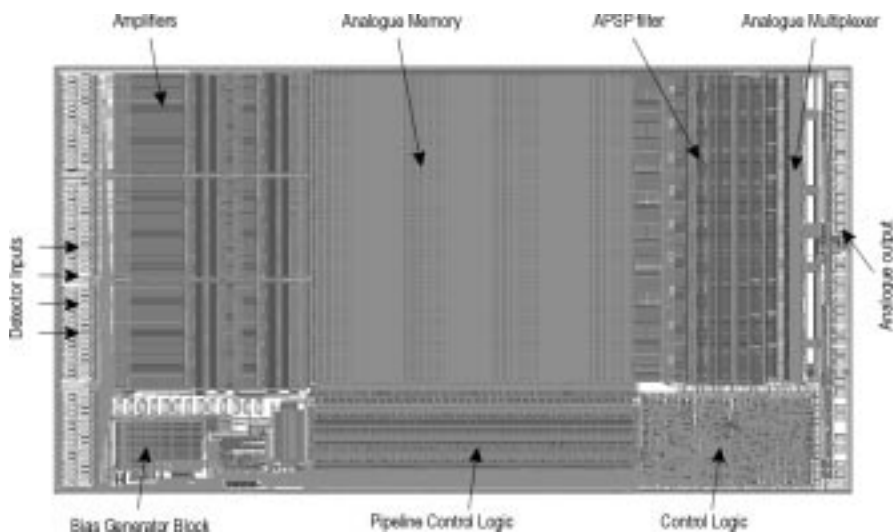
low radiation levels



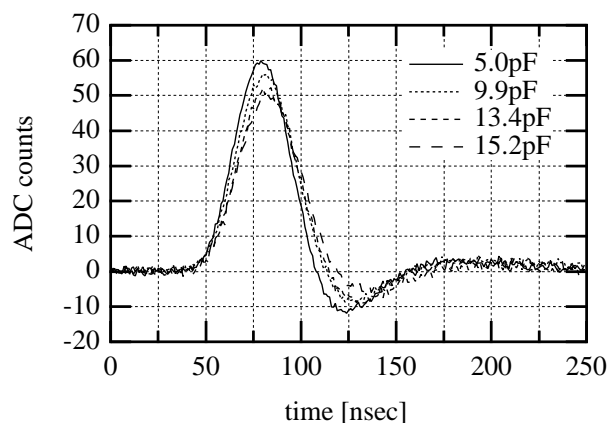
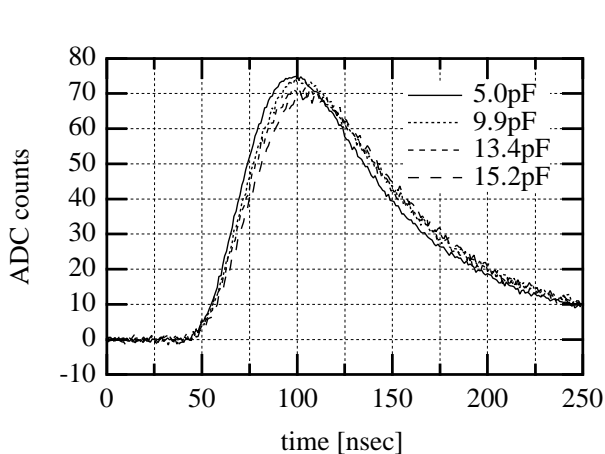
Each microstrip is read out by a charge sensitive amplifier with $\tau = 50$ ns.
 The o/p voltage is sampled at the beam crossing rate of 40 MHz.
 Samples are stored in analog pipeline for up to Level-1 latency (3.2 μ s)
 Following a trigger form a weighted sum of 3 samples in analog circuit
 This confines signal to single bx and gives pulse height
 Buffered pulse height data multiplexed out on optical fibres
 Output of laser modulated by the pulse height for each strip

Layout of APV6

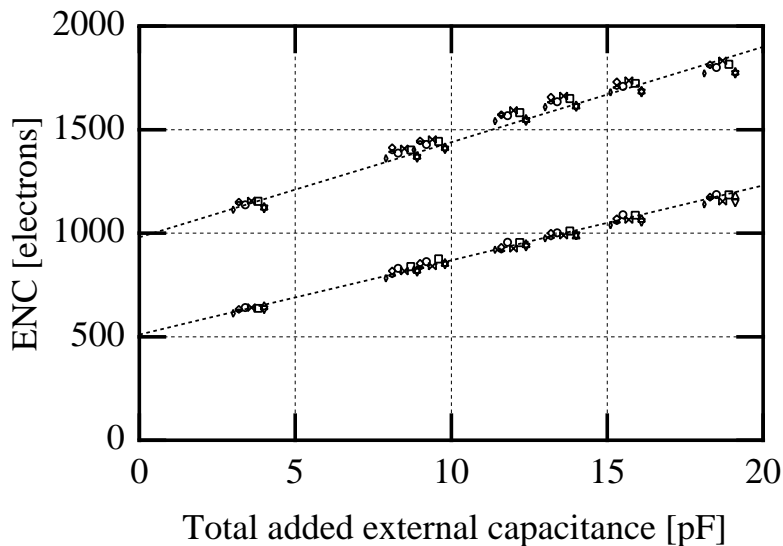
Size 6.4 x 12 mm²



Pulse shape in peak and deconvolution mode of APV6

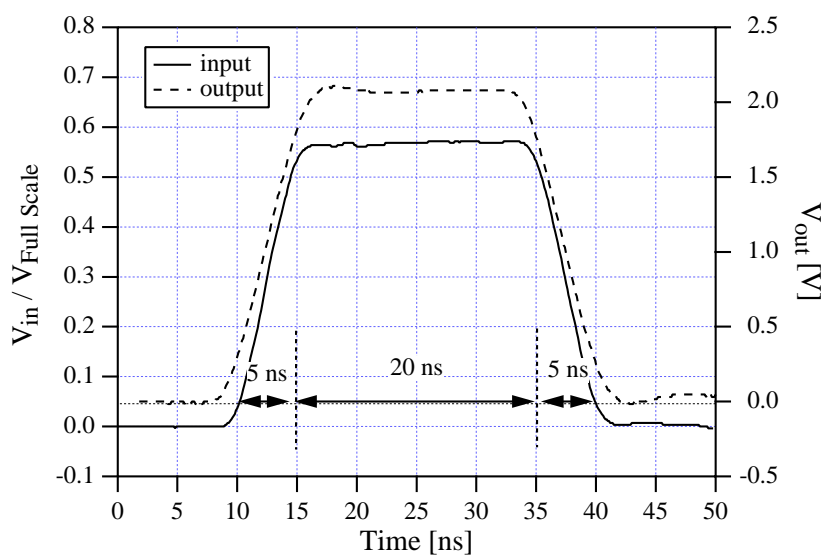
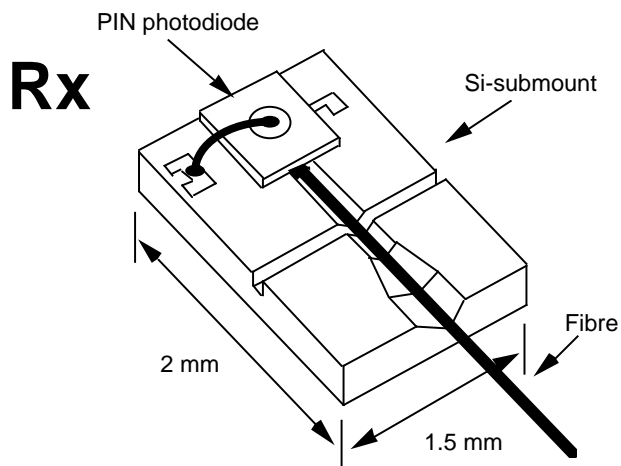
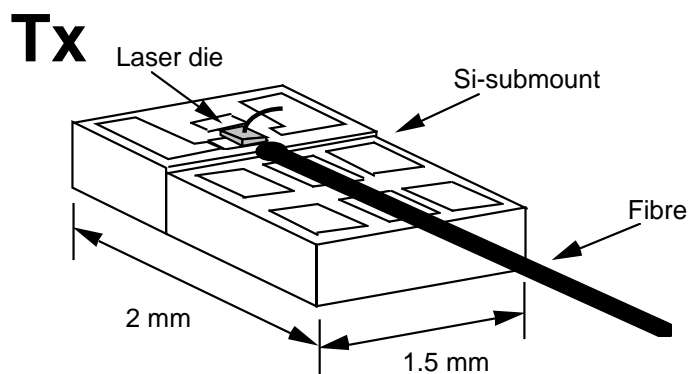


Si μ -strips
Overall Noise in e-
 APV6 1500
 $i_l=2 \mu\text{A}$ 500
 Opt. Lnk 750
Total ≈ 1750
 cf mip signal 25 k e-



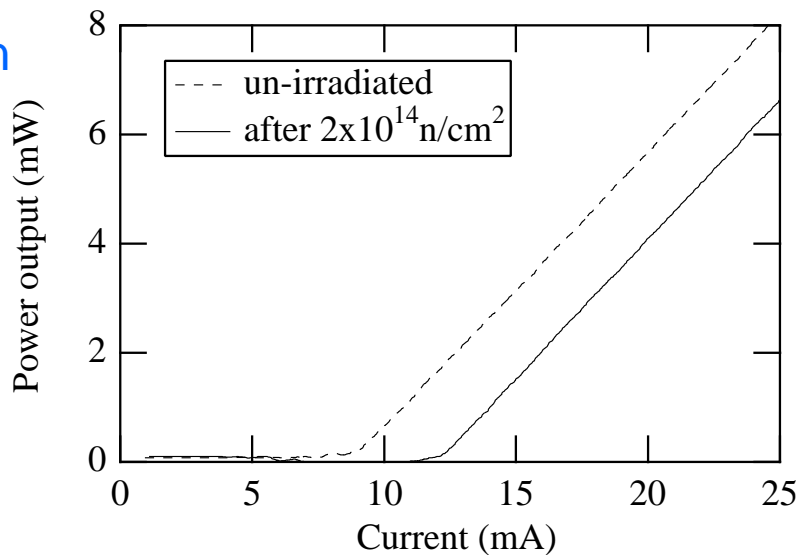
Analog Optical Links

Edge emitting 1.3 μm InGaAsP laser diodes



Pulse Response

Pre- and Post-Irradiation
OK to $\gg 10^{14}$ n/cm²





Features of Calorimetry

1. Calorimeters can measure energies of neutral and charged particles, jets and deduce the presence of neutrinos.

2. The relative energy resolution improves with energy as

$$\sigma/E \propto 1/\sqrt{E}$$

This contrasts with momentum measurement of charged particles where the relative transverse momentum resolution $dp_t/p_t \propto p_t$.

3. The longitudinal depth required to contain the cascades only increases logarithmically whereas for magnetic spectrometers the size increases as \sqrt{p} for constant dp_t/p_t .

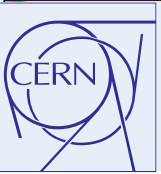
4. The cascade develops differently, longitudinally and laterally, for e/γ , hadrons and muons. This can be exploited for particle identification.

5. The pattern of energy deposit in a calorimeter with good lateral and longitudinal segmentation allows fast, efficient and very selective triggering on e/γ , jets and E_T^{miss} .

6. Good simulation codes exist to design of calorimeters (EGS4 for e.m. and FLUKA, GHEISHA, GCALOR for hadronic cascades).

7. Large precision electromagnetic calorimeter systems are operating well (CLEO, KTeV, NA48), will soon be commissioned (BaBar, Belle) or are under construction (CMS, ATLAS)

8. Calorimeter systems have played an important role in recent discoveries e.g. W , Z in UA1/UA2, top quark in CDF/D0 and will play a similarly crucial role in the next generation of experiments ATLAS/CMS.



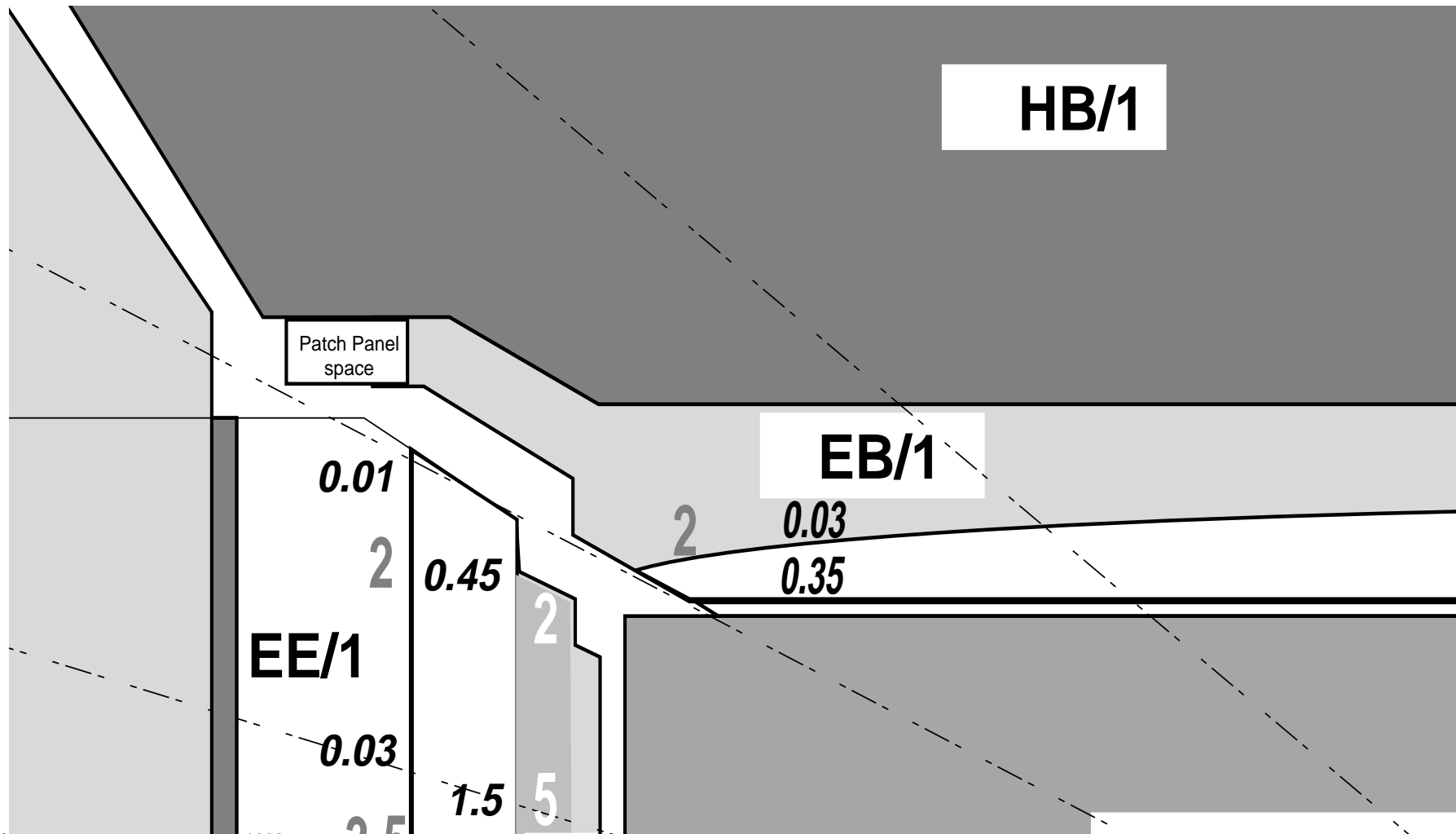
Radiation Levels in LHC calorimeters

Dose and neutron fluence in and around the crystal calorimeter of CMS.

Bold Italics : dose in kGy (10^5 rads) at shower maximum and rear of calorimeter

Plain : neutron fluence in 10^{13} n/cm²

Numbers corresponds to first ten years of LHC operation





Crystal Calorimeters

- Inorganic Scintillators
- Radiation Damage in Crystals
- CMS ECAL
- PbWO₄ Energy Resolution
- Response from 280 GeV electrons
- Si Avalanche Photodiodes
- Si Avalanche Photodiodes
- CMS PbWO₄ Crystals Assembly



Inorganic Scintillators

Desirable Properties

- high scintillation efficiency (energy → light)
- conversion (energy → light) linear
- medium transparent to its own emitted light
- short luminescence decay time
- $n \approx 1.5$ for efficient coupling to photosensors
- radiation hard for LHC operation

No material simultaneously meets all these criteria

Inorganic: best light output and linearity (e.g. NaI)

Organic (eg. plastic scint.) faster (ns), smaller light yield ($\approx 1\gamma/100$ eV), saturation

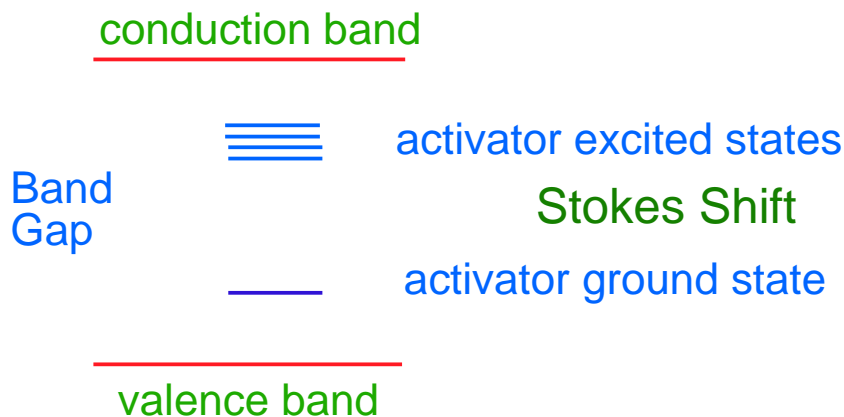
Fluorescence - prompt emission of visible radiation

Phosphorescence - (slower) emission of longer wavelength

Inorganic Scintillators

Valence band - electrons bound at lattice sites

conduction band - electrons free to move throughout the crystal



- Pure crystal - insufficient scintillation efficiency
- Add small amount of impurities (called activators) to increase prob. of visible γ emission
- Create energy states within forbidden gap through which an electron, excited to conduction band, can de-excite



Inorganic Scintillators

- a charged particle creates large no. of e-h pairs:
electrons elevated to conduction band
- +ve holes quickly drift to an activator and ionize it
- e migrates freely in crystal until it encounters an ionised activator,
- e drops into impurity site creating activator energy levels
- typically $T_{1/2}$ of activator sites ≈ 100 ns

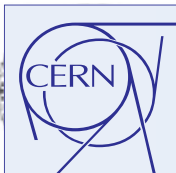
Competing processes

- excited to state where transition to ground state is forbidden
- additional energy required to raise to a higher lying state from which de-excitation can take place
- one source of energy is thermal
 \Rightarrow **slow component or afterglow**
- radiationless transition (quenching processes)

- in wide category of materials, energy reqd. to create e-h pair
 $W \approx 3 E_g$

e.g in NaI, $W \approx 20$ eV, NaI(Tl) : $N_\gamma \approx 40,000$ γ /MeV of 3 eV
**consequence of luminescence through activator sites
crystal is transparent to its own scintillation light**

in pure crystal - emission and absorption spectra overlap -
substantial self absorption \Rightarrow **need a Stokes shift**

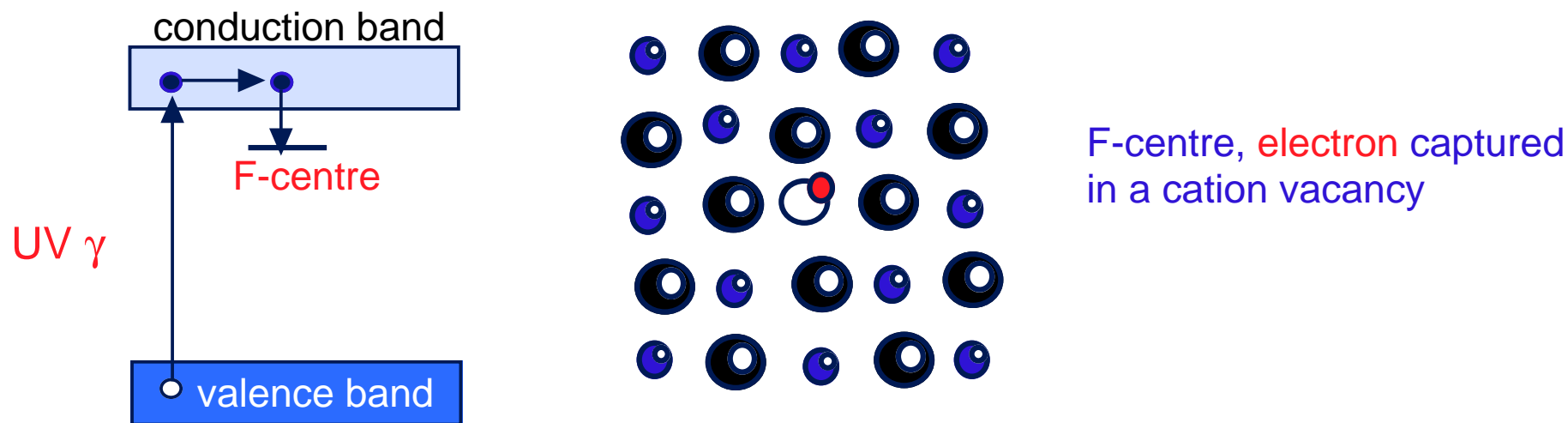


Radiation Damage in Crystals

All known crystals suffer from radiation damage

- absorption bands caused by colour centre formation or impurities
- light attenuation length is affected - loss of collected light (change of calibration)
- scintillation mechanism is not affected

Colour centre - crystal defect that absorbs visible (or near UV) light
most simple colour centre known as an F-centre (*farbe*-colour in German)



To improve radiation tolerance of PbWO_4 crystals

Decrease concentration of defects
stoichiometry, annealing

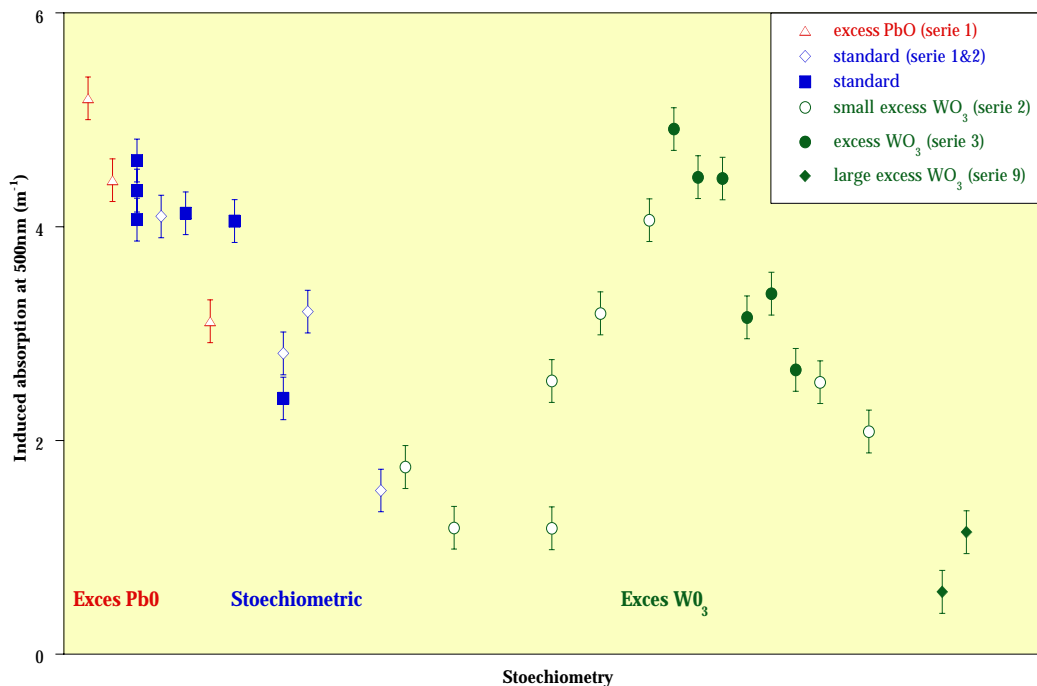
Compensation of remaining defects

control purity of raw material, specific doping-pentavalent of W site, trivalent on Pb site



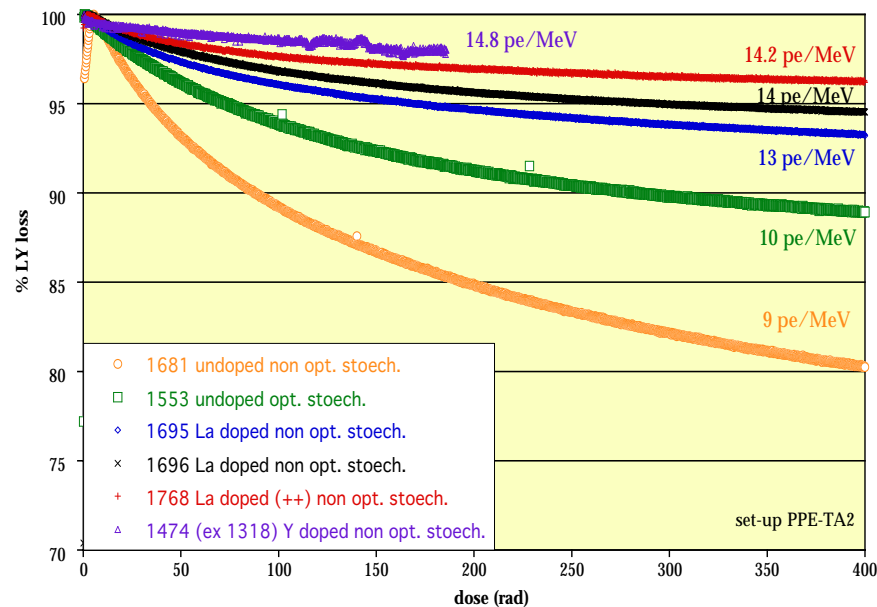
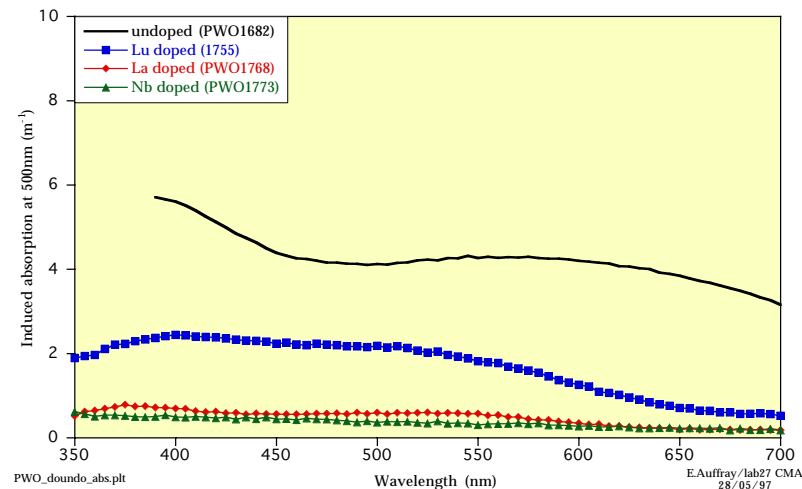
Radiation Tolerance of PbWO_4 Crystals

Specific Doping



PWO_pind500/stoech.corplt6

E.Auffray_lab27 CMA 28/03/97



PWO_Lowdose_undo.do.plt2

E.Auffray/CMS_Ecal 24/05/97

Low Dose Rate Front Irradiation v/s Specific Doping



Radiation Damage in Crystals

All known crystals suffer from radiation damage

- absorption bands caused by colour centre formation or impurities
- light attenuation length is affected - loss of collected light (change of calibration)
- scintillation mechanism is not affected
- dependence on dose rate

Colour centre - crystal defect that absorbs visible (or near UV) light
high concentration of blue colour centres makes crystals yellowish
crystal that is coloured after irradiation has poor radiation tolerance

most simple colour centre known as an F-centre (farbe-colour in German)

electron in an anion vacancy

E.g. R&D for improved radiation tolerance of PbWO_4 crystals

Decrease concentration of defects

stoichiometry

annealing

Compensation of remaining defects

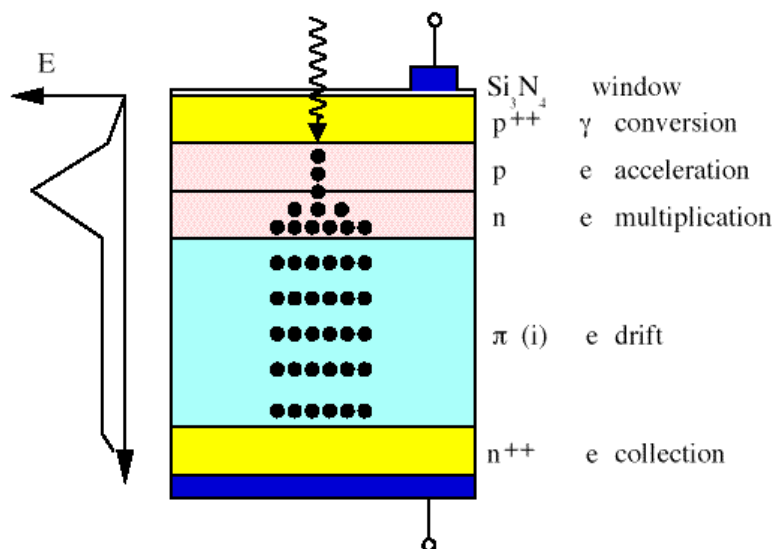
control purity of raw material

specific doping, pentavalent of W site, trivalent on Pb site

Si Avalanche Photodiodes

Light output from PbWO_4 crystal is low, require a photodetector with amplification. Calorimeter will operate in 4T field !
 Solution is to use Si avalanche photodiodes.

Working Principle



- Consider a crystal with a light yield of N_γ photons/MeV
- For deposited energy E , $N_\gamma \cdot E$ photons hit APD
- For q.e. Q (can easily be 85%) $N_{pe} = N_\gamma EQ$
- photostatistics fluctuation $N_{pe} \pm \sqrt{N_{pe}}$
- If there is NO fluctuation in the gain, no. of electrons collected $M \cdot N_{pe} \pm M \sqrt{N_{pe}}$

but multiplication process in APD is noisy i.e. gain has a fluctuation, σ_M

$$M \pm \sigma_M$$

because of this fluctuation no. of electrons collected is

$$M \cdot N_{pe} \pm \sqrt{M^2 + \sigma_M^2} \sqrt{N_{pe}}$$

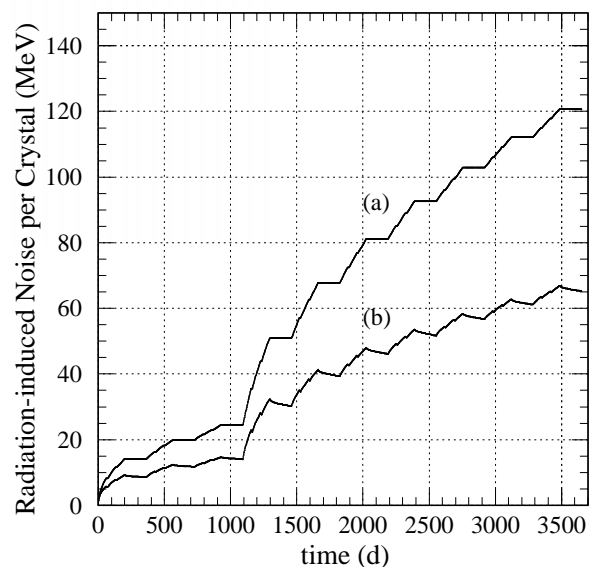
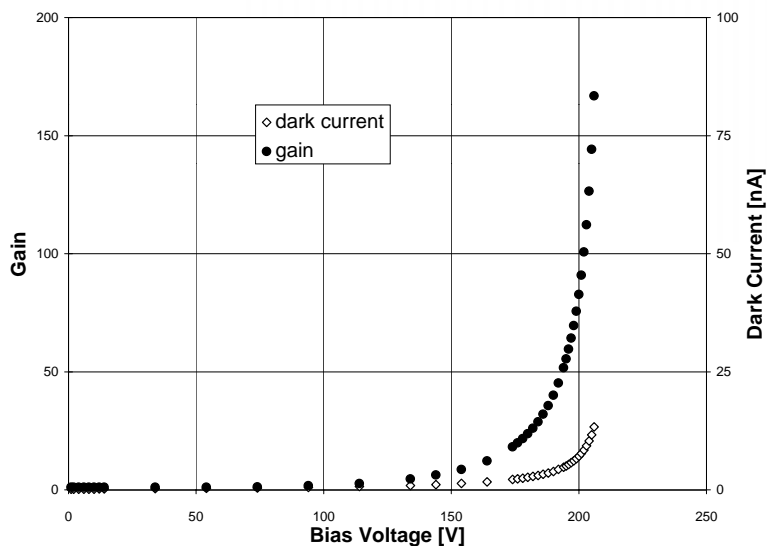
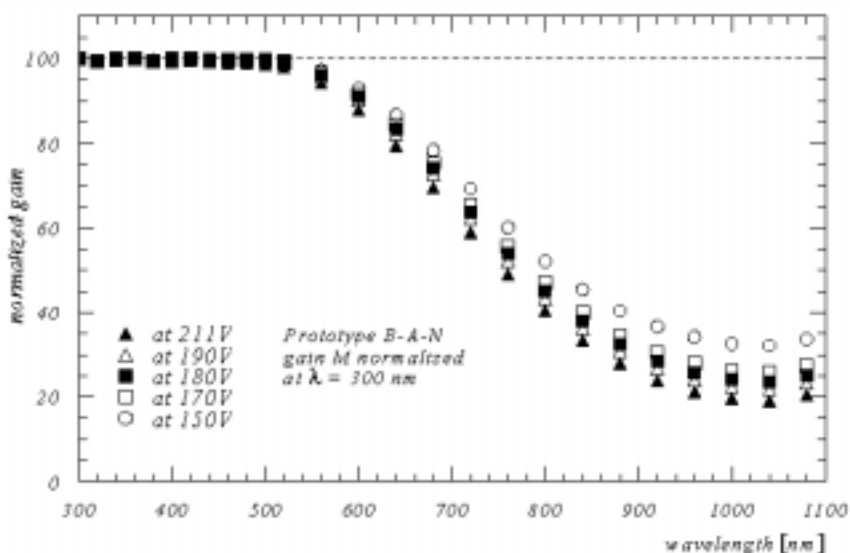
so photostatistical contribution to energy resolution becomes

$$\frac{\sigma_{pe}(E)}{E} = \frac{1}{\sqrt{N_\gamma EQ}} \sqrt{\frac{M^2 + \sigma_M^2}{M^2}} = \frac{1}{\sqrt{N_\gamma EQ}} \sqrt{F}$$



Si Avalanche Photodiodes

Parameter	Goal	Hamamatsu	EG&G
Active area	> 50 mm ²	25 mm ²	25 mm ²
Quantum efficiency @ 450 nm	> 80%	80%	75%
Capacity	<100 pF	100 pF	25 pF
Serial resistance	< 1Ω	5 Ω	5 Ω
Excess noise factor	< 2	2.0	2.3
Operating bias voltage	< 500 V	400–420 V	350–450 V
Initial dark current	< 100 nA	2–3 nA	30–70 nA
dM/dV × 1/M @ M = 50	< 2%	5%	0.6%
kdM/dTl × 1/M @ M = 50	< -2%	-2.3%	-2.7%
Passivation layer	Si ₃ N ₄	Si ₃ N ₄	Si ₃ N ₄
Packaging	non-magnetic	non-magnetic	non-magnetic





Noble Liquids Calorimetry

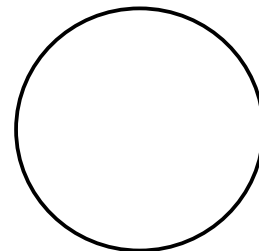
- Signal Generation in Noble Liquids
- Properties of Noble Liquids
- Charge Collection in Ionisation Chambers
- ATLAS LAr e.m. Calorimeter
- Performance of ATLAS ECAL



Signal Generation in Noble Liquids

- The number of ion pairs/100 eV \approx that in gases.
- Not all electrons in liquids become "free". The motion of the electrons in liquids is governed by Coulomb attraction between the ions and by diffusion. A certain number of electrons will recombine with positive ions.
- Consider an e-ion pair. Assume r_c is the distance at which the Coulomb potential energy equals the mean thermal energy. Then

$$kT = \frac{e^2}{4\pi\epsilon_0\epsilon_r} \frac{1}{r_c}$$



e.g. $r_c \sim 1300\text{\AA}$ in liquid argon (LAr).

- An electron will escape recombination if $\rho > r_c$ where ρ is the mean distance at which the electron thermalizes.
- In absence of an external electric field the escape probability is proportional to $\exp(-r_c/r)$.
- If G_{fi} is defined to be the number of "free" electrons per 100 eV of deposited energy, and W as the mean energy (in eV) required to create one electron-ion pair, then for low electric fields and low ionization density

$$G_{fi} = \frac{100}{W} e^{-r_c/r} (1 + \alpha F) \quad \text{Onsager}$$

where $\alpha = e^3 / 8\pi\epsilon_0\epsilon k^2 T^2$, ϵ is the dielectric constant, F is the electric field strength and T is the absolute temperature.

Kramers - highly ionizing particles generate a dense column of electron-ion pairs and volume (or columnar) recombination has to be considered.



Properties of Noble Liquids

Desirable properties of liquids used in ionization chambers

- high free electron (G_{fi}) for large collected charge
- a high electron mobility (μ) leading to a high drift velocity and hence a rapid charge collection.
- a high degree of purity. The presence of electron scavenging impurities leads to the reduction of electron 'lifetime' and consequently a reduction in the collected charge.

Properties of Noble Liquids	LAr	LKr	LXe
Z/A	18/40	36/84	58/131
Density g/cm ³	1.39	2.45	3.06
dE/dx <mip> MeV/cm	2.11	3.45	3.89
Critical energy MeV	41.7	21.5	14.5
Radiation Length cm	14.3	4.76	2.77
Moliere Radius* cm	7.3	4.7	4.1
W value eV	23.3	20.5	15.
Drift vel (10kV/cm) cm/ μ s	0.5	0.5	0.3
Dielectric Constant	1.51	1.66	1.95
Triple Point Temp K	84	116	161



Charge Collection in Ionisation Chambers

- Ionisation chambers are essentially a pair of parallel conducting plates a few mm apart, at a PD in an insulating liquid (LAr, TMP etc.)

- Consider what happens to a single ion pair (single carrier devices, +ve ions play no role in signal, ion mobility is much lower)

- Net charge induced on anode is $Q = -e \frac{(d-x)}{d}$

- Assume electron drifts with velocity v , and time of drift to cross the full gap is t_d

$$i(t) = \frac{dQ}{dt} = -e \frac{v}{d} = -\frac{e}{t_d}$$

- If ionisation is uniformly distributed, then fraction of electrons still moving after time t is $(t_d-t)/t_d$ for $t_d < t$.

$$\therefore i(t) = -Q_0 \frac{v}{d} \left(1 - \frac{t}{t_d}\right)$$

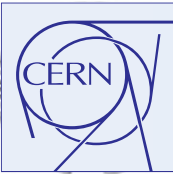
where $Q_0 = Ne$ and current is max. at $t \approx 0$

$$q(t) = \int_0^t i(t) dt = -Q_0 \left(\frac{t}{t_d} - \frac{t^2}{2t_d^2} \right) \quad t < t_d$$

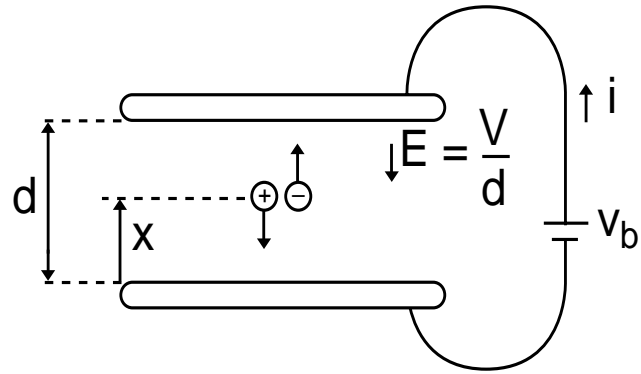
- Total charge collected ($t \geq t_d$) is $Q_c = Q_0/2$ (2 because of uniform ionisation)

- If during drift, electrons are trapped by impurities, induced current will be reduced. If electron 'lifetime' is τ

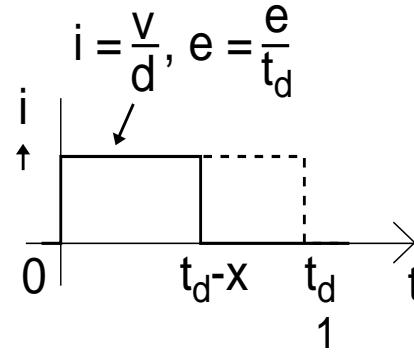
$$i(t) = \frac{Q_0}{t_d} \left(1 - \frac{t}{t_d}\right) e^{-t/\tau} \quad t < t_d$$



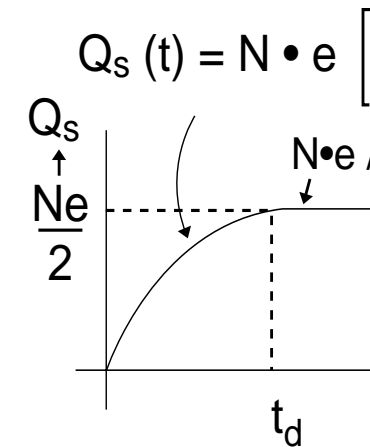
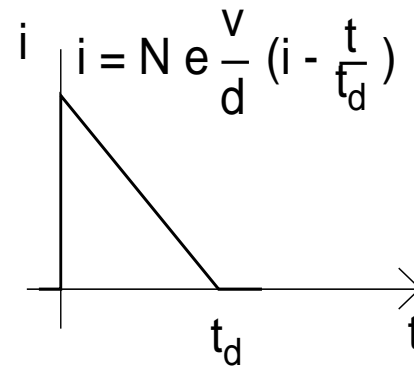
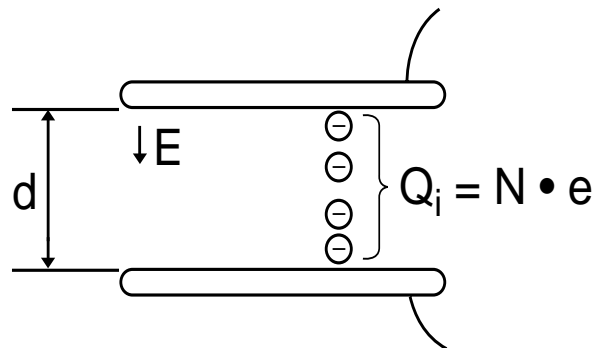
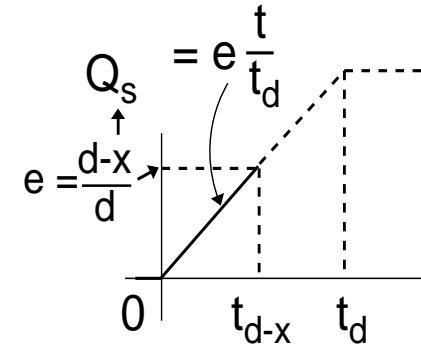
Charge Collection in LAr Ionisation Chamber



CURRENT



CHARGE



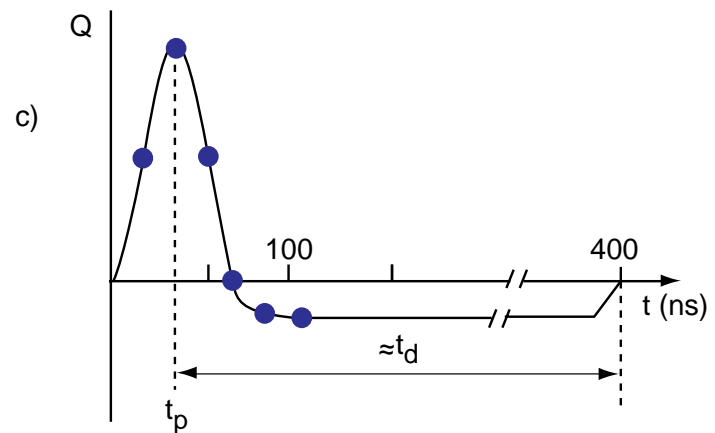
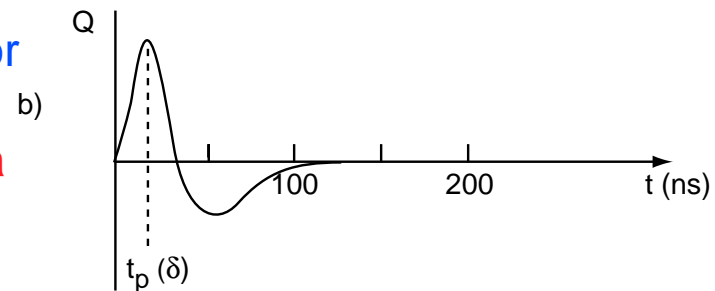
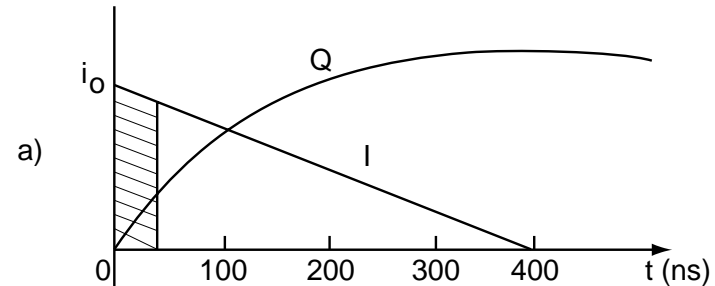
The current and charge for a) single electron-ion pair, b) uniformly distributed e-ion pairs

- Induced current duration = electron drift time t_d , with a triangular shape

- bipolar impulse response of chamber-preamp-shaper, most important condition for pulse shaping at high rates is
system impulse response should have zero area
 pileup then does not produce a baseline shift

- for $t_p \ll t_d$, i.e. peaking time much faster than drift time, output response becomes 1st derivative of current pulse

energy info. fully contained in the initial current i_0



JV_204



ATLAS LAr e.m. Calorimeter

The "accordion" concept, with electrodes essentially parallel to incoming particle's direction allows:

- high rate operation
avoid long connections between calorimeter cells to the electronics chain which lead to a slow response and high ENC
- high granularity readout in a barrel geometry with tower dimensions of \approx Molière radius

Features

- thin Pb-absorbers (1.2 mm for $|\eta| > 0.7$)
- towers project towards collision point, 3-fold longitudinal segmentation
- constant liquid argon gap is maintained
- fast response, by pulse shaping, exploits very fast rise of ionisation current, and reduces level of pileup



Quartz Fibre Calorimeters

- radiation hardness - quartz is one of most rad-hard solids
- fast - signal generated by C^ν irradiation
- narrow (and short showers) - only e^\pm produced in shower development give an appreciable signal
- little sensitivity to induced radioactivity | C^ν light emitted only by
- no sensitivity to evaporation neutrons | relativistic charged part.
- drawback - low light yield : 25% packing fraction \Rightarrow 10 pe/GeV !

$n=1.46$ C^ν thresholds : e^\pm - 0.7 MeV, π^\pm - 0.19 GeV, p - 1.3 GeV

Suitable for Very Forward Regions in LHC ($3 < |\eta| < 5$)

- em showers - 70% of energy deposited by e^\pm with $E > 1$ MeV
 - hadronic showers - almost all non-em energy is invisible (e.g. $\approx 15\%$ of non-em through π^\pm in shower at 5 GeV in Fe)
- expect e/h to be large (> 7) i.e. strongly non-compensating

Energy Resolution

- Hadronic signal determined by π^0 's produced
 - Expect hadronic energy resolution to be governed by event-to-event fluctuation in F_0 - will not obey Poissonian statistics
- $$F_0 \approx 0.435 - 0.052 \ln E$$
- For a calorimeter only sensitive to em shower component, energy resolution improves logarithmically with energy and not as $1/\sqrt{E}$
- $\sigma(F_0) \gg$ sampling or photostatistic (usually)

eg. 1 pe/GeV increase σ/E from 17 % to 19% at 150 GeV
at higher energies even better $\sigma(F_0) \approx 1/\ln E$ whereas $\sigma_{pe} \approx 1/\sqrt{E}$



Different ECAL/HCAL Calorimeter Structure

LHC pp experiments have put more emphasis on high precision e.m. calorimetry

High precision e.m. calorimetry is not compatible with perfect compensation

e.g. ZEUS :

$$\frac{\sigma_e}{E} = \frac{17\%}{\sqrt{E}} \quad \text{and} \quad \frac{\sigma_h}{E} = \frac{35\%}{\sqrt{E}}$$

BUT considerable importance has still to be placed on

- Gaussian hadronic energy response function (exact value of (σ/E) less important
- hermiticity
- linearity for jets

How do ATLAS and CMS calorimeter systems perform ?

Comparison with hadronic MC codes.



Trigger and Data Acquisition

The Challenge at the LHC

Purpose

Trends

Trigger Levels at LHC

Physical Trigger Levels - CMS

Level-1 Calorimeter Trigger - ATLAS

Calorimeter Trigger Rates - CMS

Muon Chamber Trigger Logic - CMS

Muon Rates

Summary - CMS

Selective Event Building and Higher Level Triggers

Trigger Rates and Physics

Super-Computing Trends

LHC Trigger/DAQ Perspectives



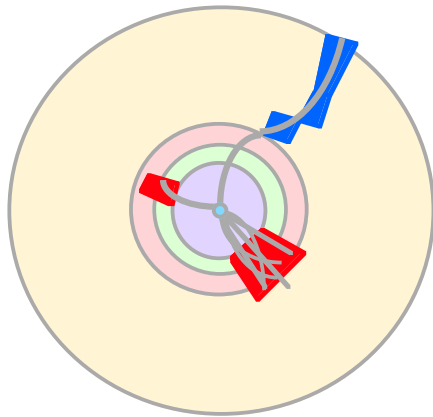
Trigger/DAQ : The Challenge at the LHC

Trigger is a key part of any HEP experiment

At LHC in pp general purpose experiments
select 100 events to record out of 10^9 interactions !

- very high efficiency of selection
none of the few rare events should be missed
- select events without bias
- selection process should incur as little deadtime as possible
- reduce data flow as early and as quickly as possible
<20> interactions every 25 ns \Rightarrow 40,000 GB/s !!
need information superhighway !
- must make sure selection process uses all subdetector data
from the same crossing
synchronise millions of channels to \ll 25 ns !
- can only store data at \approx 100 Hz
need to reject almost all events
- all done in real time
cannot go back and recover events
need to monitor selection process

Interaction rate 10^9 Hz

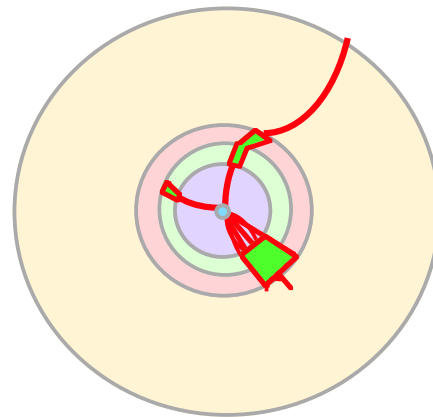


Trigger Objects

cut on p_T , E_T of em clusters, muons, jets, missing E_T , isolation

- $\Delta t_{\text{dec}} \approx 3 \mu\text{s}$ - no time to combine information from different sub-detectors
- Perform elementary operations with elementary conditions
- Local pattern recognition and energy evaluation using prompt reduced granularity information
- Parallel and pipelined processing custom made processors

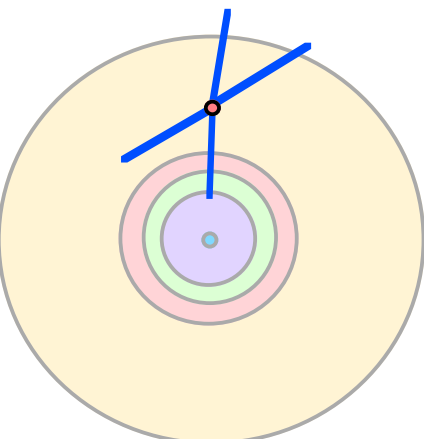
Level-1 selected events 10^5 Hz



Clean particle signature (Z, W, ..)

- Full granularity used for precise meas.
- Kinematics. Effective mass cuts and event topology
- Track reconstruction and detector matching (shower shape, E/p etc)

Level-2 selected events 10^3 Hz

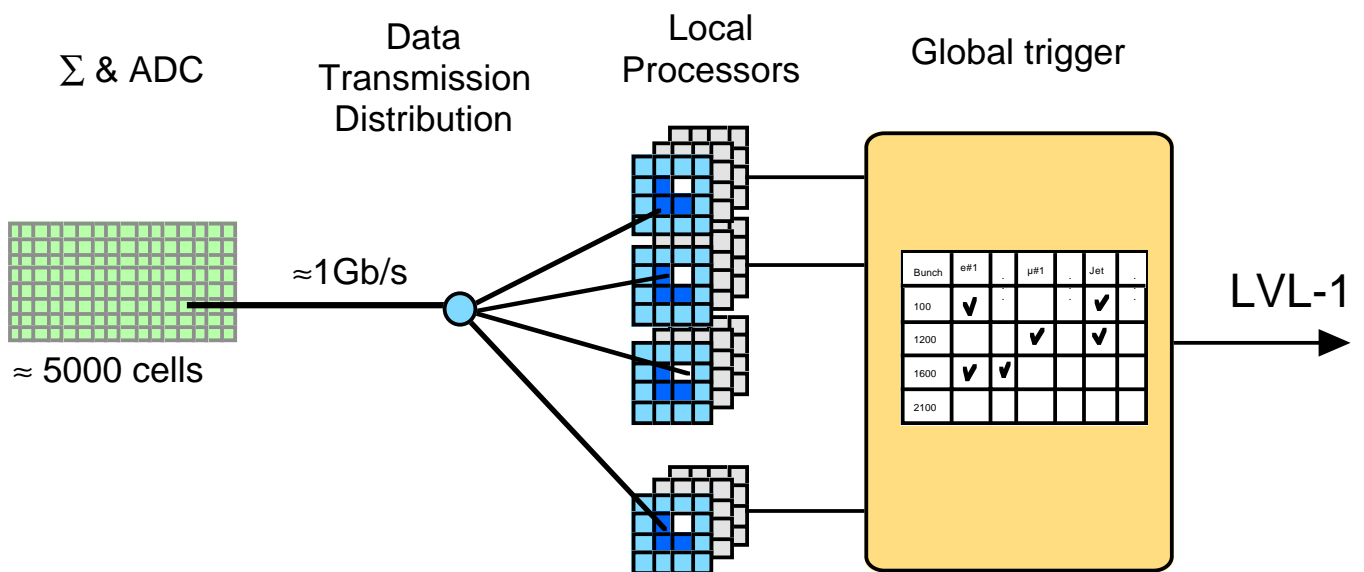
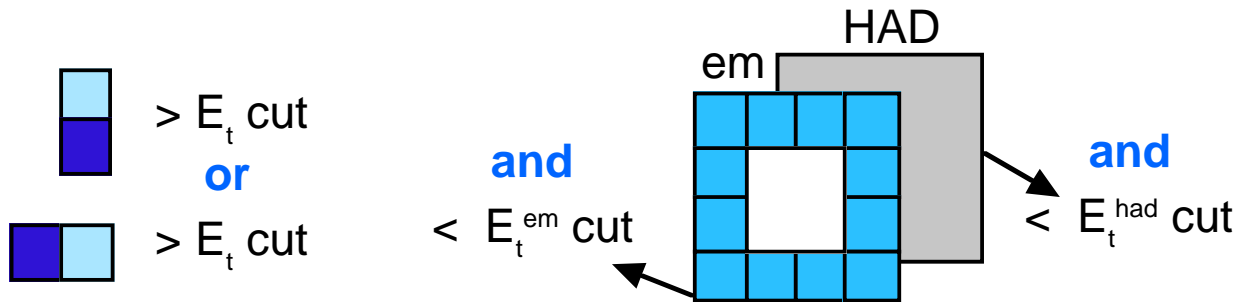


Physics process identification

- Event reconstruction and analysis

Level-3 events to tape 10..100 Hz

Isolated electron algorithm:



Sliding window for each tower

Extension to a τ -trigger

Vertical or horizontal sum of two trigger towers in both

ECAL + HCAL $> E_t^{cut}$

Isolation as before with different E_t^{cut}

Sliding window for each tower

Jet-trigger

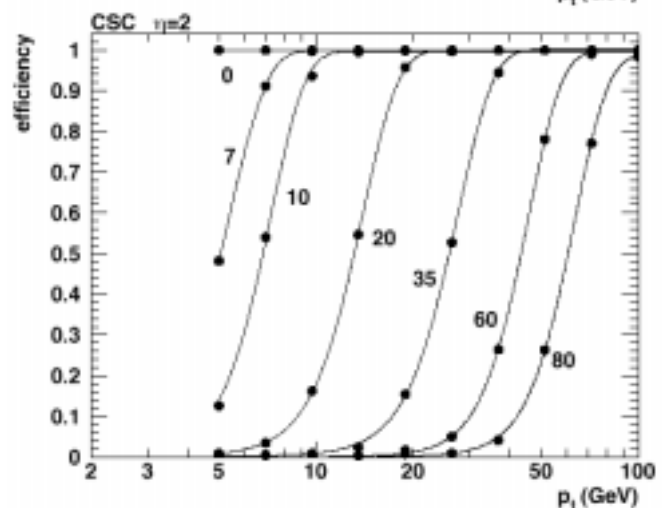
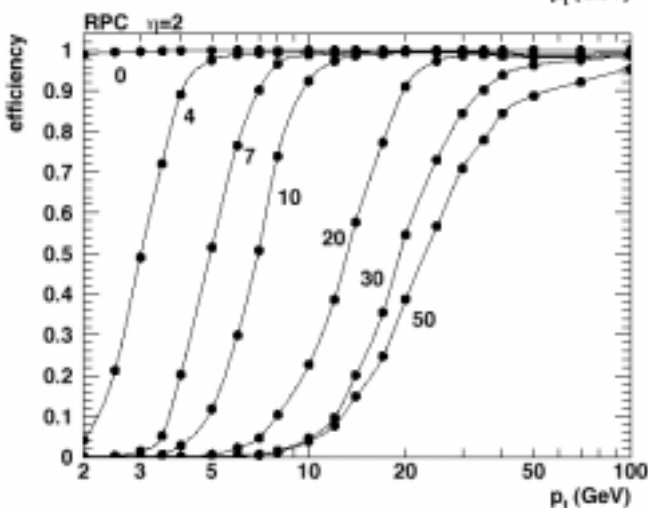
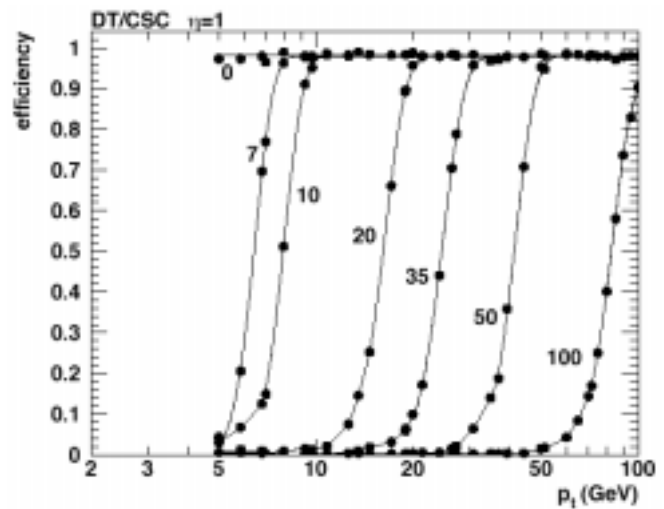
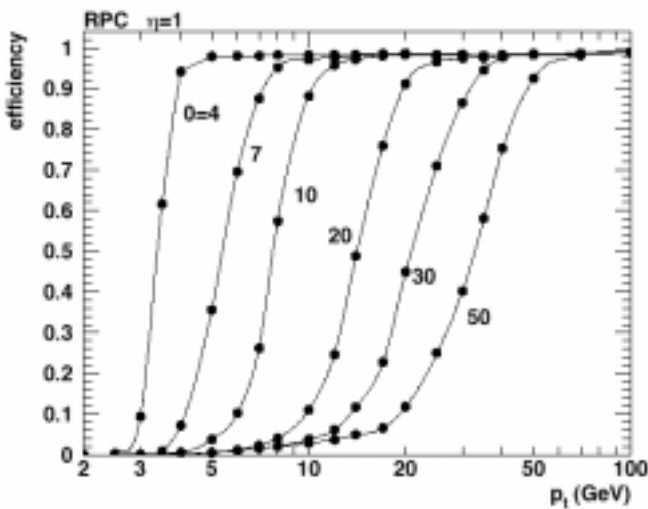
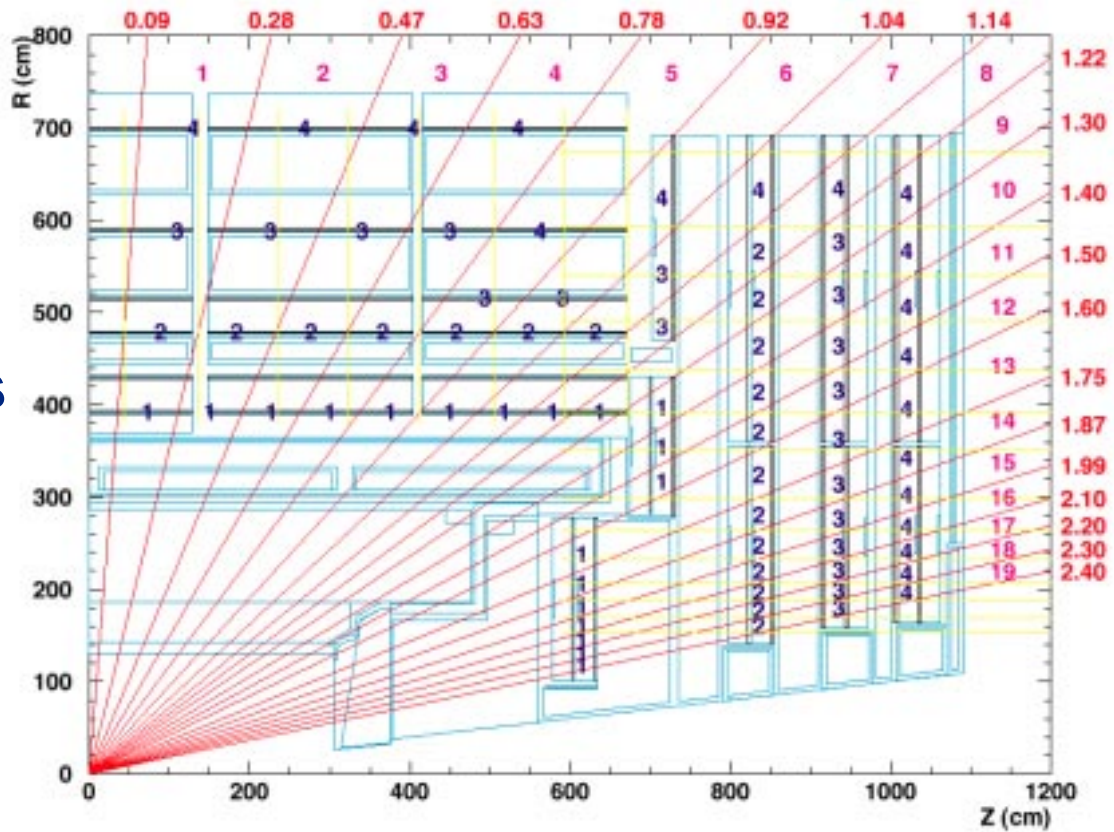
Sum of energies in 4x4 trigger towers in ECAL and HCAL $> E_t^{cut}$

Sliding window for each block of 2x2 towers



Muon Trigger Segmentation and Efficiency

CMS
RPCs





Trigger Rates and Physics

Calorimeter Trigger Rate at High Luminosity in CMS

Type	E_t^{cut} GeV	Individ. kHz	Increm. kHz
Sum E_t	400	0.3	0.3
E_t^{miss}	80	1.2	0.9
e	25	11.4	9.3
2-e	12	2.1	1.8
1- jet	100	1.5	1.0
2 - jet	60	1.2	0.7
jet + e	50/12	1.3	0.3
Cumulative		≈ 17	

Muon Trigger Rate at High Luminosity in CMS

Type	E_t^{cut} GeV	Individ. kHz	Increm. kHz
μ	20	7.8	7.8
2 - μ	4	1.6	9.2
μ e/ γ	4/8	5.5	14.4
μ -jet	4/40	0.3	14.4
μ - E_t^{miss}	4/60	1.0	15.3
Cumulative		≈ 15	

Physics Efficiency

H(80GeV) $\rightarrow \gamma\gamma$	99%
H(150 Gev) $\rightarrow 4l$	≈ 100 %
pp $\rightarrow tt \rightarrow eX$	88%
Σ SUSY	83%