

Theoretical physics for the LHC, Lecture IV



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Higgs production at the LHC

Several production mechanisms are possible, each of them being more or less important depending on:

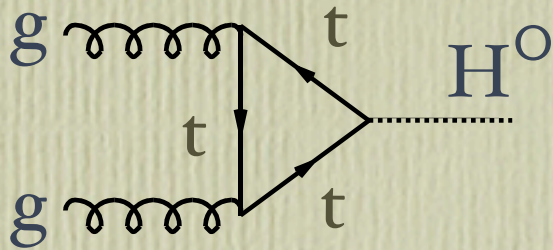
- the value of the production rate
- the value of the decay BR to usable channels
- the size of the backgrounds

The relative importance of these aspects is a function of the Higgs mass

The ability to detect more than one production and/or decay channels is crucial to fully establish the properties of the Higgs boson, and to understand whether it behaves as predicted by the Standard Model

While a complete study of the Higgs boson will require data from several accelerators (e+e- linear collider, photon-photon collider, muon collider), the LHC will provide the first important inputs. Depending on m_H , the value of these inputs will vary significantly.

Four main production mechanisms at the LHC:

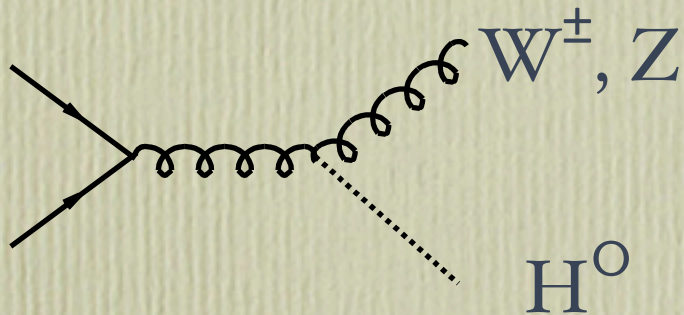
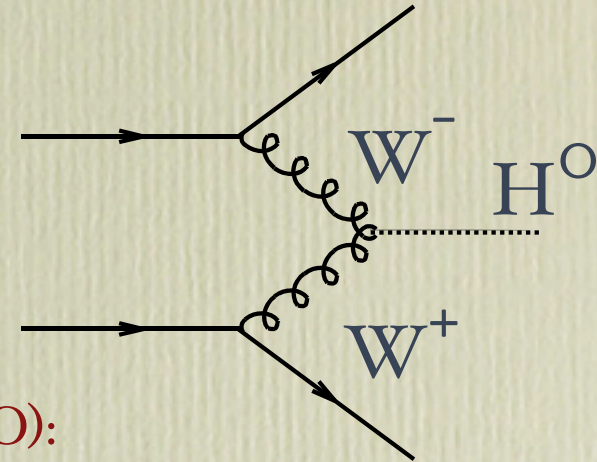


Gluon-gluon fusion (NNLO):

- Largest rate for all $m(H)$.
- Proportional to the top Yukawa coupling, y_t
- gg initial state

Vector-boson (W or Z) fusion (NLO):

- Second largest, and increasing rate at large $m(H)$.
- Proportional to the Higgs EW charge
- mostly ud initial state

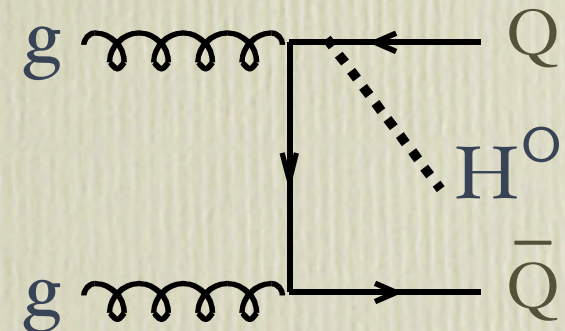


W(Z)-strahlung (NNLO):

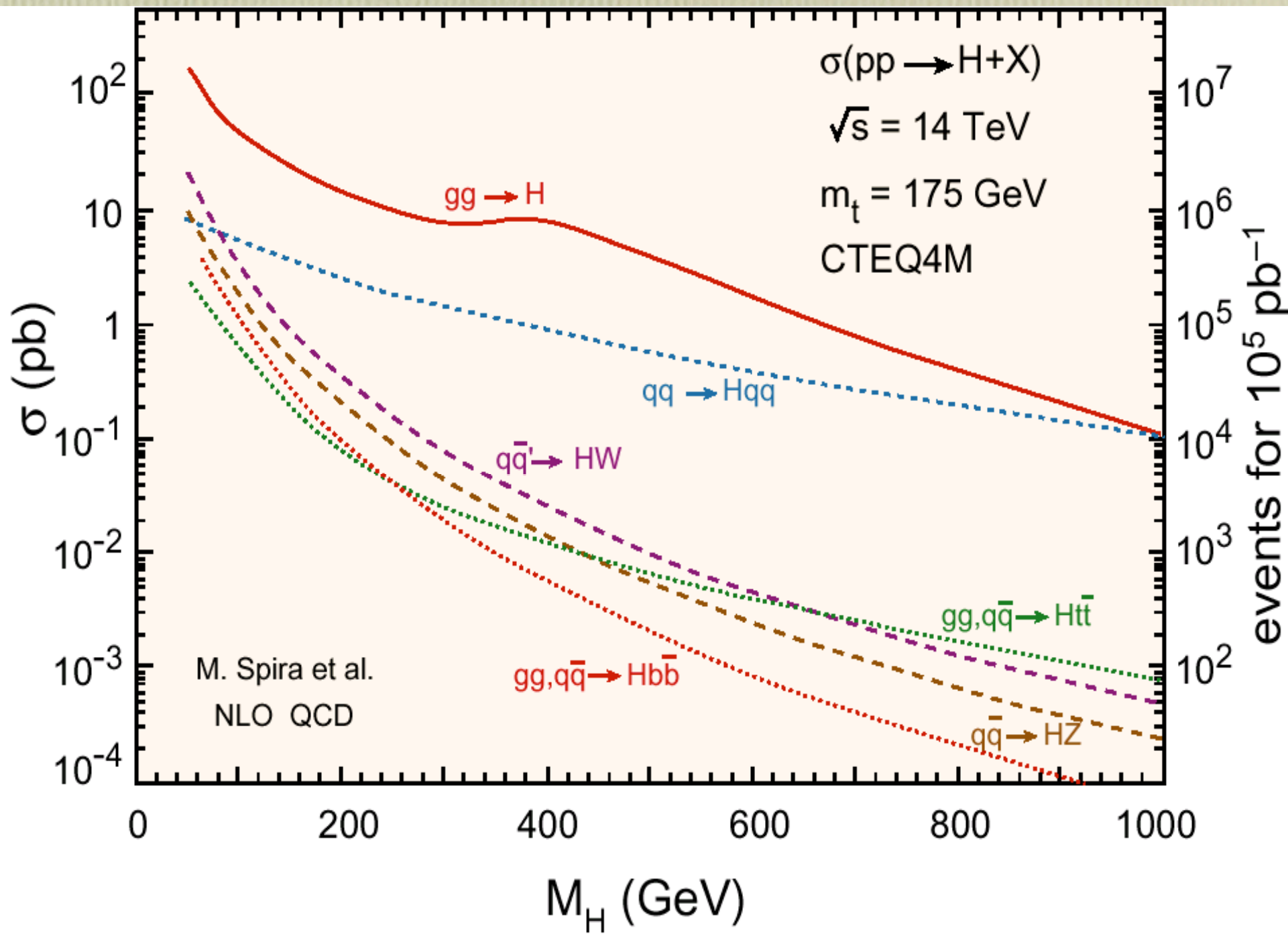
- Same couplings as in VB fusion
- Different partonic luminosity (uniquely $qqbar$ initial state)

ttH/bbH associate production (NLO):

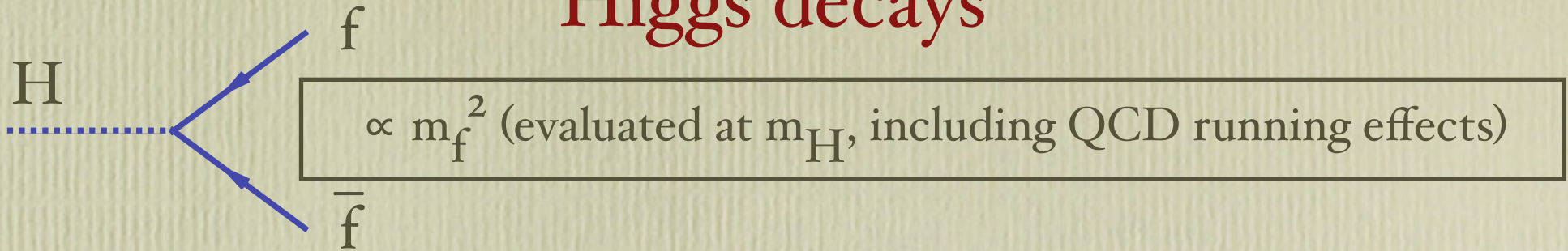
- Proportional to the heavy quark Yukawa coupling, y_Q , dominated by ttH , except in 2-Higgs models, such as SUSY, where b -coupling enhanced by the ratio of the two Higgs expectations values, $\tan\beta^2$
- Same partonic luminosity as in gg -fusion, except for different x -range



Higgs production rates at the LHC

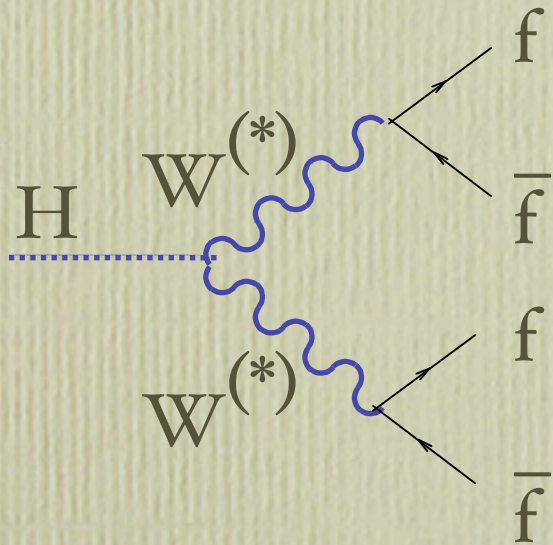
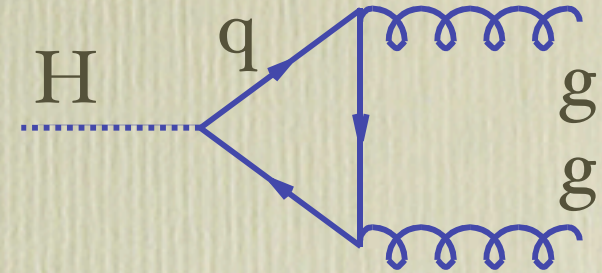


Higgs decays



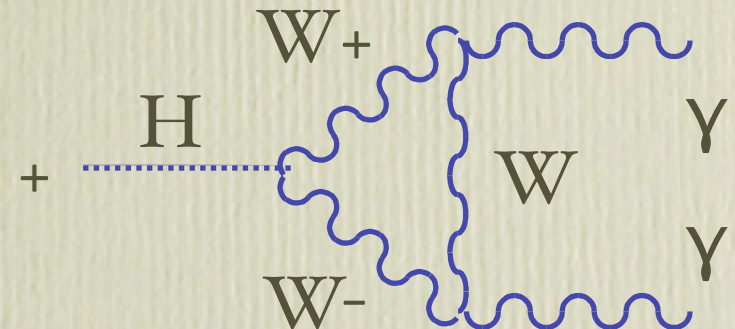
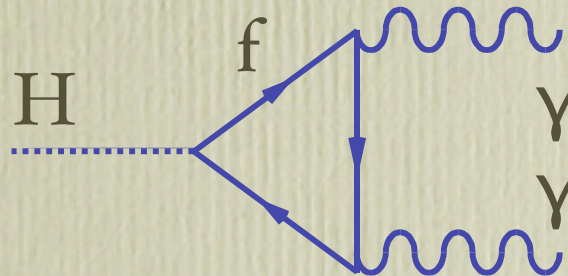
$\propto m_f^2$ (evaluated at m_H , including QCD running effects)

$\propto m_f^2$ (dominated by top-quark loops)

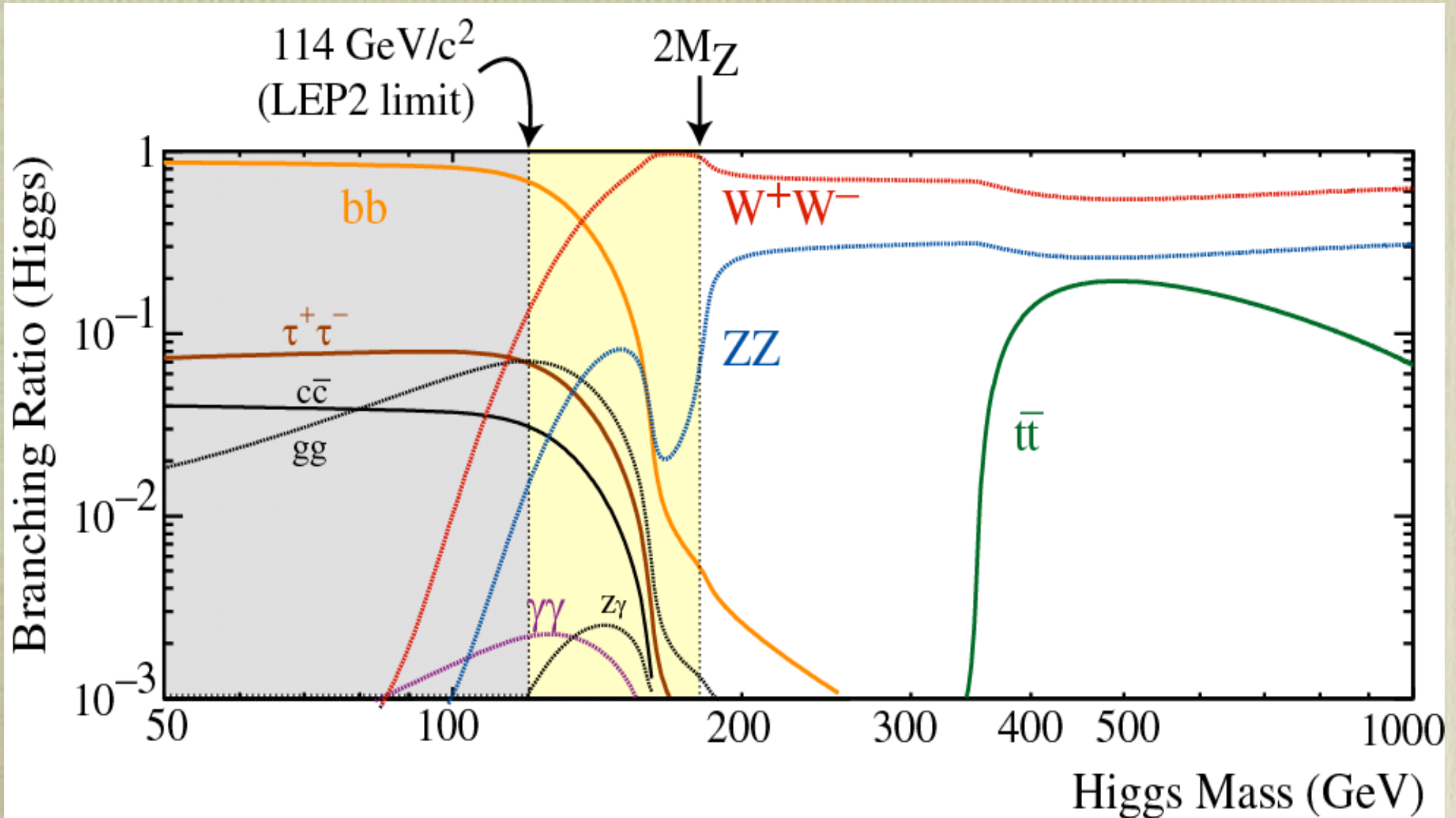


$\propto \alpha_W$ (sharp threshold at $m_H=2m_W$, but large BR even down to 130 GeV). Similar processes with $W \leftrightarrow Z$.

Dominated by the EW couplings, only minor contribution from top loop $m \Rightarrow$ correlated to $H \rightarrow WW$



Higgs decays



Not all decay modes are accessible at a given mass. Very high luminosity is required to thoroughly investigate the Higgs couplings

Search channels:

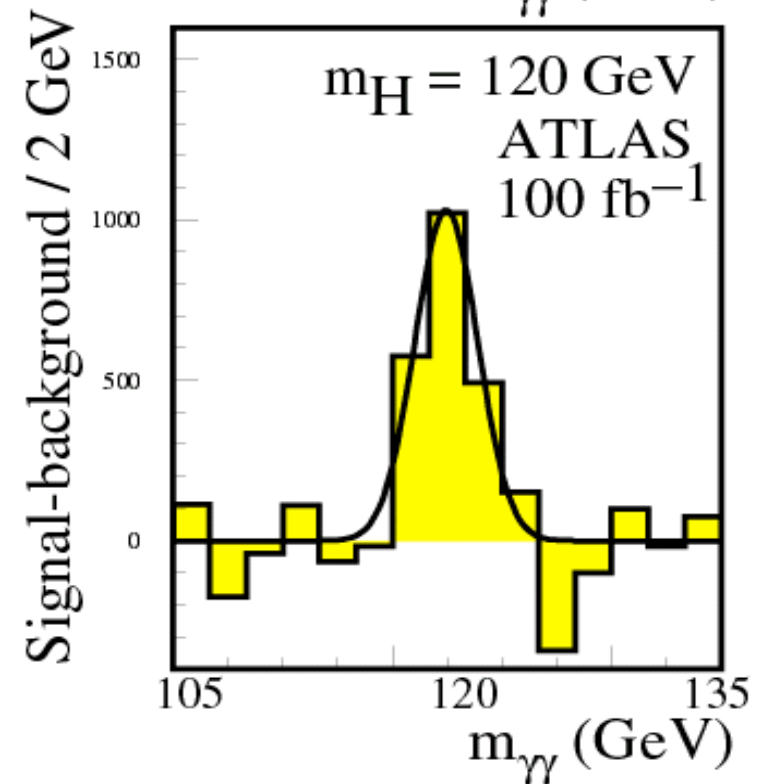
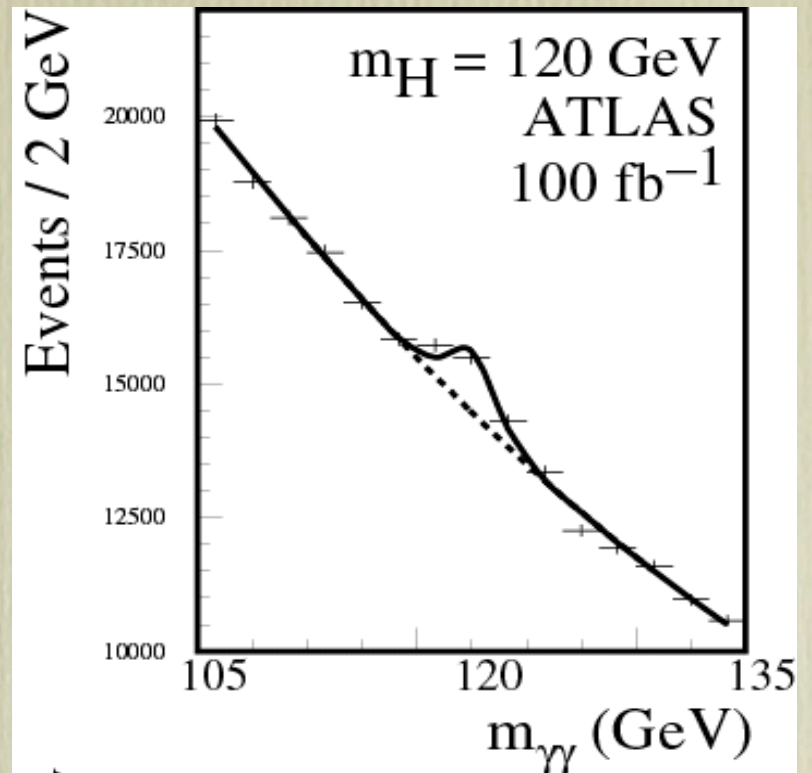
$$gg \rightarrow H \rightarrow \gamma\gamma$$

Acceptable BR only in the mass range

$m_H < 140 \text{ GeV}$ ($O(10^{-3})$).

Dominant background: QCD continuum production of $\gamma\gamma$ final states, plus tails in the QCD dijet or γ -jet production, with one or more jets fragmenting into isolated π^0 , faking a γ .

Significance:
2.8 to 4.3 σ
for 100 fb^{-1}

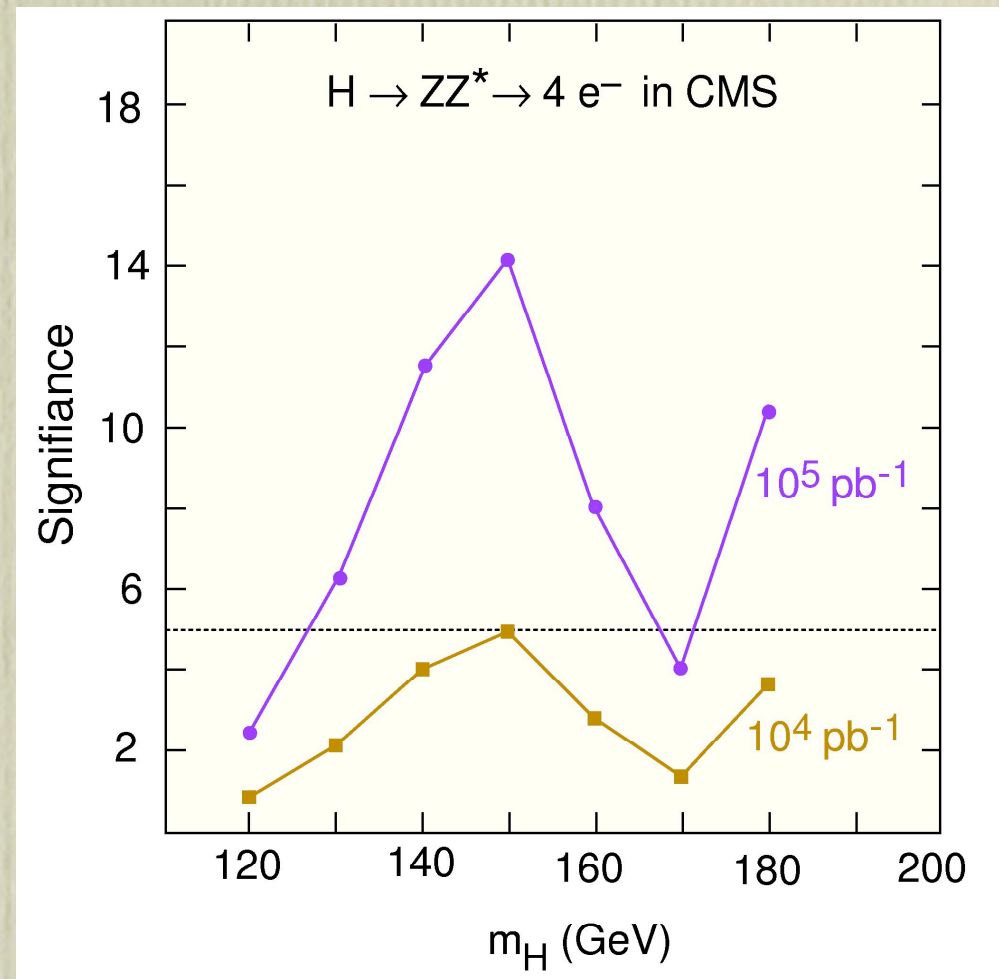
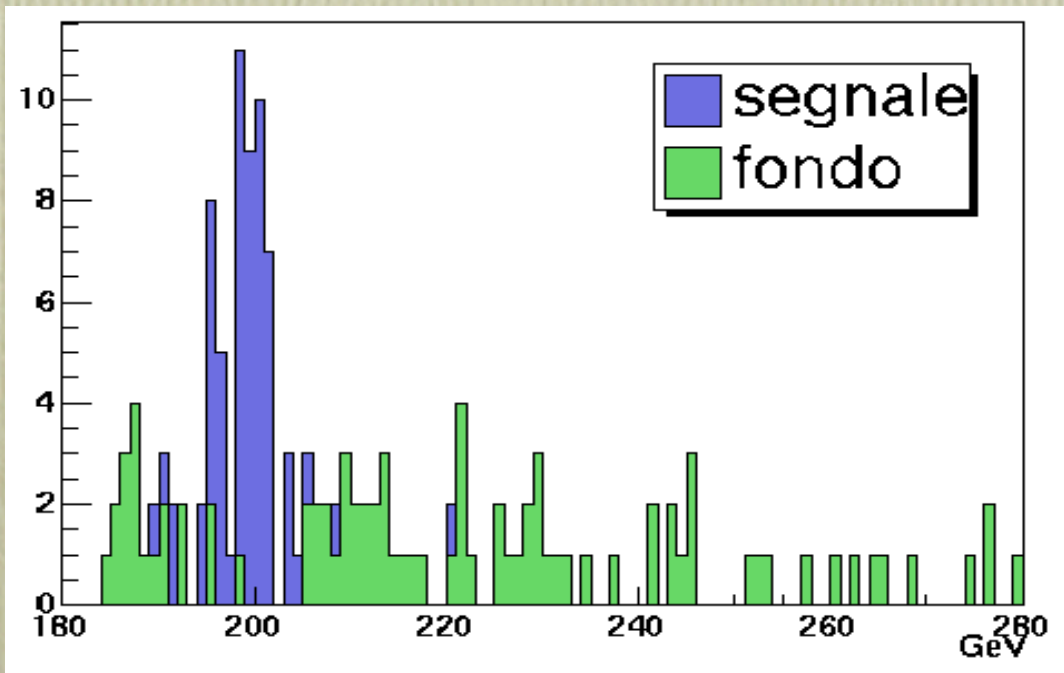


Search channels: $H \rightarrow ZZ^{(*)} \rightarrow \ell^+ \ell^- \ell'^+ \ell'^-$

Effective once at least one Z can be on-shell, $m_H > 130$ GeV, both in the gluon fusion and vector boson fusion production modes

Main bg: direct QCD ZZ production

Main bg rejection criteria: low rate, sideband interpolation



Search channels: $H \rightarrow WW^{(*)} \rightarrow \ell\bar{\ell}'\ell\ell'$

Effective once at least one W can be on-shell, $m_H > 120$ GeV, both in the gluon fusion and vector boson fusion production modes

Main bg: W -pair production from $t\bar{t}$ decays, and (smaller) from direct WW production

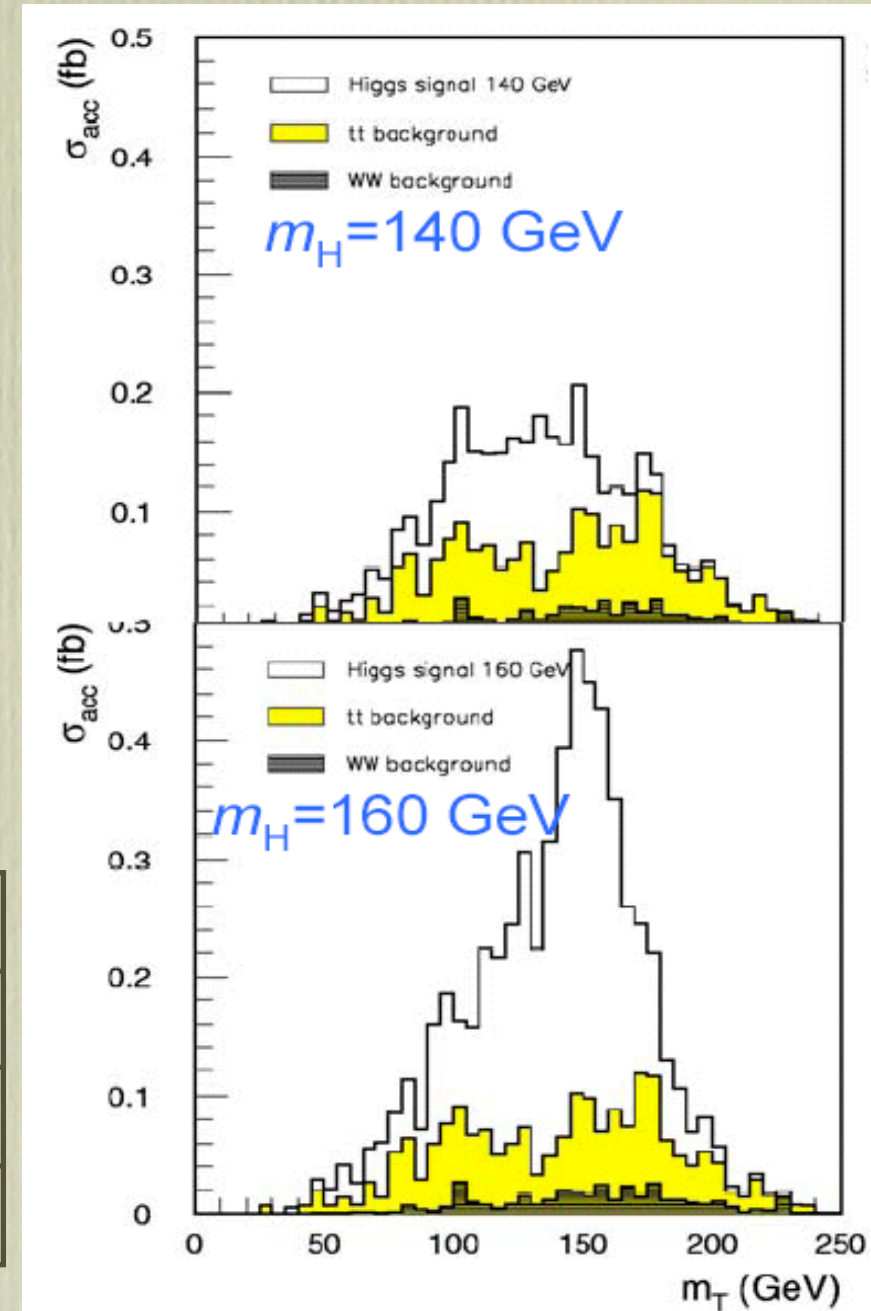
Main bg rejection criteria:

- 1) absence of additional jets (as in top decays)
- 2) momentum correlation among charged leptons
- 3) fwd jets (for VB fusion mode)

Exercise: prove that the matrix element for the signal is maximized when the two charged leptons have small invariant mass

With 5fb^{-1} , and 5% bg systematics:

| m_H (GeV) | 130 | 150 | 170 | 190 |
|--------------|-----|-----|-----|-----|
| Signal | 5 | 13 | 22 | 14 |
| Bg | 3 | 4 | 5 | 7 |
| S/\sqrt{B} | 2.1 | 4.7 | 6.5 | 4.2 |



Search channels: $gg \rightarrow t\bar{t}H \rightarrow t\bar{t}b\bar{b}$

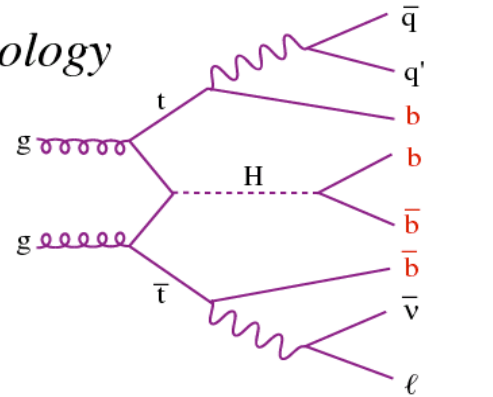
Challenging and complex topology

4 b-jets, 2 jets, 1 lepton

$H \rightarrow b\bar{b}$

$t \rightarrow bqq'$

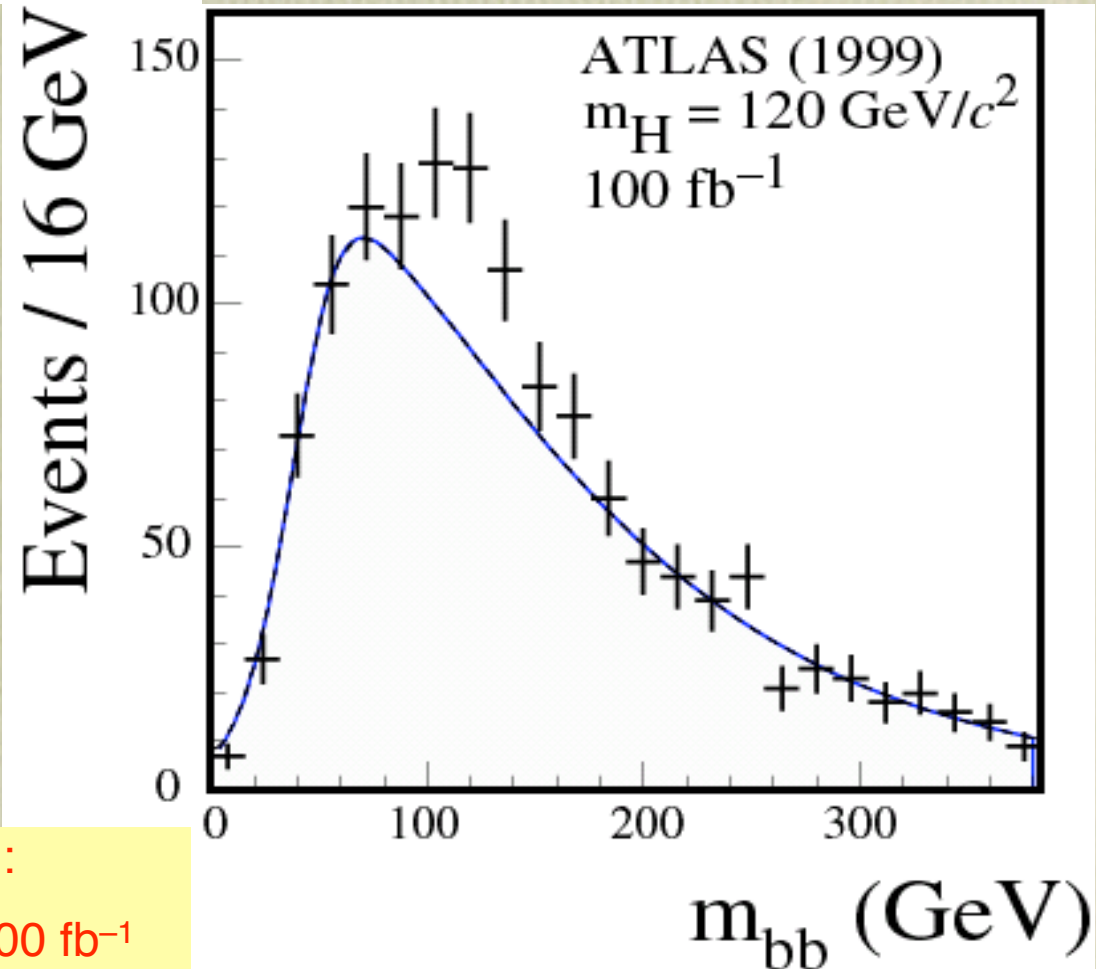
$t \rightarrow b\ell\nu$



Main bg: $t\bar{t}b\bar{b}$ production, in association with (possibly b) jets

Main bg rejection criteria:

- 1) multiple b tags
- 2) peak in $m(bb)$ (try to achieve as good mass resolution as possible)



Signal significance (5σ) :

$m_H < 120 \text{ GeV}$ needs 100 fb^{-1}

Discovery reach for low-mass Higgs at the LEP2 limit (115 GeV, 10fb⁻¹)

| | H → γγ | ttH → ttbb | qqH → qqττ |
|------|--------|------------|------------|
| S | 130 | 15 | 10 |
| B | 4300 | 45 | 10 |
| S/√B | 2.0 | 2.2 | 2.7 |

Will require the combination of several, low-significance, channels. Combined significance:

$$4^{+2.2}_{-1.3} \sigma$$

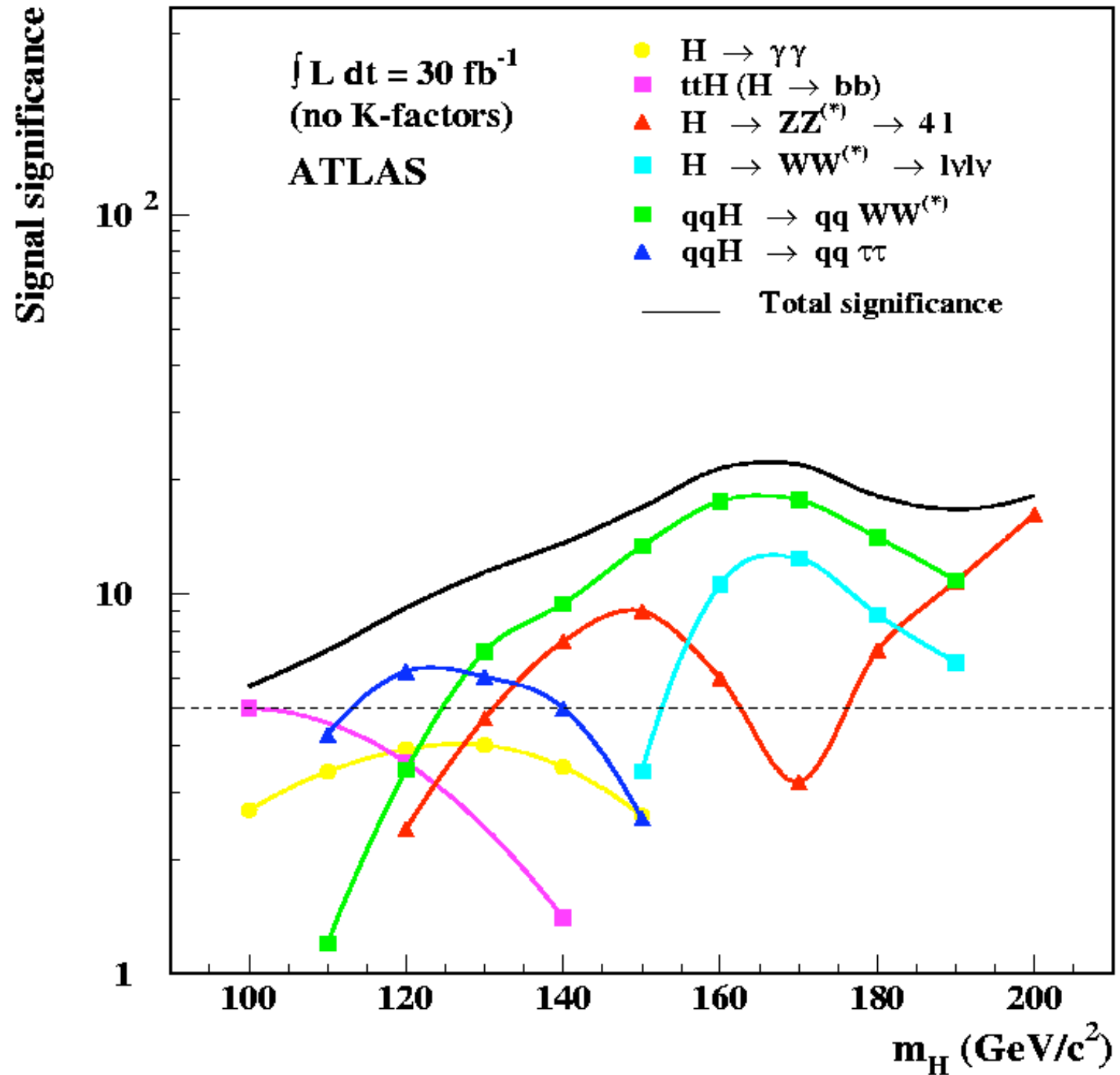
Discovery reach for low-mass Higgs just above the LEP2 limit (130 GeV, 10fb⁻¹)

| | $H \rightarrow \gamma\gamma$ | $qqH \rightarrow qqWW$ | $qqH \rightarrow qq\tau\tau$ | $H \rightarrow 4l$ |
|---------------|------------------------------|------------------------|------------------------------|--------------------|
| S | 120 | 18 | 8 | 5 |
| B | 3400 | 15 | 6 | <1 |
| S/ \sqrt{B} | 2.0 | 3.9 | 2.7 | 2.8 |

Combined significance: **6 σ**

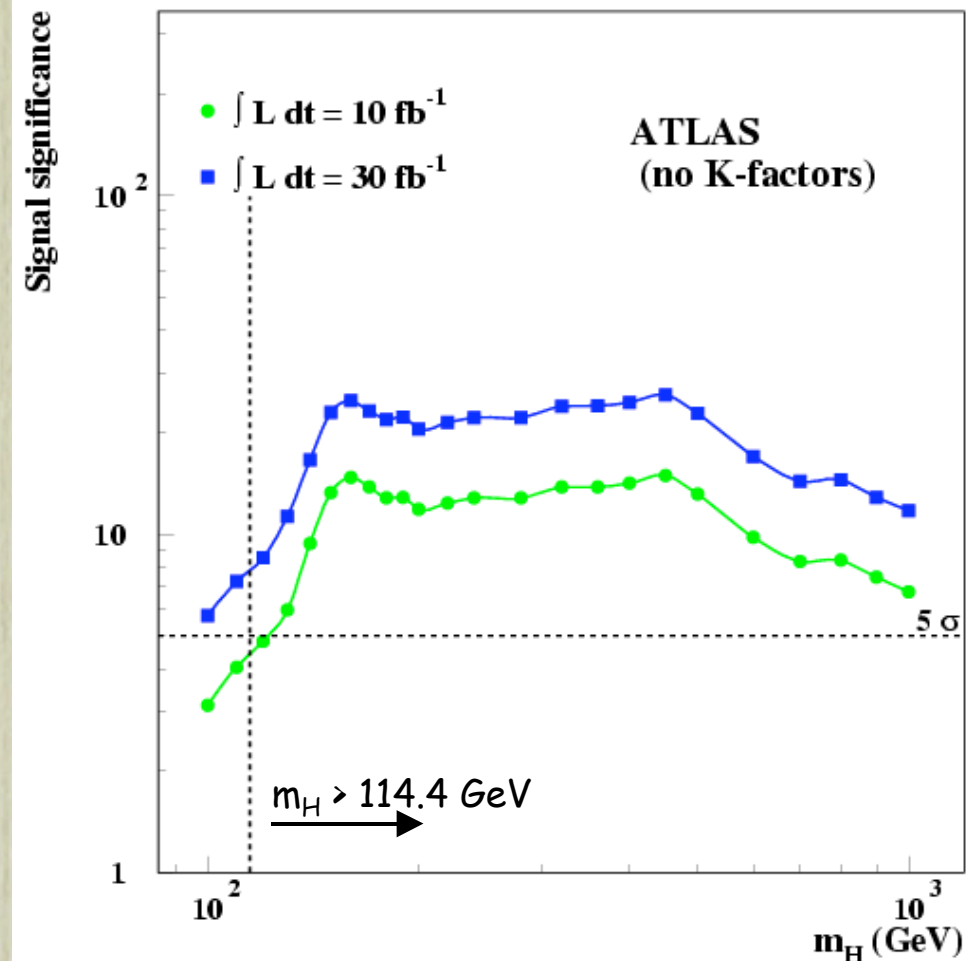
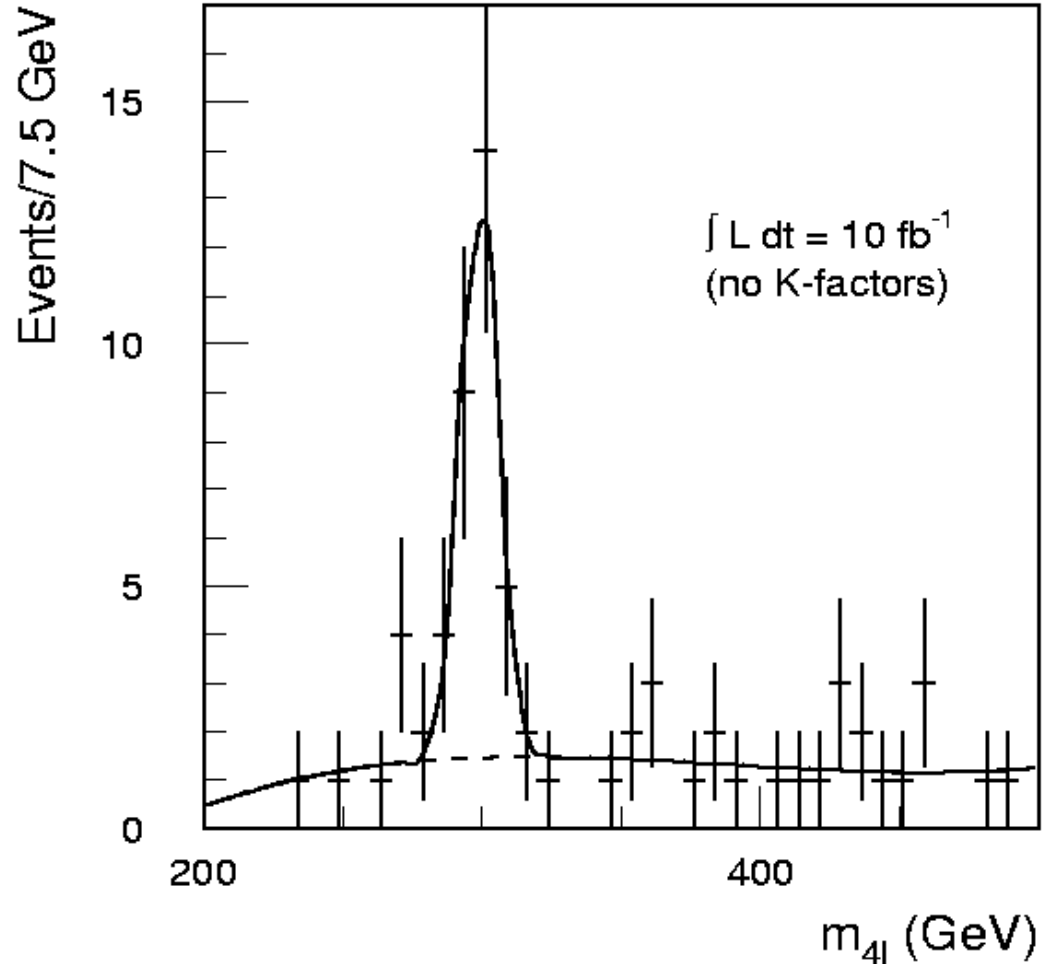
Light Higgs reach at the LHC

1 year of data taking at nominal luminosity should be sufficient for the two experiments to detect a Higgs through most of the expected mass range



High mass region

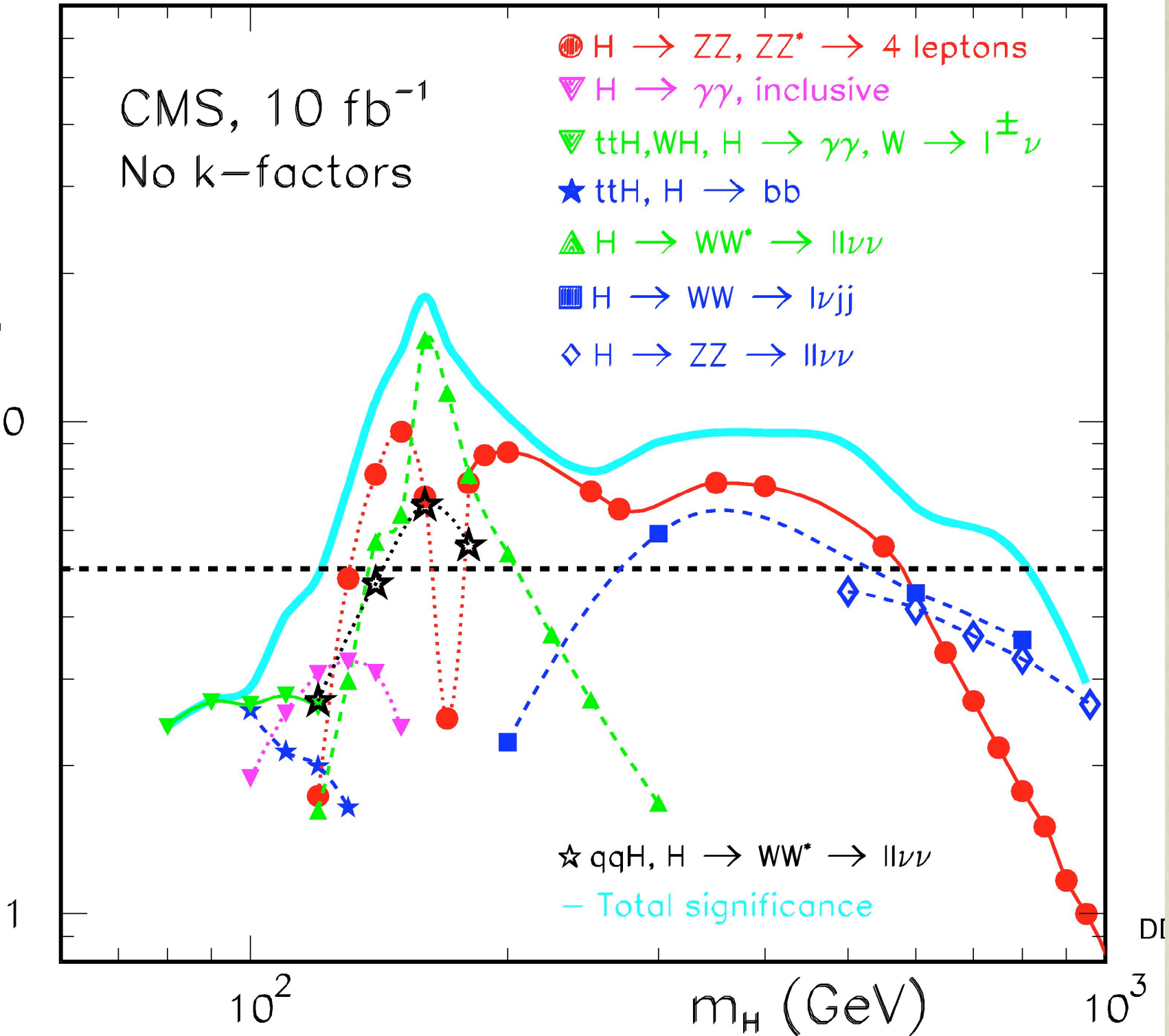
- Easy discovery using $H \rightarrow ZZ \rightarrow 4$ leptons for $200 < m_H < 600$ GeV
- H width larger than detector resolution for $m_H > 300$ direct measurement of total width!
- Combine several channels $m_H > 600$ GeV:
 - $H \rightarrow ZZ \rightarrow 2\text{lept } 2 \nu$, $2\text{lept } q \bar{q}$
 - $H \rightarrow WW \rightarrow l\nu \ q \bar{q}$



Significance

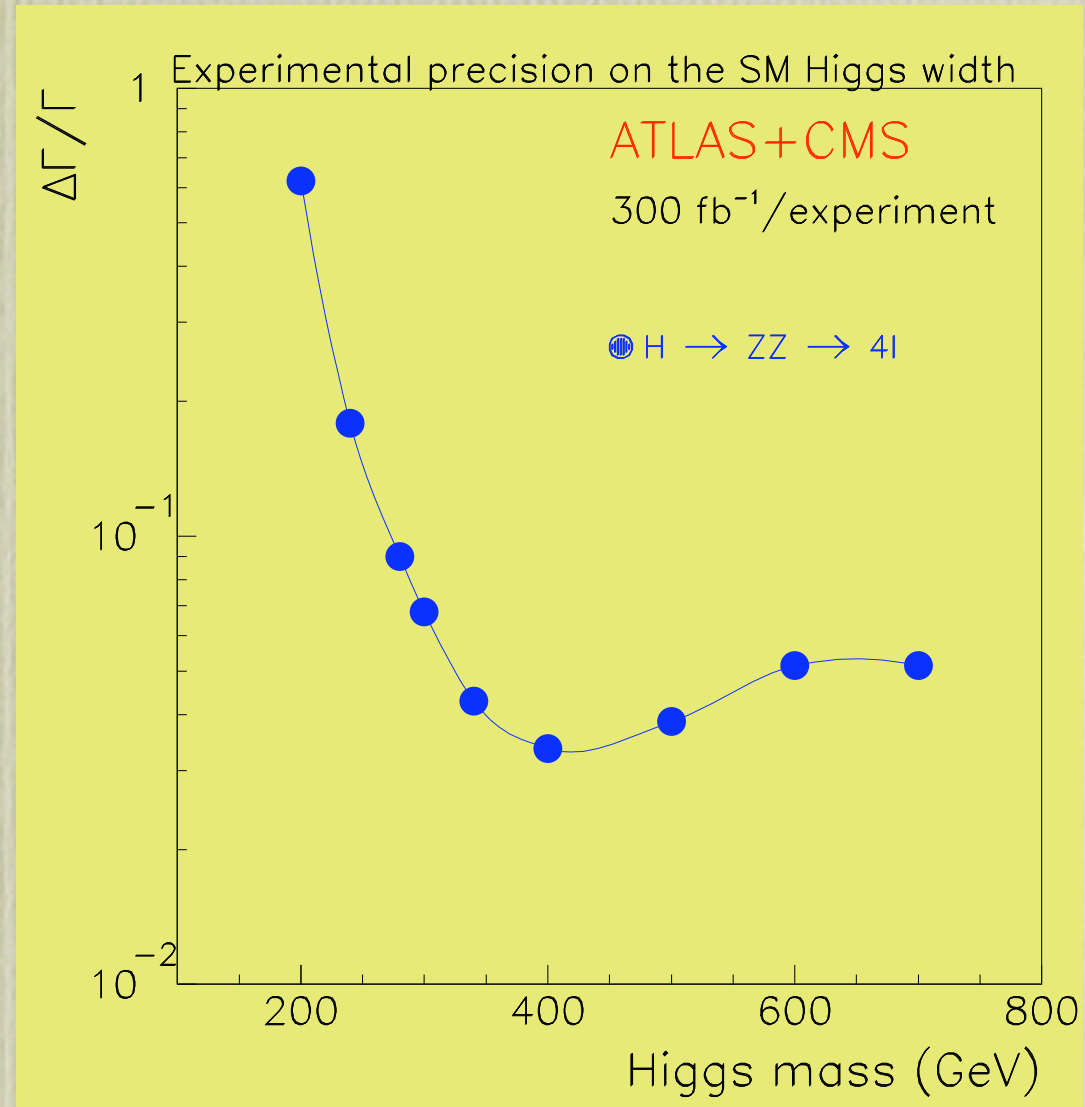
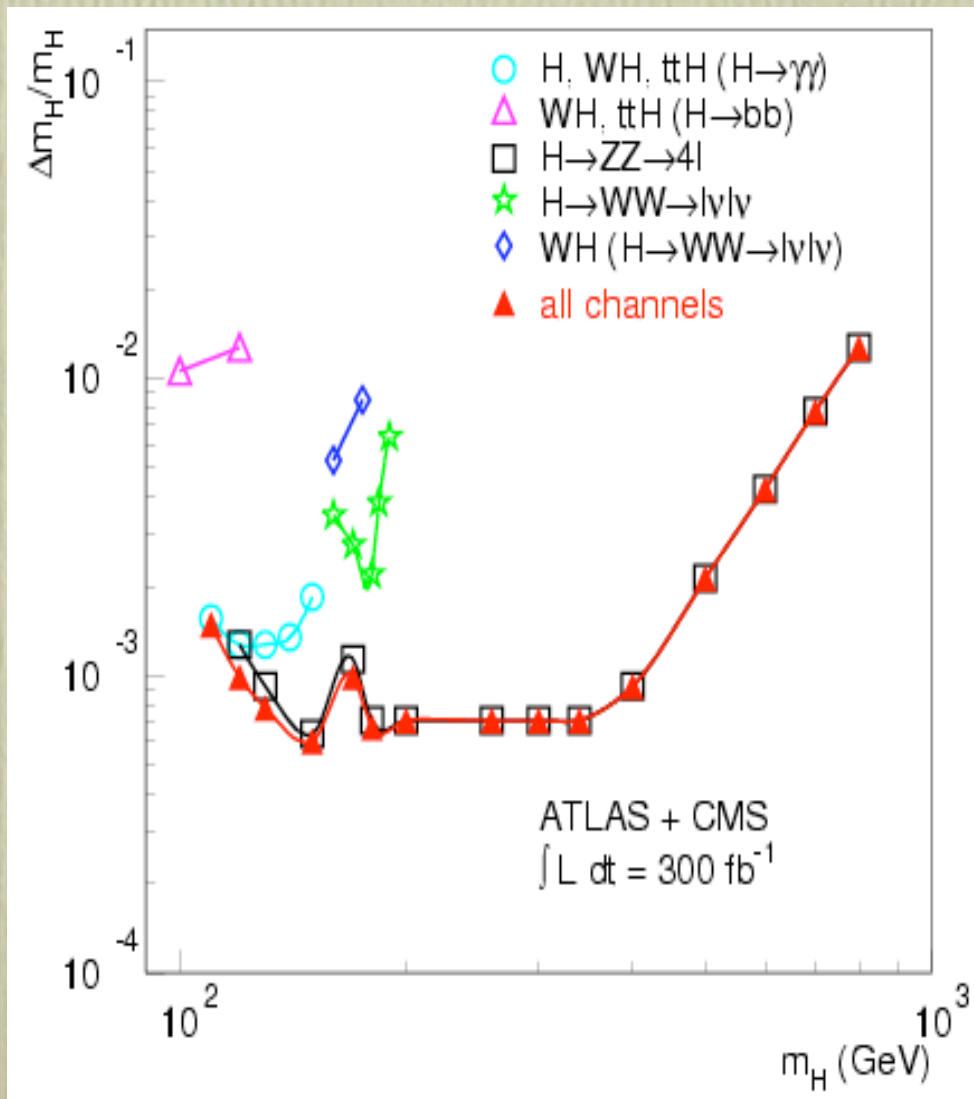
CMS, 10 fb^{-1}
No k-factors

- $H \rightarrow ZZ, ZZ^* \rightarrow 4 \text{ leptons}$
- ▼ $H \rightarrow \gamma\gamma, \text{ inclusive}$
- ▽ $ttH, WH, H \rightarrow \gamma\gamma, W \rightarrow l^\pm \nu$
- ★ $ttH, H \rightarrow bb$
- ▲ $H \rightarrow WW^* \rightarrow ll\nu\nu$
- $H \rightarrow WW \rightarrow l\nu jj$
- ◇ $H \rightarrow ZZ \rightarrow ll\nu\nu$



DI

Direct measurement of Higgs mass and width



Direct measurement of Higgs couplings

Different production and decay channels provide measurements of the following combinations of partial decay widths

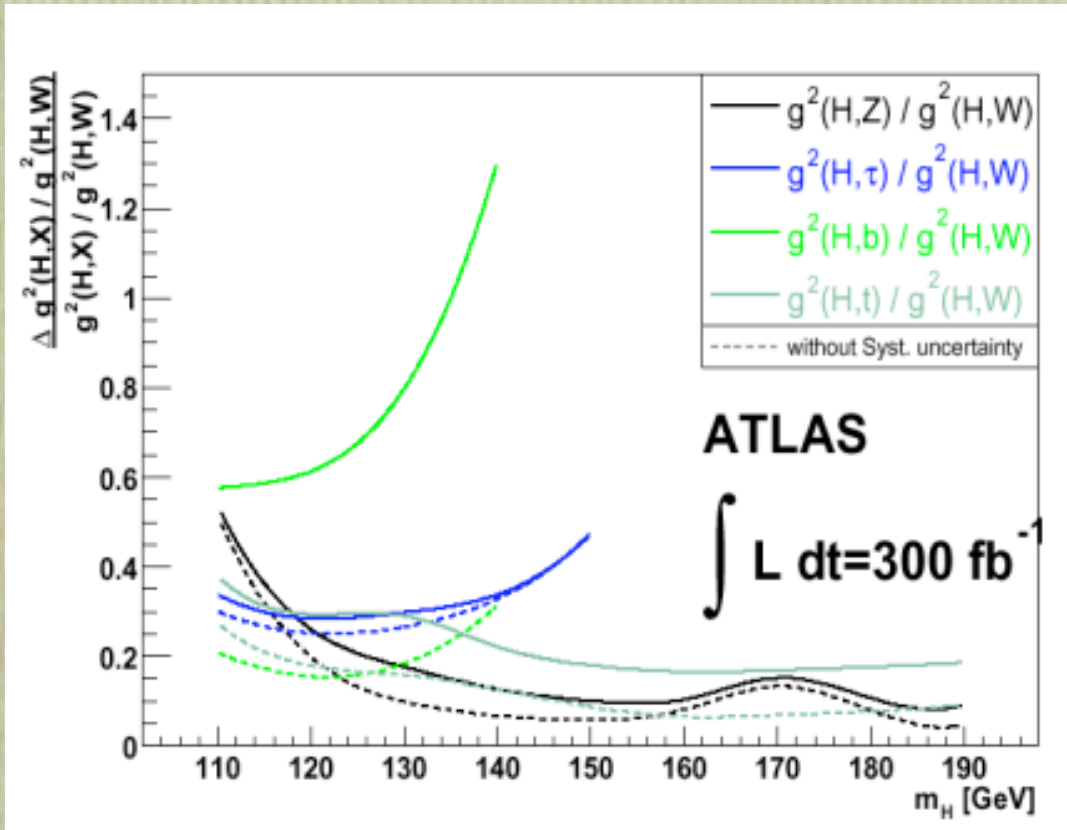
$$\begin{aligned}
 X_{\gamma} &= \frac{\Gamma_W \Gamma_{\gamma}}{\Gamma} & \text{from } qq \rightarrow qqH, H \rightarrow \gamma\gamma, & & Y_{\gamma} &= \frac{\Gamma_g \Gamma_{\gamma}}{\Gamma} & \text{from } gg \rightarrow H \rightarrow \gamma\gamma, \\
 X_{\gamma} &= \frac{\Gamma_W \Gamma_{\gamma}}{\Gamma} & \text{from } qq \rightarrow qqH, H \rightarrow \gamma\gamma, & & Y_Z &= \frac{\Gamma_g \Gamma_Z}{\Gamma} & \text{from } gg \rightarrow H \rightarrow ZZ^{(*)}, \\
 X_W &= \frac{\Gamma_W^2}{\Gamma} & \text{from } qq \rightarrow qqH, H \rightarrow WW^{(*)}, & & Y_W &= \frac{\Gamma_g \Gamma_W}{\Gamma} & \text{from } gg \rightarrow H \rightarrow WW^{(*)}
 \end{aligned}$$

Ratios of X or Y quantities factor out not just the partial widths to either W or gluon, but also the overall initial-state parton luminosities and uncertainties on the production cross-sections.

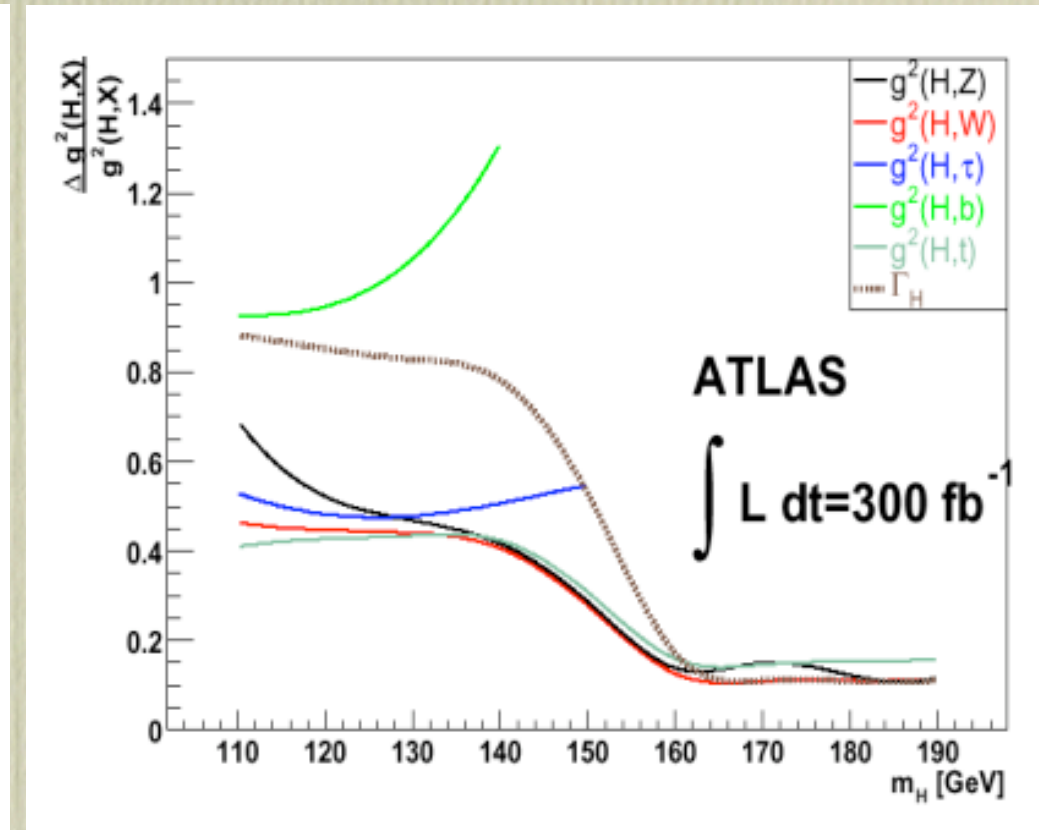
$$\begin{aligned}
 y &= \frac{\Gamma_b}{\Gamma_{\gamma}} = 3c_{QCD} \frac{g_{Hbb}^2}{g_{H\gamma\gamma}^2} = 3c_{QCD} \frac{m_b^2(m_H)}{m_{\gamma}^2} \\
 \gamma &= 1 - \left(B(H \rightarrow b\bar{b}) + B(H \rightarrow \gamma\gamma) + B(H \rightarrow WW^{(*)}) + B(H \rightarrow ZZ^{(*)}) + B(H \rightarrow gg) + B(H \rightarrow \gamma\gamma) \right) \ll 1 \\
 \tilde{\Gamma}_W &= \left(\Gamma_{\gamma} + \Gamma_b + \Gamma_W + \Gamma_Z + \Gamma_{\gamma} + \Gamma_g \right) \frac{\Gamma_W}{\Gamma} = (1 - \gamma) \Gamma_W
 \end{aligned}$$

Measurement of Higgs couplings

Coupling ratios



Absolute couplings



Rare Higgs decays

$H \rightarrow e^+ e^-$: SM BR = 10^{-4} , reach for 6000 fb^{-1}

| m_H (GeV) | S/\sqrt{B} | $\delta\sigma \times \text{BR} / \sigma \times \text{BR}$ |
|-------------|--------------|---|
| 120 | 7.9 | 0.13 |
| 130 | 7.1 | 0.14 |
| 140 | 5.1 | 0.20 |
| 150 | 2.8 | 0.36 |

$H \rightarrow Z\gamma \rightarrow e^+ e^- \gamma$: independent determination of HZ coupling.

Sensitivity in the range of 3.5σ with 6000 fb^{-1} , 11σ with 60000 fb^{-1}

MSSM Higgs discovery potential

h^0, H^0, A^0, H^\pm

MSSM specific decays:

$A/H \rightarrow \tau\tau, tt$

$H \rightarrow hh$

$A \rightarrow Zh$

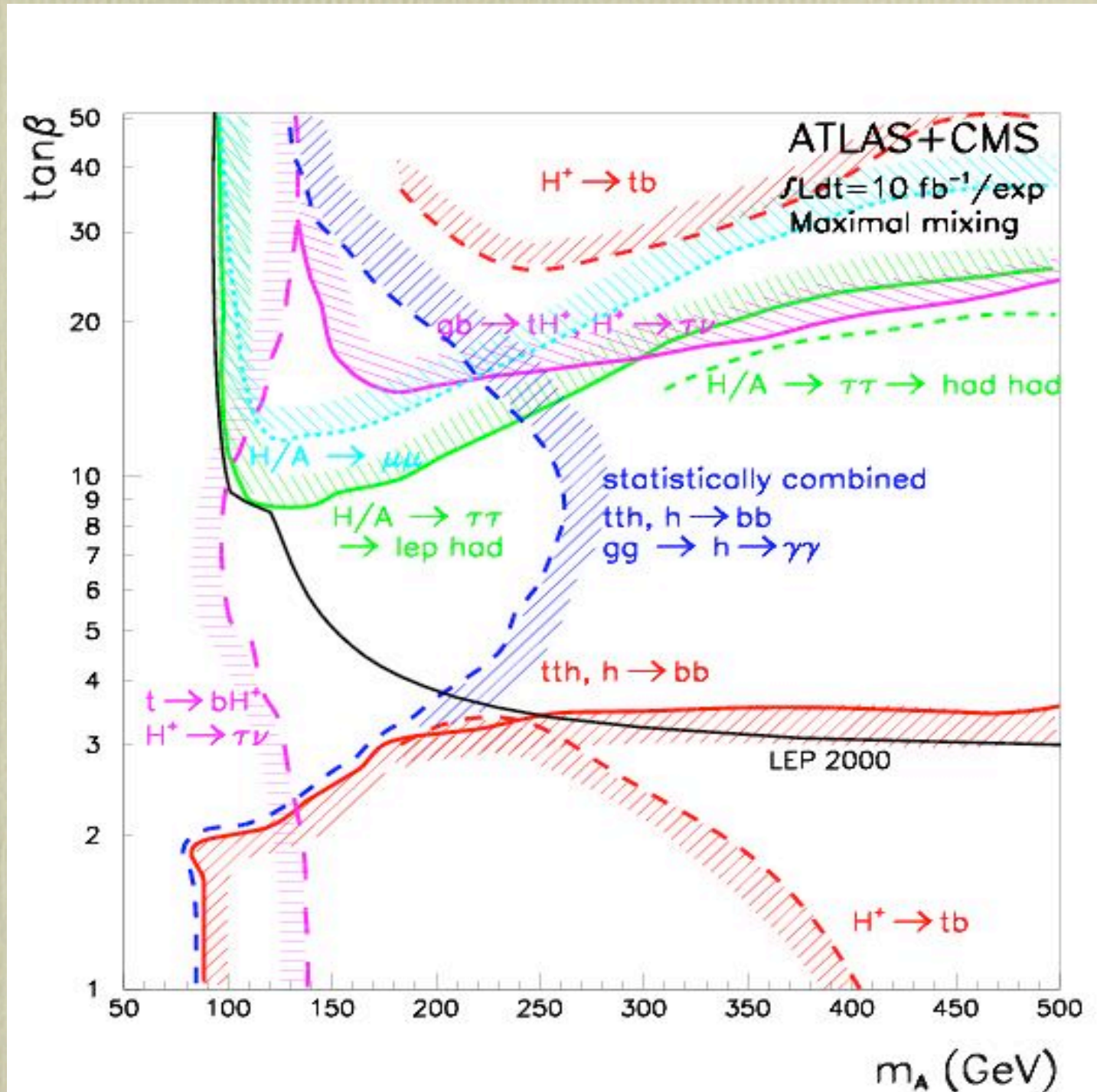
$H^\pm \rightarrow \tau\nu$

If SUSY particles
light enough:

- $H/A \rightarrow \chi_2^0 \chi_2^0 \rightarrow$

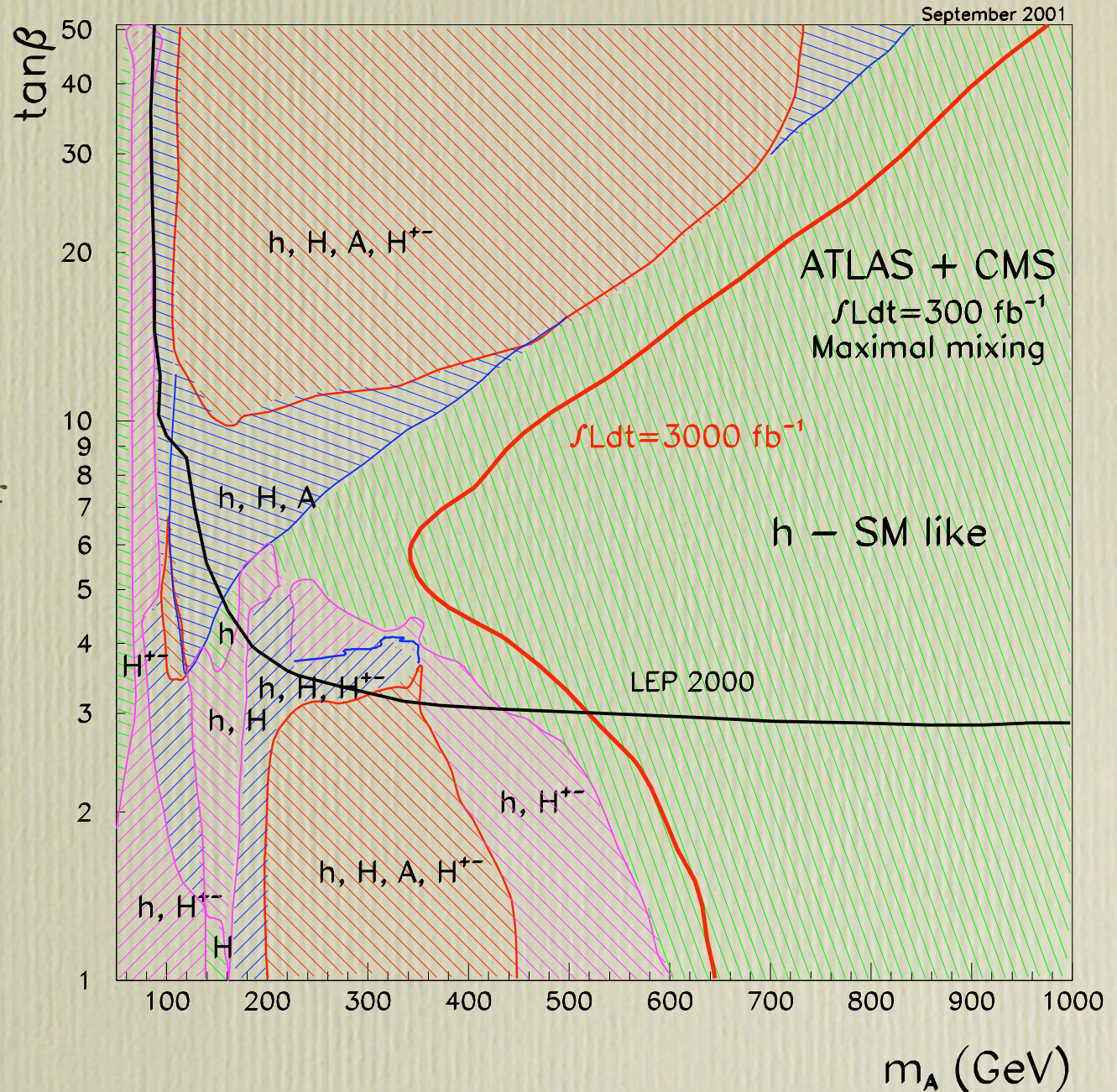
$\chi_1^0 \chi_1^0 + 4\text{lept}'s$

- h produced in
cascade decays

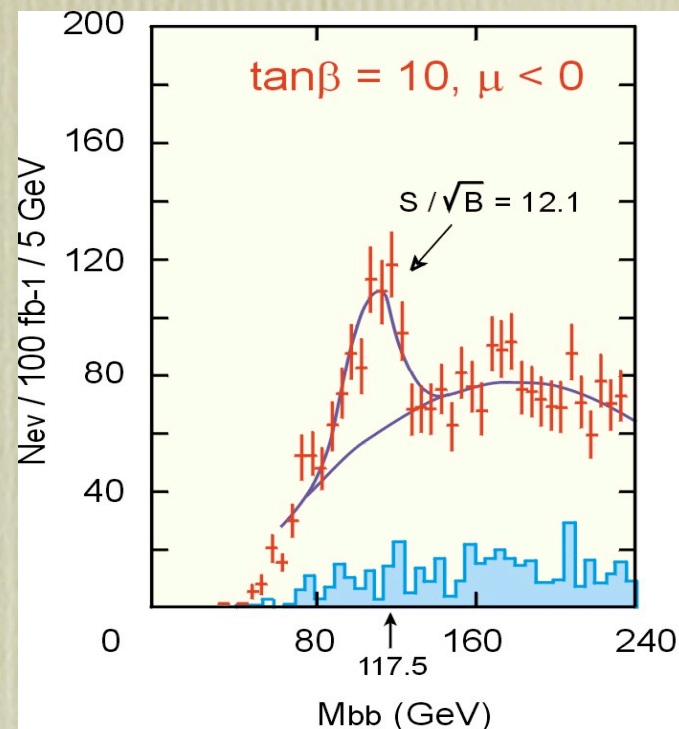
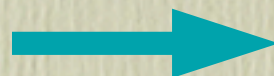
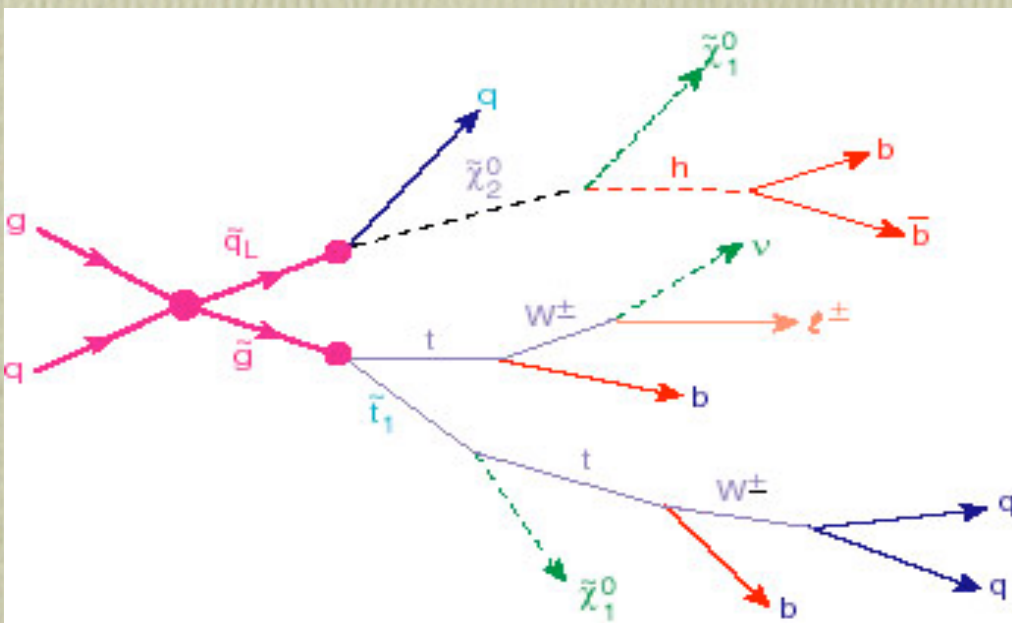


For a large fraction of the parameter space with $m_A < 500 \text{ GeV}$, more than one Higgs bosons will be visible with the expected luminosity

Higgs particles which can be observed with $>5\sigma$ in different areas of m_A - $\tan\beta$ parameter space



Example, h production in cascade decays



Supersymmetry: what, why, where

- Spectrum doubling: one bosonic degree of freedom (dof) of for each fermionic dof, and viceversa
- enhanced relations among and constraints on couplings/masses
- space-time Lorentz symmetry \Rightarrow particle \leftrightarrow antiparticle
- space-time Supersymmetry \Rightarrow particle \leftrightarrow sparticle
- SUSY has a priori fewer parameters than non-SUSY:
 - $m(\text{particle})=m(\text{sparticle})$
 - $\text{couplings}(\text{particle})=\text{couplings}(\text{sparticle})$
 - Higgs selfcoupling (λ) related to weak gauge coupling:
$$\lambda \mu^4 \sim g_w \mu^4$$
- All complexity and parameter proliferation of SUSY are just a consequence of SUSY breaking (SSB)!!

- A minimal SUSY extension of the SM, with arbitrary pattern of spontaneous SUSY breaking, has over 100 extra parameters (scalar and gauge-fermion masses, mixings among SUSY partners of quarks and leptons)
- This is not much worse than an arbitrary extension to leptons and hadrons of Fermi's theory of weak interactions, before Feynman, Gell-Mann and Cabibbo, or even before LEP/SLC firmly established the parameters of the SM. One could have needed parameters to describe:
 - non V-A couplings (S, P, T, V+A)
 - non-universal couplings to hadronic currents, and to W or T currents
 - more complex Higgs structures
 - different realisations of EWSB
- Therefore parameter proliferation in SUSY is most likely the consequence of our current ignorance of the specific dynamics leading to SUSY breaking.

Benchmark goal for SUSY studies at the LHC:

GET CLUES ON THE MECHANISM OF SUSY BREAKING

The accuracy of SUSY measurements at the LHC should be gauged by the above goal:

is the accuracy sufficient to discriminate among different SSB models?

Supersymmetry breaking: constraints

- No SUSY observed as yet: Susy particles must have masses typically larger than 100 GeV
- Nevertheless they cannot be arbitrarily large, to prevent the artificial fine tuning which justified SUSY in first place:

$$m_{\tilde{p}} \not\gg 1 \text{ TeV}$$

- Generic Susy breaking (SSB) leads to unacceptable FCNC. Therefore need to require suppressed FCNC (Flavour conservation is to SUSY what GIM has been for the SM):

$$\epsilon_K \sim \left(\frac{100 \text{ TeV}}{m_{\tilde{q}}} \right)^2 \text{Im} \left(\frac{\epsilon m_{\tilde{d}_L \tilde{s}_L}^2}{m_{\tilde{d}}^2} \frac{\epsilon m_{\tilde{d}_R \tilde{s}_R}^2}{m_{\tilde{d}}^2} \right) < 2 \cdot 10^{-3}$$

$$\mu \not\rightarrow e \Rightarrow \sin 2\epsilon_{\tilde{e}\tilde{\mu}} \frac{\epsilon m_{\tilde{e}\tilde{\mu}}^2}{m_{\tilde{e}}^2} < 0.01$$

Supersymmetry breaking models: minimal Supergravity

SUSY breaking at an intermediate scale:

$$M_{SSB} \sim \sqrt{m_W m_{Plank}} \sim 10^{11} \text{ GeV}$$

Universal scalar and fermion SSB masses at the Planck scale:

$$m_H = m_0$$

$$m_{\tilde{V}} = m_{1/2} \quad \forall V = g, \square, W, Z$$

Implications:

- mass splitting at EW scale induced radiatively \Rightarrow no FCNC problems
- mass squared for H naturally driven negative by large top Yukawa coupling
- correlation between Higgs and gaugino masses
- correlations between different gaugino masses:

$$m(\tilde{g})/m(\square) \sim \square_s/\square_W$$

$$m(\tilde{B}) = (5g'^2/3g^2) m(\tilde{W}) \sim 0.5m(\tilde{W})$$

Supersymmetry breaking models: gauge-mediated SSB

SUSY breaking in a strongly coupled sector, transferred to the low energy sector only via gauge interactions at an intermediate scale:

$$m_{\text{SSB}} \sim 1\text{-}100 \text{ TeV}$$

Consequences:

- SSB flavour independent \Rightarrow no FCNC problems
- Relations among SSB parameters determined by gauge couplings:

$$\frac{m(\tilde{q})}{m(\tilde{\ell})} \sim \frac{\alpha_s}{\alpha_w} \gg 1, \quad \text{unlike SUGRA}$$

$$\frac{m(\tilde{g})}{m(\tilde{\square})} \sim \frac{\alpha_s}{\alpha_w}, \quad \text{like SUGRA}$$

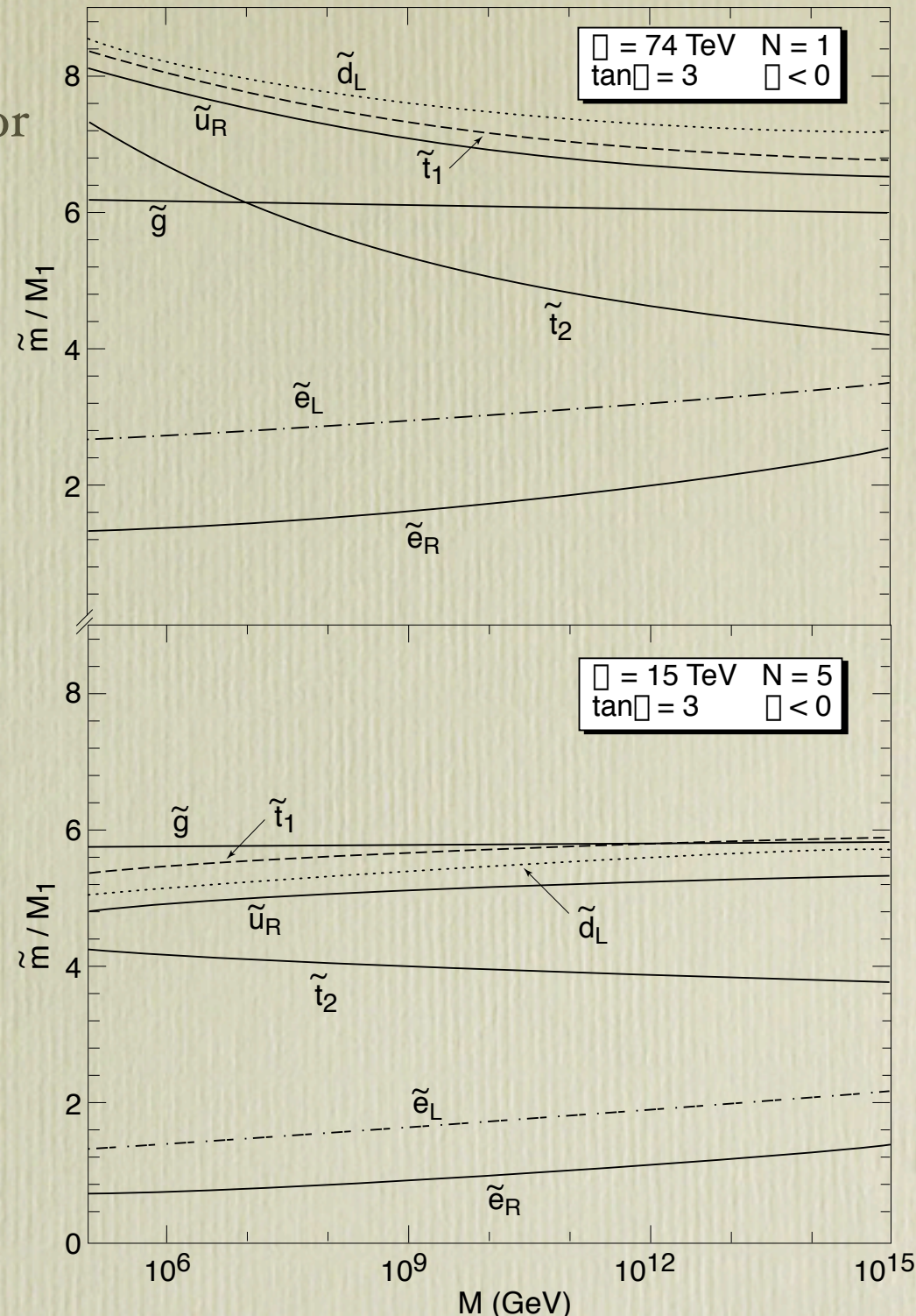
$$m(\tilde{q}) \sim m(\tilde{g}), \quad m(\tilde{\ell}) \sim m(\tilde{\square})$$

$$m(\tilde{\square}_1^\pm) \sim m(\tilde{\square}_2^0)$$

- gravitino as Lightest SUSY Particle:

$$\tilde{\square}^0 \rightarrow \tilde{G}\tilde{\square} \quad \text{or} \quad \tilde{\ell} \rightarrow \tilde{G}l$$

depending on which is the NLSP

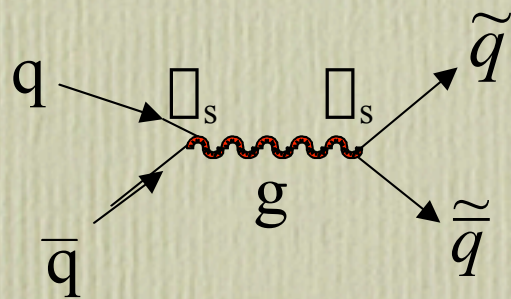


In conclusion:

- The exploration of the SUSY spectrum provides invaluable information on the physics at scales much larger than the LHC's.
- Indications of a mSUGRA-like spectrum would set the scale of SSB at 10^{11} GeV, and would provide indication of no interesting phenomena up to that scale
- Indications of a GMSB-like spectrum would indicate the existence of new phenomena at a scale of the order of 10-100-TeV
- The most valuable information will come from the comparison of
 - gaugino masses (gluino vs. charginos vs. neutralinos)
 - scalar masses (SU(2) doublet (L-type) vs singlet (R-type) scalars, squarks vs sleptons, 1st generation vs 2nd and 3rd)
 - of particular interest is the value of the stop mass, because of its connection with the Higgs mass

Production of SUSY particles

- Discrete quantum number, $R=1$ for “normal” particles, $R=-1$ for SUSY states. If R conserved:
 - pair production.
 - lightest SUSY particle is stable (\Rightarrow Dark matter candidate)
- Strongly interacting (squarks -- e.g. stops, gluinos):

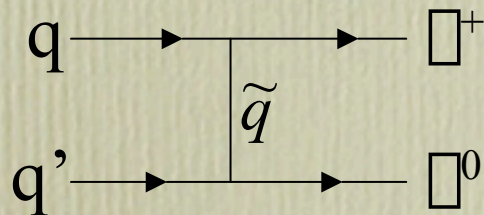


A Feynman diagram showing the production of a squark (\tilde{q}) and a gluino (\tilde{g}) through a quark loop. An incoming gluon (g) and a quark (q) interact via a loop of a squark (\tilde{q}) and a gluon (g). The final state consists of a squark (\tilde{q}) and a gluino (\tilde{g}).

$$m_{\tilde{q},\tilde{g}} \sim 1 \text{ TeV} \Rightarrow \sigma \sim 1 \text{ pb}^{-1}$$

$$\Rightarrow 10^4 \text{ events/yr}$$

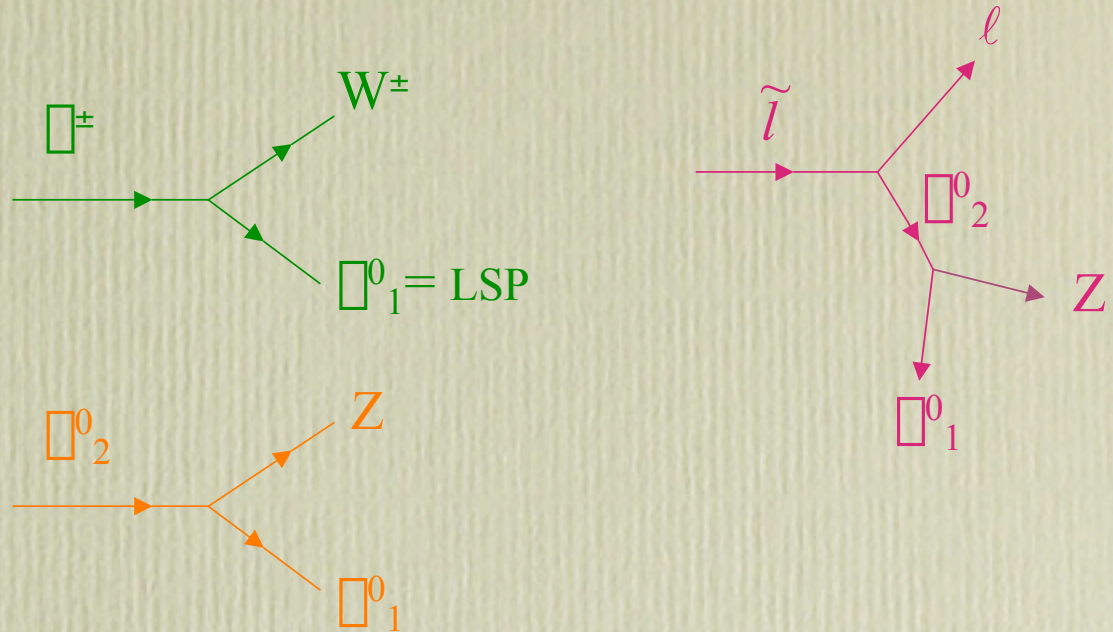
- Weakly interacting (photino, W -ino, Z -ino, higgsino \Rightarrow charginos/neutralinos)



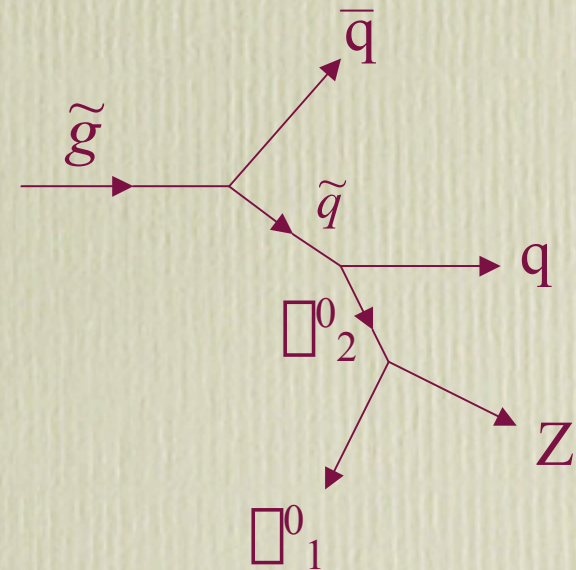
$$m_{\tilde{\chi}} \sim 150 \text{ GeV} \Rightarrow \sigma \sim 1 \text{ pb}^{-1}$$

Decays of SUSY particles

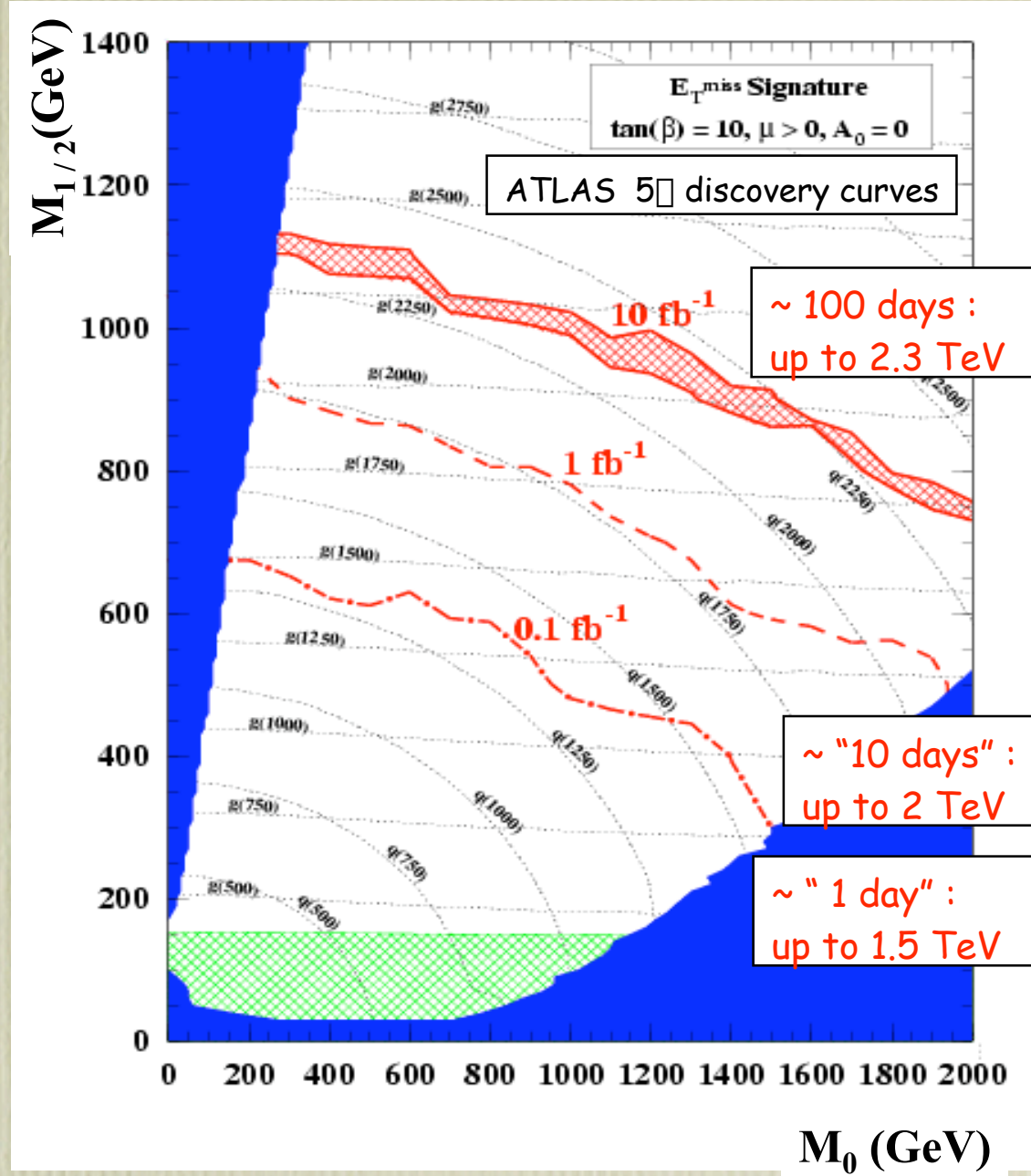
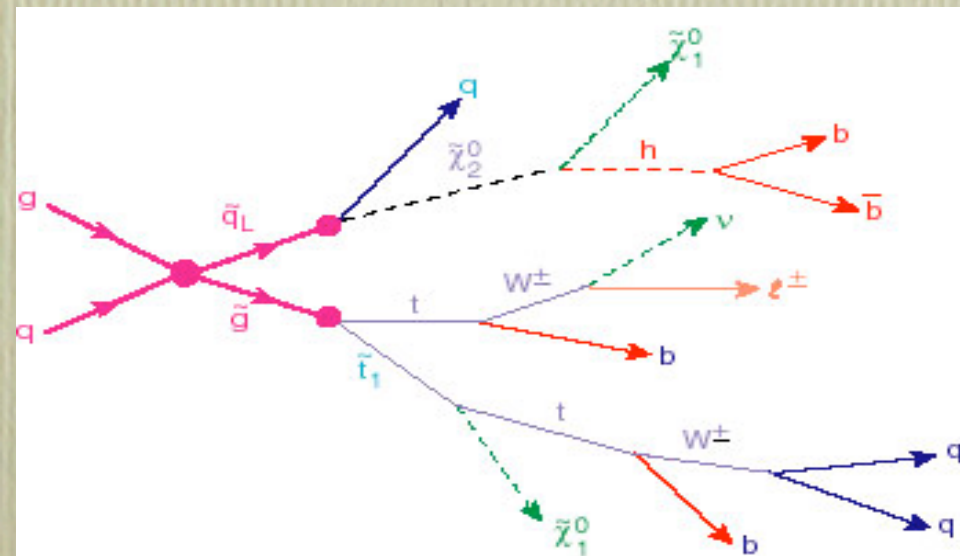
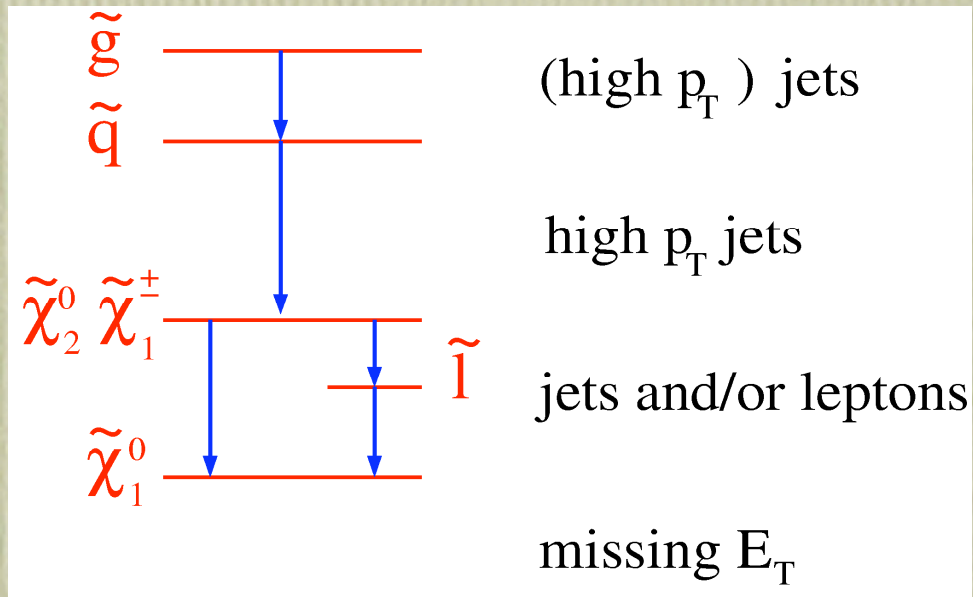
- weakly interacting:



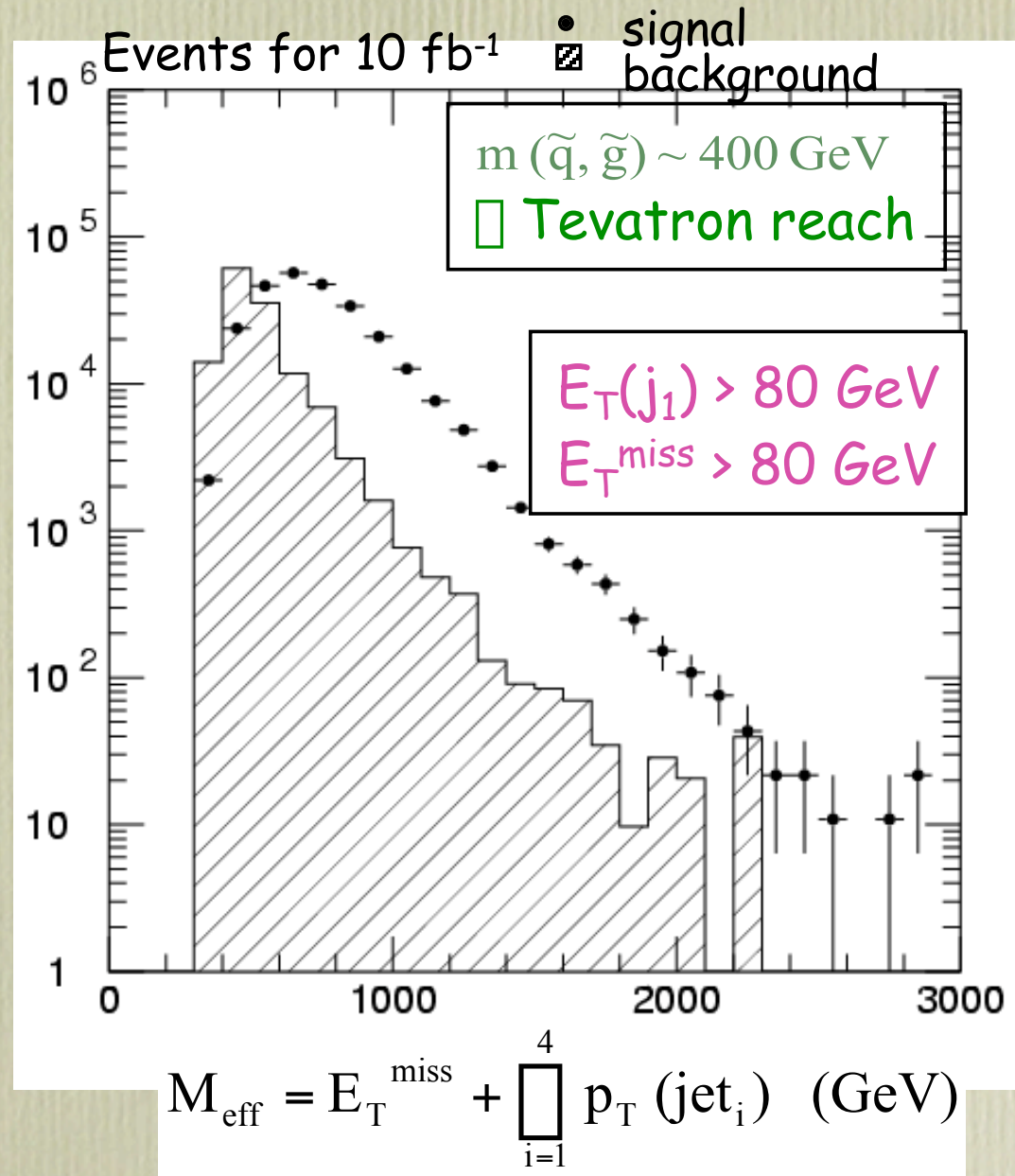
- strongly interacting: for massive states spectacular multi-body chain decays, possibly including EW sparticles, enhancing their production rate. Very difficult, but possible, to disentangle the full spectroscopy!



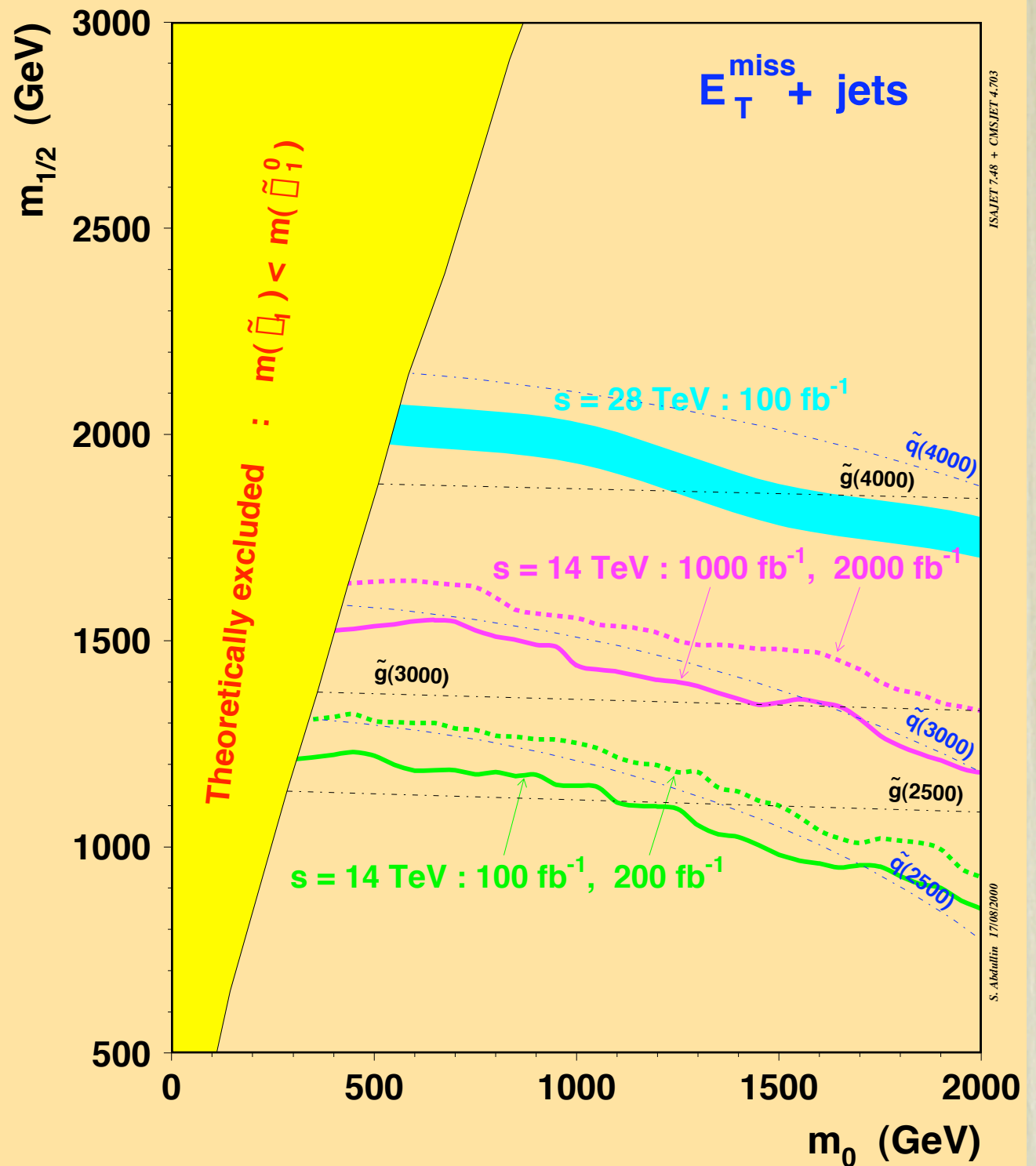
SUSY searches at the LHC



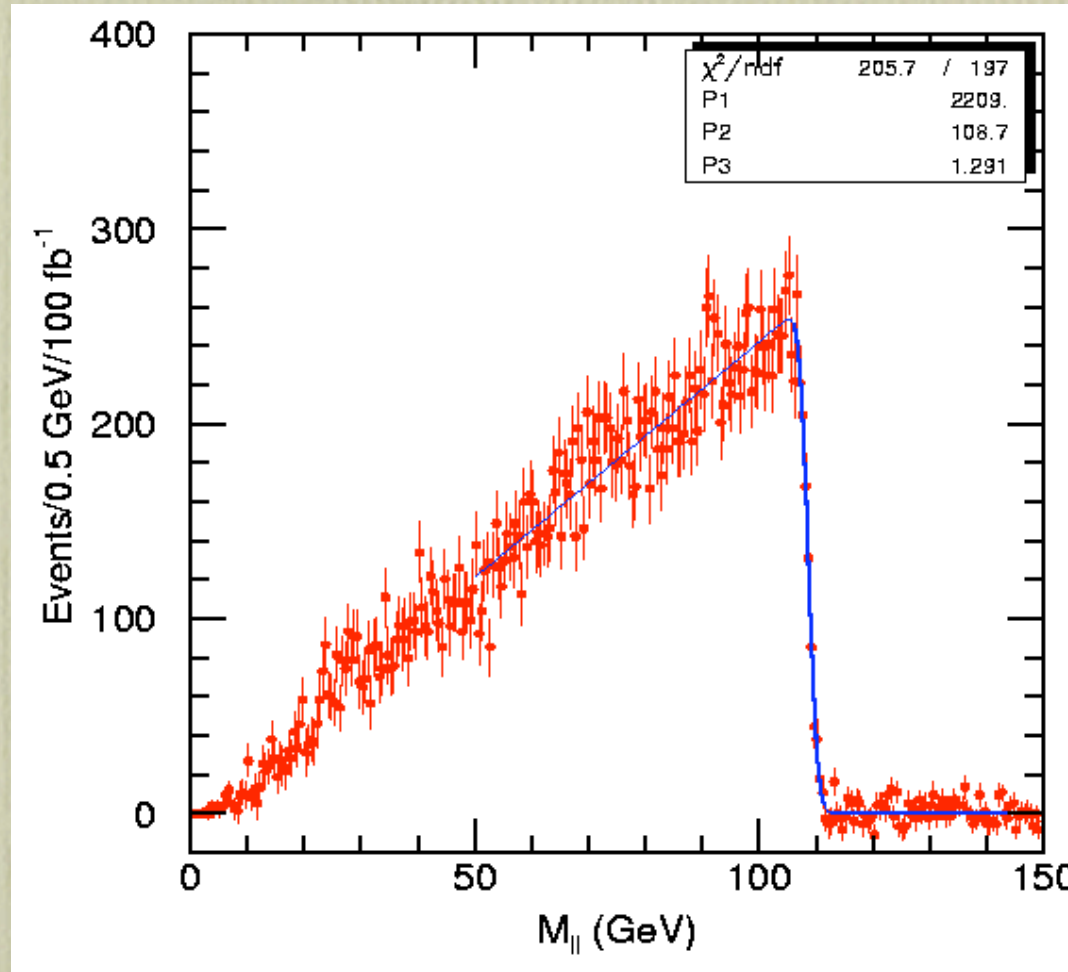
Low-mass matching with Tevatron's discovery reach: trigger thresholds!



Discovery reach
for mSUGRA
models, with
various
luminosity and
CM energy
options



$$\Box_2^0 \rightarrow \tilde{\ell}^\pm \ell^\mp \rightarrow \Box_1^0 \ell^+ \ell^-$$



$$\max(m(\ell^+ \ell^-)) = m(\Box_2) \sqrt{\frac{m^2(\Box_2) - m^2(\tilde{\ell})}{m^2(\Box_2)}} \sqrt{\frac{m^2(\tilde{\ell}) - m^2(\Box_1)}{m^2(\ell)}}$$

Examples of measurement accuracies for a specific model, in ATLAS:

| Measurement | Expected value (GeV) | Error (%) 300 fb ⁻¹ |
|------------------------------|-------------------------|-----------------------------------|
| m_0 | 100 GeV | ±3 |
| $m_{1/2}$ | 300 GeV | ±1.3 |
| $\tan\beta$ | 2.1 | ±2 |
| m_h | 93 | ±0.2 |
| $m_{\ell^+\ell^-}$ end-point | 109 | ±0.2 |
| $m_{\tilde{\ell}_R}$ | 157 | ±0.3 |
| $m_{\tilde{\ell}_L}$ | 240 | ±1 |
| $m_{\tilde{q}_L}$ | 690 | ±1 |
| $m_{\tilde{q}_R}$ | 660 | ±1.5 |
| $m_{\tilde{g}}$ | 770 | ±1.5 |
| $m_{\tilde{t}_1}$ | 490 | ±10 |

Summary of LHC physics potential

- Quark substructure:
 - probed in high-transverse momentum, large-angle quark-quark scattering; measure the deviation from point-like rate. Push the “size” of the quark down by more than one order of magnitude w.r.t. today
- New gauge interactions, e.g. right-handed W bosons, extra $U(1)$'s (as present in string theories), etc.
 - probed in $pp \rightarrow l+l^-$ or jet-jet, searching for peaks in the invariant-mass spectrum. Can test presence of interactions with EW-like strength up to 5-6 TeV
- Discover the Higgs boson over the domain up to 1 TeV, and determine to 10-20% the value of several of its couplings
- Detect several Higgses, if SUSY, over a good fraction of parameter space

- Measure the anomalous couplings of gauge bosons, and test for possible deviations from EW dynamics at scales up to several TeV.
- Provide first key measurements of SUSY parameters:
 - $m(\text{gluino}), m(\text{chargino}) \rightarrow$ test possible GUT relations, adding to evidence of GUT from gauge coupling unification
- Assess whether the neutralino accounts for DM
- Explore in unprecedented detail the physics of b-flavour: rare BR's to $1/10^9$, deviations from unitarity of the CKM mixing matrix. Potential to test the presence of virtual SUSY particles in loop-mediated decays, such as $B_s \rightarrow \mu^+ \mu^-$, $b \rightarrow s[\dots]$
- Ready to detect the unexpected!

Conclusions

- Many independent probes of the frontier of physics exist or are being built:
 - Cosmology: WMAP, Planck, SN, Digital Sloan, Dark Matter searches ...
 - Astrophysics: Gravitational wave detectors, VHE cosmic ray arrays, ...
 - Gravity: measurements of deviations from Newton's law
 - Low-energy precision tests: $g-2$, K physics, B-physics, Atomic Parity Violation, etc
 - and more.....
- Indirect observation of possibly revolutionary indications of new physics, however, are no substitute for the direct observation of the particles responsible for this new physics:
 - which particle is associated to DM?
 - what is the field-theory origin of the inflaton? of the quintessence?
 - what is giving $g-2$ different than expected?
- The next generation of accelerators will be extremely expensive (time and \$\$), and input from the LHC results will be crucial to define the future directions of the field.
- We unfortunately still don't know of alternatives to the quest for the most basic laws of Nature other than HEP collisions.
- **LHC is a crucial step forward in this quest.**